

Inflation of a Square Airbag

Introduction

The numerical treatment of thin structures with a membrane model is much simpler than with a shell model due to the assumption of zero bending stiffness. However, for some load cases this assumption is disadvantageous. For instance, when a membrane is subjected to compressive stresses, it may trigger wrinkling due to zero bending stiffness. This undesirable limitation can be overcame with the incorporation of a wrinkling model that removes these instabilities.

In this example, a squared airbag is inflated using an inner air pressure. The results are compared with the example presented in Ref. 1.

Model Definition

A squared airbag 6 mm in thickness and 1.2 m in diagonal length is inflated using a constant air pressure of 5 kPa. The membrane is modeled with an isotropic linear elastic material. The material properties given in Table 1 are taken from Ref. 1.

MATERIAL PROPERTIES

TABLE I: MATERIAL PROPERTIES.

Property	Variable	Isotropic Model
Young's modulus	E	588 MPa
Poisson's ratio	ν	0.4

Only a quarter of the square airbag is analyzed due to the intrinsic symmetry of the model.

Results and Discussions

Figure 1 shows the wrinkled regions in the inflated airbag. Apart from the central region, wrinkles develop everywhere.

The transverse displacement in the inflated airbag is shown in Figure 2. The variation of the principal stresses at the end of the inflation process is shown in the Figure 3 and Figure 4. The minimum value of the second principal stress is almost zero. Both figures show tensile principal stresses after inflation.

Figure 5 shows the displacement at various points versus the inflating pressure, these points are compared to the results given in Ref. 1. At the final pressure, the values match the reference values very well. Similarly, Figure 6 shows the variation of the first principal (tensile) stress at the midpoint versus the inflating pressure. The result also matches the reference value given in Ref. 1.

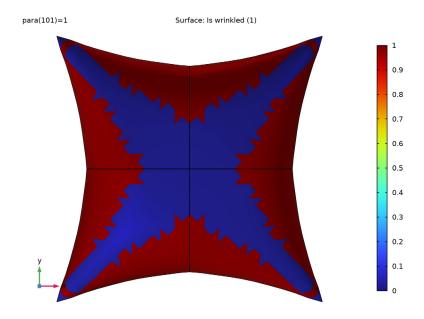


Figure 1: Wrinkled region in the inflated airbag.

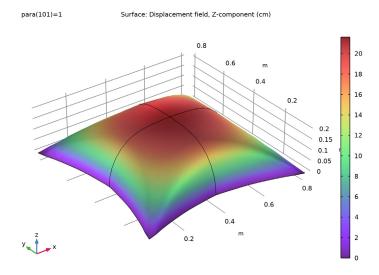


Figure 2: Transverse displacement after inflation.

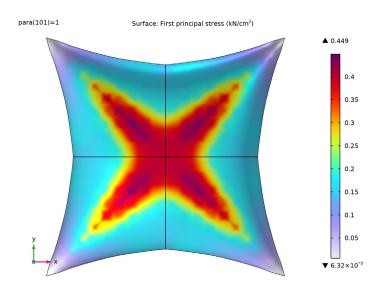


Figure 3: First principal stress after inflation.

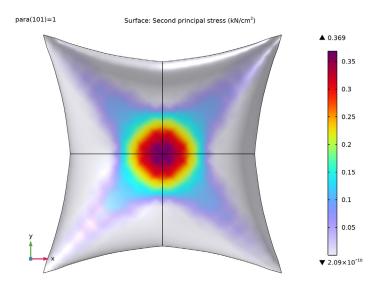


Figure 4: Second principal stress after inflation.

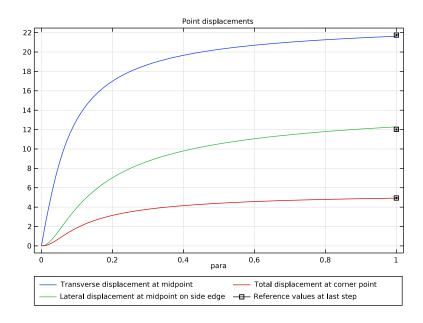


Figure 5: Displacements at different points after inflation.

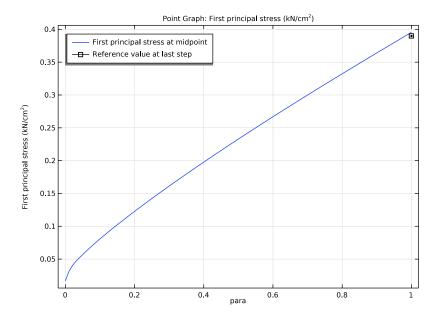


Figure 6: First principal stress at midpoint.

Notes About the COMSOL Implementation

A wrinkling model based on the modified deformation gradient is incorporated within the membrane theory using the Wrinkling feature, which solves a set of nonlinear equations with the Newton-Raphson method.

Since the unstressed membrane does not have any stiffness in the normal direction, a very small spring support is added in order to stabilize the model. To further improve the numerical stability, a spring support is provided in the form of an edge load which decreases parametrically as the model becomes stable.

Constant strain triangle (CST) elements are numerically stable for wrinkling problems. CST elements give constant strains, which in turn give constant stresses for homogeneous material properties, ensuring that the whole element is either wrinkled, slack, or taut. These type of elements are used for the analysis.

Reference

1. A. Jarasjarungkiat, R. Wuchner, and K.U.Bletzinger, "A wrinkling model based on material modification for isotropic and orthotropic membranes," Compt. Methods Appl. Mech. Engrg., vol. 197, pp. 773-788, 2008.

Application Library path: Structural Mechanics Module/ Buckling and Wrinkling/membrane airbag inflation

Modeling Instructions

From the File menu, choose New.

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics>Membrane (mbrn).
- 3 Click Add.
- 4 Click 🔵 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

GLOBAL DEFINITIONS

Model Parameters

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, type Model Parameters in the Label text field.
- 3 Locate the Parameters section. Click **Load from File.**
- 4 Browse to the model's Application Libraries folder and double-click the file membrane_airbag_inflation_parameters.txt.

DEFINITIONS

Interpolation I (int I)

- I In the Home toolbar, click f(x) Functions and choose Local>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 In the Function name text field, type F.
- **4** In the table, enter the following settings:

t	f(t)
0	100
1	1

5 Locate the **Units** section. In the **Function** table, enter the following settings:

Function	Unit
F	N/m

6 In the **Argument** table, enter the following settings:

Argument	Unit
t	1

Variables 1

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
wmax_ref	21.75[cm]	m	Transverse displacement at midpoint, reference
vmax_ref	12.03[cm]	m	Lateral displacement at midpoint on side edge, reference
dispmax_ref	4.94[cm]	m	Total displacement at corner point, reference
sp1max_ref	0.39[kN/cm ²]	N/m²	First principal stress at midpoint, reference

Due to symmetry only a quarter of the geometry is constructed.

GEOMETRY I

Work Plane I (wpl)

- I In the Model Builder window, expand the Component I (compl)>Geometry I node.
- 2 Right-click Geometry I and choose Work Plane.

Work Plane I (wbl)>Square I (sql)

- I In the Work Plane toolbar, click Square.
- 2 In the Settings window for Square, locate the Size section.
- 3 In the Side length text field, type L/2.
- 4 Locate the **Position** section. In the xw text field, type L/2.
- 5 In the Work Plane toolbar, click **Build All**.

MATERIALS

Material I (mat I)

In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.

When modeling wrinkling, constant strain triangular (CST) elements are a good choice due to their numerical stability. Use a triangular mesh and change the default Quadratic discretization to Linear.

MEMBRANE (MBRN)

- I In the Settings window for Membrane, click to expand the Discretization section.
- 2 From the Displacement field list, choose Linear.

Linear Elastic Material I

In the Model Builder window, under Component I (compl)>Membrane (mbrn) click Linear Elastic Material I.

Wrinkling I

In the Physics toolbar, click 📃 Attributes and choose Wrinkling.

Thickness and Offset I

- I In the Model Builder window, under Component I (compl)>Membrane (mbrn) click Thickness and Offset 1.
- 2 In the Settings window for Thickness and Offset, locate the Thickness and Offset section.
- **3** In the d_0 text field, type th.

Symmetry I

- I In the Physics toolbar, click **Edges** and choose Symmetry.
- **2** Select Edges 1 and 3 only.

Prescribed Displacement 1

- I In the Physics toolbar, click Edges and choose Prescribed Displacement.
- 2 Select Edges 2 and 4 only.
- 3 In the Settings window for Prescribed Displacement, locate the Prescribed Displacement section.
- 4 Select the **Prescribed in z direction** check box.

Face Load 1

- I In the Physics toolbar, click **Boundaries** and choose Face Load.
- 2 Select Boundary 1 only.
- 3 In the Settings window for Face Load, locate the Force section.
- 4 From the Load type list, choose Pressure.
- **5** In the *p* text field, type -Pmax*para.

Add a parametrically decreasing edge load on the outer edges in the lateral direction as form of spring support in order to achieve numerical stability for this problem.

Edge Load 1

- I In the Physics toolbar, click Edges and choose Edge Load.
- 2 Select Edges 2 and 4 only.
- 3 In the Settings window for Edge Load, locate the Coordinate System Selection section.
- 4 From the Coordinate system list, choose Local edge system.
- **5** Locate the **Force** section. Specify the \mathbf{F}_{L} vector as

0	хl
-F(para)	yl
0	zl

Add a spring support in the thickness direction in order to improve numerical stability.

Spring Foundation 1

- I In the Physics toolbar, click **Boundaries** and choose Spring Foundation.
- 2 In the Settings window for Spring Foundation, locate the Boundary Selection section.
- 3 From the Selection list, choose All boundaries.

- 4 Locate the Spring section. From the list, choose Symmetric.
- **5** In the \mathbf{k}_A table, enter the following settings:

0	0	0
0	0	0
0	0	1e-3[N/m^3]

MATERIALS

Material I (mat I)

- I In the Model Builder window, under Component I (compl)>Materials click Material I (matl).
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	EE	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	Nu	I	Young's modulus and Poisson's ratio
Density	rho	0	kg/m³	Basic

MESH I

Mapped I

- I In the Mesh toolbar, click A Boundary and choose Mapped.
- 2 In the Settings window for Mapped, locate the Boundary Selection section.
- 3 From the Selection list, choose All boundaries.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Edge Selection section.
- 3 From the Selection list, choose All edges.
- **4** Locate the **Distribution** section. In the **Number of elements** text field, type 10.

Convert I

- I In the Mesh toolbar, click A Modify and choose Convert.
- 2 In the Settings window for Convert, locate the Element Split Method section.

- **3** From the **Element split method** list, choose **Insert centerpoints**.
- 4 Click Build All.

Customize the study settings in order to achieve a better convergence.

STUDY I

Step 1: Stationary

- I In the Model Builder window, under Study I click Step I: Stationary.
- 2 In the Settings window for Stationary, click to expand the Study Extensions section.
- 3 Select the Auxiliary sweep check box.
- 4 Click + Add.
- **5** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Parameter)	range(0,0.01,1)	

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Stationary Solver I node, then click Parametric I.
- 4 In the Settings window for Parametric, click to expand the Continuation section.
- **5** Select the **Tuning of step size** check box.
- 6 In the Maximum step size text field, type 0.01.
- 7 From the Predictor list, choose Linear.
- 8 In the Model Builder window, under Study I>Solver Configurations>Solution I (soll)> Stationary Solver I click Fully Coupled I.
- 9 In the Settings window for Fully Coupled, click to expand the Method and Termination section.
- 10 From the Nonlinear method list, choose Constant (Newton).
- II From the Stabilization and acceleration list, choose Anderson acceleration. Before solving the study, add default plots in order to visualize the results while solving.
- 12 In the Model Builder window, click Study 1.
- 13 In the Settings window for Study, locate the Study Settings section.

14 Clear the Generate default plots check box.

15 In the Study toolbar, click In Show Default Plots.

RESULTS

Mirror 3D I

- I In the Model Builder window, expand the Results node.
- 2 Right-click Results>Datasets and choose More 3D Datasets>Mirror 3D.
- 3 In the Settings window for Mirror 3D, locate the Plane Data section.
- 4 From the Plane list, choose XZ-planes.
- 5 In the Y-coordinate text field, type 0.5*L.

Mirror 3D 2

- I Right-click Mirror 3D I and choose Duplicate.
- 2 In the Settings window for Mirror 3D, locate the Data section.
- 3 From the Dataset list, choose Mirror 3D 1.
- 4 Locate the Plane Data section. From the Plane list, choose yz-planes.
- 5 In the x-coordinate text field, type 0.5*L.
- 6 In the Results toolbar, click Add Predefined Plot.

ADD PREDEFINED PLOT

- I Go to the Add Predefined Plot window.
- 2 In the tree, select Study I/Solution I (soll)>Membrane (mbrn)>Displacement (Mbrn).
- 3 Click Add Plot in the window toolbar.

RESULTS

Transverse Displacement

- In the Settings window for 3D Plot Group, type Transverse Displacement in the Label text field.
- 2 Locate the Data section. From the Dataset list, choose Mirror 3D 2.

Surface I

- I In the Model Builder window, expand the Transverse Displacement node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type w.

- 4 From the **Unit** list, choose **cm**.
- 5 Click to expand the Quality section. From the Smoothing threshold list, choose None.
- 6 Click the Zoom Extents button in the Graphics toolbar.
- 7 In the Transverse Displacement toolbar, click Plot.

STUDY I

Steb 1: Stationary

- I In the Model Builder window, under Study I click Step I: Stationary.
- 2 In the Settings window for Stationary, click to expand the Results While Solving section.
- **3** Select the **Plot** check box.
- 4 In the Home toolbar, click **Compute**.

RESULTS

First Principal Stress

- I Right-click Transverse Displacement and choose Duplicate.
- 2 Drag and drop Transverse Displacement I below Transverse Displacement.
- 3 In the Settings window for 3D Plot Group, type First Principal Stress in the Label text field.
- 4 Locate the Color Legend section. Select the Show maximum and minimum values check box.

Surface I

- I In the Model Builder window, expand the First Principal Stress node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Membrane> Stress>Principal stresses>mbrn.spl - First principal stress - N/m2.
- 3 Locate the Expression section. In the Unit field, type kN/cm².
- 4 Locate the Coloring and Style section. Click Change Color Table.
- 5 In the Color Table dialog box, select Rainbow>Prism in the tree.
- 6 Click OK.

First Principal Stress

- I In the Model Builder window, click First Principal Stress.
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- **3** From the **View** list, choose **New view**.

- 4 In the First Principal Stress toolbar, click Plot.
- **5** Click the XY **View** button in the **Graphics** toolbar.
- 6 Click the Show Grid button in the Graphics toolbar.

Second Principal Stress

- I Right-click First Principal Stress and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Second Principal Stress in the Label text field.
- 3 Drag and drop below First Principal Stress.

Surface I

- I In the Model Builder window, expand the Second Principal Stress node, then click Surface 1.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Membrane> Stress>Principal stresses>mbrn.sp2 - Second principal stress - N/m2.

Second Principal Stress

- I In the Model Builder window, click Second Principal Stress.
- 2 In the Second Principal Stress toolbar, click Plot.

Wrinkled Region

- I Right-click Second Principal Stress and choose Duplicate.
- 2 Drag and drop Second Principal Stress I below Second Principal Stress.
- 3 In the Settings window for 3D Plot Group, type Wrinkled Region in the Label text field.
- 4 Locate the Color Legend section. Clear the Show maximum and minimum values check box.

Surface I

- I In the Model Builder window, expand the Wrinkled Region node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Membrane> Wrinkling>mbrn.iswrinkled - Is wrinkled.
- 3 Locate the Coloring and Style section. Click Change Color Table.
- 4 In the Color Table dialog box, select Rainbow>Rainbow in the tree.
- 5 Click OK.
- 6 In the Settings window for Surface, locate the Quality section.

- **7** From the **Smoothing** list, choose **None**.
- 8 In the Wrinkled Region toolbar, click **Plot**.

Point Displacements

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Point Displacements in the Label text field.

Point Grabh 1

- I Right-click Point Displacements and choose Point Graph.
- **2** Select Point 2 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.
- **4** In the **Expression** text field, type w.
- **5** From the **Unit** list, choose **cm**.
- 6 Click to expand the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legends

Transverse displacement at midpoint

Point Graph 2

- I Right-click Point Graph I and choose Duplicate.
- 2 In the Settings window for Point Graph, locate the Selection section.
- 3 Click Clear Selection.
- **4** Select Point 1 only.
- **5** Locate the **y-Axis Data** section. In the **Expression** text field, type v.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends

Lateral displacement at midpoint on side edge

Point Graph 3

- I Right-click Point Graph 2 and choose Duplicate.
- 2 In the Settings window for Point Graph, locate the Selection section.
- 3 Click Clear Selection.

- **4** Select Point 3 only.
- 5 Locate the y-Axis Data section. In the Expression text field, type mbrn.disp.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legend	ls				
Total	displacement	at	corner	point	

Global I

- I In the Model Builder window, right-click Point Displacements and choose Global.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- 4 From the Parameter selection (para) list, choose Last.
- **5** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
wmax_ref	cm	Transverse displacement at midpoint, reference

- 6 Click to expand the Coloring and Style section. From the Color list, choose From theme.
- 7 Find the Line markers subsection. From the Marker list, choose Square.
- 8 From the Positioning list, choose Interpolated.
- **9** Set the **Number** value to **12**.
- 10 Click to expand the Legends section. From the Legends list, choose Manual.
- II In the table, enter the following settings:

Legends					
Reference	values	at	last	step	

Global 2

- I Right-click Global I and choose Duplicate.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description			
vmax_ref	cm	Lateral displacement at midpoint on side edge, reference			

4 Locate the Legends section. Clear the Show legends check box.

Global 3

- I Right-click Global 2 and choose Duplicate.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description		
dispmax_ref	cm	Total displacement at corner point, reference		

Point Displacements

- I In the Model Builder window, click Point Displacements.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the **Title** text area, type Point displacements.
- 5 Locate the Legend section. From the Layout list, choose Outside graph axis area.
- **6** From the **Position** list, choose **Bottom**.
- 7 In the Number of rows text field, type 2.
- 8 In the Point Displacements toolbar, click Plot.

Point Stress

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Point Stress in the Label text field.
- 3 Locate the Legend section. From the Position list, choose Upper left.

Point Graph 1

- I Right-click Point Stress and choose Point Graph.
- **2** Select Point 2 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.
- 4 In the Expression text field, type mbrn.sp1.
- 5 In the Unit field, type kN/cm².
- **6** Locate the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legend	ls			
First	principal	stress	at	midpoint

Point Stress

- I In the Model Builder window, click Point Stress.
- 2 In the Settings window for ID Plot Group, locate the Plot Settings section.
- **3** Select the **y-axis label** check box.

Global I

- I Right-click Point Stress and choose Global.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- 4 From the Parameter selection (para) list, choose Last.
- **5** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description		
sp1max_ref	kN/cm^2	First principal stress at midpoint, reference		

- **6** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 7 Locate the Coloring and Style section. From the Color list, choose From theme.
- 8 Find the Line markers subsection. From the Marker list, choose Square.
- **9** From the **Positioning** list, choose **Interpolated**.
- 10 Locate the Legends section. From the Legends list, choose Manual.
- II In the table, enter the following settings:

Legends					
Reference	value	at	last	step	

Point Stress

- I In the Model Builder window, click Point Stress.
- 2 In the Point Stress toolbar, click Plot.