

# Frequency Selective Surface, Periodic Complementary Split Ring Resonator

Frequency selective surfaces (FSS) are periodic structures with a bandpass or a bandstop frequency response. This example shows that only signals around the center frequency can pass through the periodic complementary split ring resonator layer.

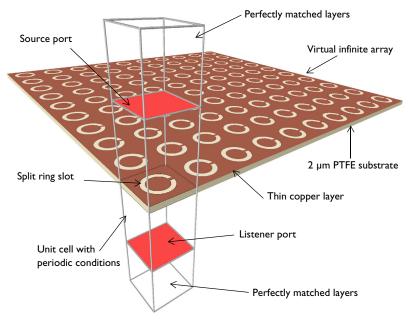


Figure 1: One unit cell of the complementary split ring resonator is modeled with periodic boundary conditions to simulate an infinite 2D array. Perfectly matched layers at the top and bottom of the unit cell absorb the excited and higher order modes.

# Model Definition

A split ring slot is patterned on a geometrically thin copper layer that sits on a 2 µm PTFE substrate (Figure 1). The copper layer is much thicker than the skin depth in the simulated frequency range, so it is modeled as a perfect electric conductor (PEC). The rest of the simulation domain is filled with air.

Floquet-periodic boundary conditions are used on four sides of the unit cell to simulate the infinite 2D array. Perfectly matched layers (PMLs) on the top and bottom of the unit cell absorb the excited mode from the source port and any higher order modes generated by the periodic structure. The PMLs attenuate the wave as it propagates in the direction perpendicular to the PML boundary. Since the model is solved for a range of incident

angles, the wavelength in the PMLs is set to  $2\pi/|k_0\cos\theta|$ . This accounts for the angular dependence of the normal component of the wave vector inside the PMLs.

Port boundary conditions are placed on the interior boundaries of the PMLs, adjacent to the air domains. The Port boundary conditions automatically determine the reflection and transmission characteristics in terms of S-parameters. The interior port boundaries with PML backing require the slit condition. A slit condition means that the dependent variable can have different values on the two sides of the boundary. The port orientation is specified to define the inward direction for the S-parameter calculation. Since higher-order diffraction modes are not of particular interest in this example, the combination of a domain-backed type slit port and PMLs is used instead of adding a diffraction order port for each diffraction order and polarization.

The periodic boundary condition requires identical surface meshes on paired boundaries. This is accomplished in two steps: first by creating a mesh on only one of the boundaries and then using the Copy Face operation for the mesh on the other boundary. This mesh configuration is automatically set when using the physics-controlled mesh as shown in the step-by-step instructions. If you are interested in seeing more details about the mesh, build the physics-controlled mesh once and then change the mesh sequence type to the usercontrolled mesh in the mesh settings. Then you can inspect the generated mesh sequence.

The periodic conditions are split by the ports, having the slit conditions. To make sure that the periodic conditions couples the correct dependent variables on the two sides of the slit condition, multiple periodic conditions are defined—both in front of the port and behind the port.

## Results and Discussion

The modified multislice default plot (Figure 2) shows the electric field norm on the complimentary split ring resonator. Strong fields are observed inside the slot. The Sparameter plot in Figure 3 shows that this periodic structure functions as a bandpass filter near 4.6 THz. In Figure 4, the S-parameters appear as a function of incident angle and show that the periodic structure is penetrable at 4.6 THz over the simulated range, except for grazing angles.

The resonance frequency of this periodic structure can be quickly evaluated as 4.59 THz using an Eigenfrequency study, which is not included in this example.

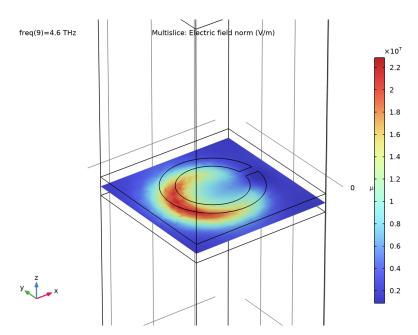


Figure 2: The fields are confined in the split ring slot.

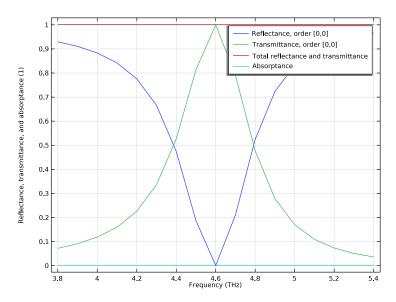


Figure 3: The S-parameter plot shows a bandpass resonance near 4.6 THz.

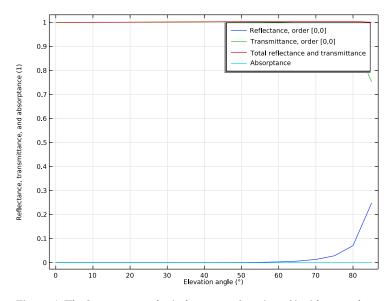


Figure 4: The S-parameter plot is shown as a function of incident angle.

**Application Library path:** Wave\_Optics\_Module/Gratings\_and\_Metamaterials/frequency\_selective\_surface\_csrr

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 1 3D.
- 2 In the Select Physics tree, select Optics>Wave Optics>Electromagnetic Waves, Frequency Domain (ewfd).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click M Done.

## STUDY I

## Steb 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type range (3.8[THz], 0.1[THz], 5.4[THz]).

## **GLOBAL DEFINITIONS**

#### Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
theta	O[deg]	0 rad	Elevation angle

#### **GEOMETRY I**

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose µm.

Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 15.
- 4 In the **Depth** text field, type 15.
- 5 In the Height text field, type 45.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 Click **Pauld Selected**.
- 8 Click the Wireframe Rendering button in the Graphics toolbar.

Work Plane I (wbl)

In the Geometry toolbar, click Work Plane.

Work Plane I (wb I)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wbl)>Circle I (cl)

- I In the Work Plane toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 5.
- 4 Click **Build Selected**.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Work Plane I (wp I)>Circle 2 (c2)

- I In the Work Plane toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 3.5.

Work Plane I (wp I)>Rectangle I (r I)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 4.

- 4 Locate the Position section. From the Base list, choose Center.
- 5 In the xw text field, type 4.

Work Plane I (wpl)>Difference I (difl)

- I In the Work Plane toolbar, click Booleans and Partitions and choose Difference.
- 2 Select the object cl only.
- 3 In the Settings window for Difference, locate the Difference section.
- 4 Find the Objects to subtract subsection. Click to select the Activate Selection toggle button.
- 5 Select the objects c2 and r1 only.
- 6 Click **P** Build Selected.

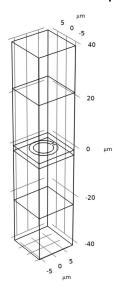
Block 2 (blk2)

- I In the Model Builder window, right-click Geometry I and choose Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 15.
- 4 In the **Depth** text field, type 15.
- 5 In the Height text field, type 2.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the z text field, type -1.

Block 3 (blk3)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 15.
- 4 In the **Depth** text field, type 15.
- 5 In the Height text field, type 80.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 Click Build All Objects.

**8** Click the **Zoom Extents** button in the **Graphics** toolbar.





## ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD)

Wave Equation, Electric 1

- I In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (ewfd) click Wave Equation, Electric 1.
- 2 In the Settings window for Wave Equation, Electric, locate the Electric Displacement Field section.
- 3 From the Electric displacement field model list, choose Relative permittivity.

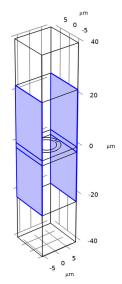
Perfect Electric Conductor 2

- I In the Physics toolbar, click **Boundaries** and choose Perfect Electric Conductor.
- 2 Select Boundary 12 only.

Use Floquet-periodic conditions on all side boundaries.

Periodic Condition I

2 Select Boundaries 4, 7, 10, and 24–26 only.

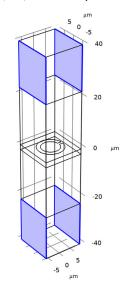




- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.
- 5 From the k-vector for Floquet periodicity list, choose From periodic port.

## Periodic Condition 2

2 Select Boundaries 1, 13, 23, and 27 only.

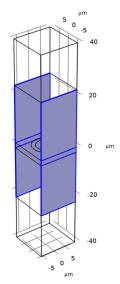




- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.
- 5 From the k-vector for Floquet periodicity list, choose From periodic port.

## Periodic Condition 3

**2** Select Boundaries 5, 8, 11, and 18–20 only.

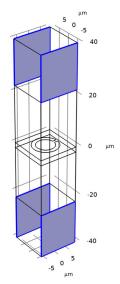




- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.
- 5 From the k-vector for Floquet periodicity list, choose From periodic port.

## Periodic Condition 4

2 Select Boundaries 2, 14, 17, and 21 only.





- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.
- 5 From the k-vector for Floquet periodicity list, choose From periodic port.

The wave is excited from the port on the top.

## Port I

- I In the Physics toolbar, click **Boundaries** and choose Port.
- 2 Select Boundary 15 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Periodic. For the first port, wave excitation is **on** by default.
- 5 Select the Activate slit condition on interior port check box.
- 6 From the Slit type list, choose Domain-backed.
- 7 Click Toggle Power Flow Direction.
- 8 Locate the Port Mode Settings section. From the Input quantity list, choose Magnetic field.

**9** Specify the  $\mathbf{H}_0$  vector as

0	x
1	у
0	z

**IO** In the  $\alpha_1$  text field, type theta.

The maximum frequency in the setting window will be used only when **Compute** Diffraction Order button is clicked to generate Diffraction Order features handling higher order mode individually. In this model, PML absorbs all higher order modes, so this setting is ineffective.

#### Port 2

- I In the Physics toolbar, click **Boundaries** and choose Port.
- 2 Select Boundary 6 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Periodic.
- 5 Select the Activate slit condition on interior port check box.
- 6 From the Slit type list, choose Domain-backed.
- 7 Click Toggle Power Flow Direction.
- 8 Locate the Port Mode Settings section. From the Input quantity list, choose Magnetic field.
- **9** Specify the  $\mathbf{H}_0$  vector as

0	x
1	у
0	z

Scattering Boundary Condition I

- In the Physics toolbar, click **Boundaries** and choose Scattering Boundary Condition.
- 2 Select Boundary 3 only.

## DEFINITIONS

Perfectly Matched Layer I (pml1)

- I In the Definitions toolbar, click M. Perfectly Matched Layer.
- 2 Select Domain 5 only.

- 3 In the Settings window for Perfectly Matched Layer, locate the Scaling section.
- 4 From the Typical wavelength from list, choose User defined.
- 5 In the Typical wavelength text field, type 2\*pi/abs(ewfd.k0\*cos(theta)).

# Perfectly Matched Layer 2 (pml2)

- I In the Definitions toolbar, click Perfectly Matched Layer.
- 2 Select Domain 1 only.
- 3 In the Settings window for Perfectly Matched Layer, locate the Scaling section.
- 4 From the Typical wavelength from list, choose User defined.
- 5 In the Typical wavelength text field, type 2\*pi/abs(ewfd.k0\*cos(theta)).

## ADD MATERIAL

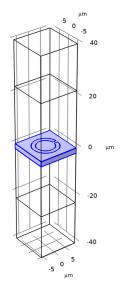
- I In the Home toolbar, click 👯 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 4 Add Material to close the Add Material window.

## MATERIALS

## Material 2 (mat2)

I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.

# **2** Select Domain 3 only.





- 3 In the Settings window for Material, locate the Material Contents section.
- **4** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	2.1	I	Basic
Relative permeability	mur_iso; murii = mur_iso, murij = 0	1	I	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

## MESH I

- I In the Model Builder window, under Component I (compl) right-click Mesh I and choose **Build All.**
- 2 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 3 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.

- 4 From the Element size list, choose Extremely fine.
- 5 Click Build All.

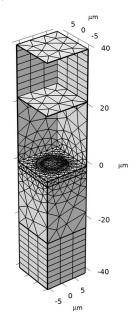
## DEFINITIONS

Hide for Physics 1

- I In the Model Builder window, right-click View I and choose Hide for Physics.
- 2 In the Settings window for Hide for Physics, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundaries 10, 11, 13, and 14 only.

## MESH I

In the Model Builder window, click Mesh 1.





## STUDY I

In the **Home** toolbar, click **Compute**.

## RESULTS

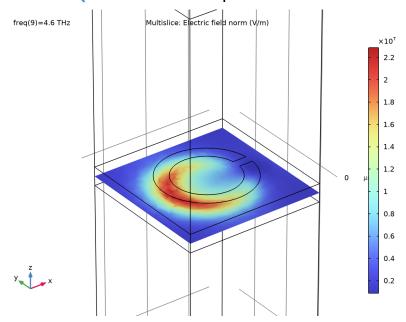
Electric Field (ewfd)

I In the Settings window for 3D Plot Group, locate the Data section.

2 From the Parameter value (freq (THz)) list, choose 4.6.

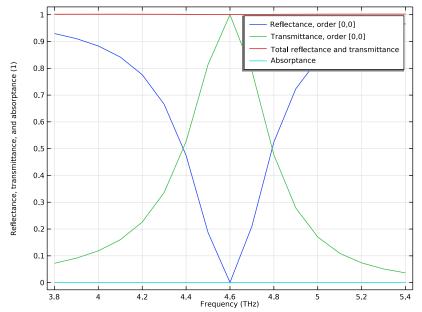
## Multislice 1

- I In the Model Builder window, expand the Electric Field (ewfd) node, then click Multislice 1.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the X-planes subsection. In the Planes text field, type 0.
- 4 Find the Y-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. From the **Entry method** list, choose **Coordinates**.
- 6 In the Coordinates text field, type -1.
- 7 In the Electric Field (ewfd) toolbar, click Plot.
- 8 Click the **Q** Zoom In button in the Graphics toolbar twice.



This reproduces Figure 2.





Identify the resonant frequency of the periodic structure from the S-parameter plot Figure 3.

Next, evaluate the reflectivity and transmittivity performance of the model with different incident angles.

## ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.

## STUDY I

Solver Configurations

- I Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 2 Click Add Study in the window toolbar. If you want to clear the Add Study window after adding, click Add Study again in the Home toolbar.
- 3 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 2

## Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
theta (Elevation angle)	range(0[deg],5[deg], 85[deg])	rad

# Step 1: Frequency Domain

- I In the Model Builder window, click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- **3** In the **Frequencies** text field, type **4.6**[THz].
- 4 In the Study toolbar, click = Compute.

## RESULTS

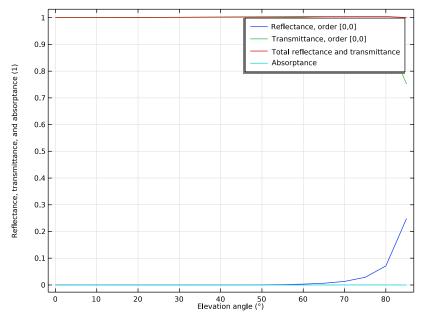
## Multislice 1

- I In the Model Builder window, expand the Electric Field (ewfd) I node, then click Multislice 1.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the X-planes subsection. In the Planes text field, type 0.
- 4 Find the Y-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. From the **Entry method** list, choose **Coordinates**.
- 6 In the Coordinates text field, type -1.

## Global I

- I In the Model Builder window, expand the Results>Reflectance, Transmittance, and Absorptance (ewfd) I node, then click Global I.
- 2 In the Settings window for Global, locate the x-Axis Data section.
- 3 From the **Unit** list, choose °.





This is the S-parameter plot as a function of incident angle shown in Figure 4.

Analyze the same model with a much finer frequency resolution using Adaptive Frequency **Sweep** based on asymptotic waveform evaluation (AWE). When a device presents a slowly varying frequency response, the AWE provides a faster solution time when running the simulation on many frequency points. The following example with the AWE can be computed 50 times faster than regular Frequency Domain sweeps with a same finer frequency resolution.

## ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD)

## Port 1

- I In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (ewfd) click Port I.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 Click **Create Selection**.
- 4 In the Create Selection dialog box, type Port 1 in the Selection name text field.
- 5 Click OK.

#### Port 2

- I In the Model Builder window, click Port 2.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 Click Create Selection.
- 4 In the Create Selection dialog box, type Port 2 in the Selection name text field.
- 5 Click OK.

## ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Adaptive Frequency Sweep.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 3

Step 1: Adaptive Frequency Sweep

- I In the Settings window for Adaptive Frequency Sweep, locate the Study Settings section.
- 2 In the Frequencies text field, type range (3.8[THz], 0.01[THz], 5.4[THz]). Use a ten times finer frequency resolution.

A slowly varying scalar value curve works well for AWE expressions. When **AWE** expression type is set to Physics controlled in the Adaptive Frequency Sweep study settings, abs (comp1.ewfd.S21) is used automatically for two-port devices.

Because such a fine frequency step generates a memory-intensive solution, the model file size will increase tremendously when it is saved. When only the frequency response of port related variables are of interest, it is not necessary to store all of the field solutions. By selecting the Store fields in output check box in the Values of Dependent **Variables** section, we can control the part of the model on which the computed solution is saved. We only add the selection containing these boundaries where the port variables are calculated. The port size is relatively small compared to the entire modeling domain, and the saved file size with the fine frequency step is more or less that of the regular discrete frequency sweep model when only the solutions on the port boundaries are stored.

3 Locate the Values of Dependent Variables section. Find the Store fields in output subsection. From the Settings list, choose For selections.

- 4 Under Selections, click + Add.
- 5 In the Add dialog box, in the Selections list, choose Port I and Port 2.
- 6 Click OK.

It is necessary to include the port boundaries to calculate S-parameters. By choosing only the port boundaries for **Store fields in output** settings, it is possible to reduce the size of a model file a lot.

Step 1: Adaptive Frequency Sweep

- I In the Model Builder window, click Step I: Adaptive Frequency Sweep.
- 2 In the Home toolbar, click **Compute**.

#### RESULTS

Multislice 1

- I In the Model Builder window, expand the Electric Field (ewfd) 2 node.
- 2 Right-click Results>Electric Field (ewfd) 2>Multislice I and choose Delete.

Surface 1

In the Model Builder window, right-click Electric Field (ewfd) 2 and choose Surface.

Selection 1

- I In the Model Builder window, right-click Surface I and choose Selection.
- **2** Select Boundaries 6 and 15 only.

Reflectance, Transmittance, and Absorptance (ewfd) 2

- I In the Model Builder window, under Results click Reflectance, Transmittance, and Absorptance (ewfd) 2.
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 From the Position list, choose Lower right.

Global I

- I In the Model Builder window, expand the Reflectance, Transmittance, and Absorptance (ewfd) 2 node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.

**3** In the table, enter the following settings:

Expression	Unit	Description
ewfd.Rorder_0_0	1	S11 Adaptive Frequency Sweep
ewfd.Torder_0_0	1	S21 Adaptive Frequency Sweep

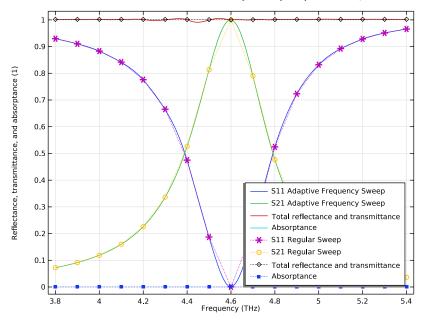
## Global 2

- I Right-click Results>Reflectance, Transmittance, and Absorptance (ewfd) 2>Global I and choose **Duplicate**.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
ewfd.Rorder_0_0	1	S11 Regular Sweep
ewfd.Torder_0_0	1	S21 Regular Sweep

- 4 Locate the Data section. From the Dataset list, choose Study I/Solution I (soll).
- 5 Click to expand the Coloring and Style section. Find the Line style subsection. From the Line list, choose Dotted.
- 6 Find the Line markers subsection. From the Marker list, choose Cycle.





Array 3D I

These final instructions create a 3D plot of the frequency selective surface. A 3D array dataset is used to generate the periodic pattern.

- I In the Results toolbar, click More Datasets and choose Array 3D.
- 2 In the Settings window for Array 3D, locate the Array Size section.
- **3** In the **X size** text field, type 16.
- 4 In the Y size text field, type 16.

# Arrayed Field Plot

- I In the Results toolbar, click 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Arrayed Field Plot in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Array 3D 1.
- 4 From the Parameter value (freq (THz)) list, choose 4.6.
- 5 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 6 Locate the Plot Settings section. Clear the Plot dataset edges check box.
- 7 Locate the Color Legend section. Clear the Show legends check box.

8 Click the Show Axis Orientation button in the Graphics toolbar.

## Surface I

- I Right-click Arrayed Field Plot and choose Surface.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Thermal>HeatCameraLight in the tree.
- 5 Click OK.
- 6 In the Settings window for Surface, locate the Coloring and Style section.
- 7 From the Color table transformation list, choose Reverse.

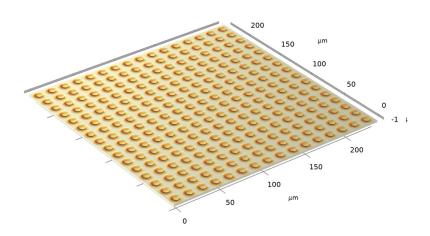
#### Filter I

- I Right-click Surface I and choose Filter.
- 2 In the Settings window for Filter, locate the Element Selection section.
- 3 In the Logical expression for inclusion text field, type  $z \ge -2.05[\mu m]$  &&  $z \le 0$ .

## Deformation I

- I In the Model Builder window, right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the **z-component** text field, type ewfd.normE.
- 4 Locate the Scale section.
- 5 Select the Scale factor check box. In the associated text field, type 0.5E-8.
- 6 In the Arrayed Field Plot toolbar, click Plot.

**7** Click the **Zoom Extents** button in the **Graphics** toolbar.



8 Click the **Q** Zoom In button in the Graphics toolbar, to better resolve the plot details. The following instruction shows how to use the Graph Marker subfeature to analyze 1D plots. When plotting transmittivity properties of a bandpass filter, the half-power bandwidth of the passband can be computed through a graph marker.

# Passband with Graph Marker

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Passband with Graph Marker in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 3/Solution 3 (sol3).

#### Global I

- I Right-click Passband with Graph Marker and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Ports>Transmittance, by order> ewfd.Torder\_0\_0 - Transmittance, order [0,0].

# Graph Marker I

I Right-click Global I and choose Graph Marker.

- 2 In the Settings window for Graph Marker, locate the Display section.
- 3 From the Display mode list, choose Bandwidth.
- 4 In the Cutoff value text field, type 0.5.
- 5 Locate the Text Format section. In the Display precision text field, type 3.
- **6** Select the **Include unit** check box.
- 7 Locate the Coloring and Style section. Select the Show frame check box.

