



# Magnetic Frill

## Introduction

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Feeding antennas with proper signals can be difficult. The signal is often described as a voltage, and voltages are not well defined in electromagnetic wave formulations. There are several tricks to model voltage generators in such situations, and one is the *magnetic frill*. This example shows the basic steps of defining a magnetic frill voltage generator for a dipole antenna, and it also compares the resulting antenna impedance with known results.

## Model Definition

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Magnetic frills can only be defined using Electromagnetic Waves interface, which is based on the time-harmonic Faraday's law.

$$\nabla \times \mathbf{E} = -j\omega\mathbf{B}$$

Although there are no magnetic charges, it is possible to mathematically define a current of magnetic charges, called a magnetic current. This current enters the right-hand side of Faraday's law in the same manner as the ordinary current enters the right-hand side of Ampère's law. Similar to the ordinary current density that has the unit  $\text{A}/\text{m}^2$ , the magnetic current density has the unit  $\text{V}/\text{m}^2$ .

A closed loop of magnetic current therefore has the unit  $V$  and represents a voltage generator for the surface closed by the loop. In this example, the loop is located around a thin straight wire and acts as a voltage source at the center of the wire. This is a dipole antenna fed by a voltage signal in the center.

The current through the wire is measured with another loop, along which a line integral of the  $\mathbf{H}$ -field is specified.

$$\int \mathbf{H} \cdot d\mathbf{l} = I$$

Note that this loop and the magnetic current loop must be two different loops.

The antenna is placed in a spherical air domain surrounded by a perfectly matched layer (PML) serving to absorb the radiation from the antenna with a minimum of reflection.

## Results and Discussion

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The dipole antenna is fed with a voltage signal of 1 V, and from the measured current it is possible to extract the impedance. Taken from [Ref. 1](#), the impedance and dimensions of a

typical dipole antenna are shown in the table below. The dimensions are given in terms of the wavelength,  $\lambda$ .

WAVELENGTH	LENGTH	RADIUS
0.3	$0.47\lambda$	$0.005\lambda$

The impedance from the COMSOL Multiphysics model is  $76.00 + 15.98i$ , which agrees well with the results from [Ref. 1](#).

### *Reference*

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1. C.A. Balanis, *Advanced Engineering Electromagnetics*, John Wiley & Sons, 1989.
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**Application Library path:** RF\_Module/Antennas/magnetic\_frill

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### *Modeling Instructions*

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From the **File** menu, choose **New**.

#### **NEW**

In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Radio Frequency>Electromagnetic Waves, Frequency Domain (emw)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Frequency Domain**.
- 6 Click  **Done**.

#### **GLOBAL DEFINITIONS**

##### *Parameters 1*

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
lda0	0.3[m]	0.3 m	Wavelength
l	0.47	0.47	Scale factor
k	0.005	0.005	Scale factor
L	l*lda0	0.141 m	Dipole length
r_wire	k*lda0	0.0015 m	Wire radius
f0	1/lda0/sqrt(epsilon0_const* mu0_const)	9.9931E8 1/s	Frequency

## STUDY I

*Step 1: Frequency Domain*

- 1 In the **Model Builder** window, under **Study I** click **Step 1: Frequency Domain**.
- 2 In the **Settings** window for **Frequency Domain**, locate the **Study Settings** section.
- 3 In the **Frequencies** text field, type f0.

## GEOMETRY I

*Work Plane 1 (wp1)*

- 1 In the **Geometry** toolbar, click  **Work Plane**.
- 2 In the **Settings** window for **Work Plane**, locate the **Plane Definition** section.
- 3 From the **Plane** list, choose **yz-plane**.
- 4 Click  **Show Work Plane**.

*Work Plane 1 (wp1)>Rectangle 1 (r1)*

- 1 In the **Work Plane** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type r\_wire.
- 4 In the **Height** text field, type L.
- 5 Locate the **Position** section. In the **yw** text field, type -L/2.

*Work Plane 1 (wp1)>Rectangle 2 (r2)*

- 1 In the **Work Plane** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type 0.3.

- 4 In the **Height** text field, type 0.6.
- 5 Locate the **Position** section. In the **xw** text field, type -0.3.
- 6 In the **yw** text field, type -0.3.

*Work Plane 1 (wp1)>Circle 1 (c1)*

- 1 In the **Work Plane** toolbar, click  **Circle**.
- 2 In the **Settings** window for **Circle**, locate the **Size and Shape** section.
- 3 In the **Radius** text field, type 0.3.

*Work Plane 1 (wp1)>Circle 2 (c2)*

- 1 In the **Work Plane** toolbar, click  **Circle**.
- 2 In the **Settings** window for **Circle**, locate the **Size and Shape** section.
- 3 In the **Radius** text field, type 0.2.

*Work Plane 1 (wp1)>Difference 1 (dif1)*

- 1 In the **Work Plane** toolbar, click  **Booleans and Partitions** and choose **Difference**.
- 2 Select the objects **c1** and **c2** only.  
Alternatively, you can select all objects and remove r1 and r2 from the selection list.
- 3 In the **Settings** window for **Difference**, locate the **Difference** section.
- 4 Find the **Objects to subtract** subsection. Click to select the  **Activate Selection** toggle button.
- 5 Select the objects **r1** and **r2** only.

*Work Plane 1 (wp1)>Line Segment 1 (ls1)*

- 1 In the **Work Plane** toolbar, click  **More Primitives** and choose **Line Segment**.
- 2 In the **Settings** window for **Line Segment**, locate the **Starting Point** section.
- 3 From the **Specify** list, choose **Coordinates**.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 Locate the **Starting Point** section. In the **xw** text field, type 0.2.
- 6 Locate the **Endpoint** section. In the **xw** text field, type 0.3.

This line segment simplifies meshing.

*Work Plane 1 (wp1)>Point 1 (pt1)*

- 1 In the **Work Plane** toolbar, click  **Point**.
- 2 In the **Settings** window for **Point**, locate the **Point** section.
- 3 In the **xw** text field, type r\_wire+0.001.

*Work Plane 1 (wp1)>Point 2 (pt2)*

- 1 In the **Work Plane** toolbar, click  **Point**.
- 2 In the **Settings** window for **Point**, locate the **Point** section.
- 3 In the **xw** text field, type 0.01.
- 4 In the **Work Plane** toolbar, click  **Build All**.

*Revolve 1 (rev1)*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** right-click **Work Plane 1 (wp1)** and choose **Revolve**.
- 2 In the **Settings** window for **Revolve**, locate the **Revolution Angles** section.
- 3 Click the **Angles** button.
- 4 In the **End angle** text field, type -90.
- 5 Click  **Build All Objects**.
- 6 Click the  **Zoom Extents** button in the **Graphics** toolbar.

*Form Union (fin)*

- 1 In the **Model Builder** window, click **Form Union (fin)**.
- 2 In the **Settings** window for **Form Union/Assembly**, click  **Build Selected**.
- 3 Click the  **Wireframe Rendering** button in the **Graphics** toolbar.

## DEFINITIONS

*Integration 1 (intop1)*

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Integration**.
- 2 In the **Settings** window for **Integration**, locate the **Source Selection** section.
- 3 From the **Geometric entity level** list, choose **Edge**.
- 4 Select Edge 20 only.

*Variables 1*

- 1 In the **Definitions** toolbar, click  **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Edge**.
- 4 Select Edge 20 only.

5 Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
intopl_source_I	$4 * (emw.Hx * t1x + emw.Hy * t1y)$	A/m	

#### Variables 2

- 1 In the **Definitions** toolbar, click  **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 In the table, enter the following settings:

Name	Expression	Unit	Description
I	intopl(intopl_source_I)	A	Current
Z	1/I	1/A	Impedance

#### Perfectly Matched Layer 1 (pml1)

- 1 In the **Definitions** toolbar, click  **Perfectly Matched Layer**.
- 2 Select Domains 1 and 3 only.
- 3 In the **Settings** window for **Perfectly Matched Layer**, locate the **Geometry** section.
- 4 From the **Type** list, choose **Spherical**.

#### ADD MATERIAL

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Built-in>Air**.
- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.

#### ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

##### Perfect Magnetic Conductor 1

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Electromagnetic Waves, Frequency Domain (emw)** and choose **Perfect Magnetic Conductor**.
- 2 Select Boundaries 1, 2, 4, 5, 9, and 10 only.

##### Magnetic Current 1

- 1 In the **Physics** toolbar, click  **Edges** and choose **Magnetic Current**.
- 2 Select Edge 21 only.

**3** In the **Settings** window for **Magnetic Current**, locate the **Magnetic Current** section.

**4** In the  $I_m$  text field, type 1.

### **MESH 1**

In the **Model Builder** window, under **Component 1 (comp1)** right-click **Mesh 1** and choose **Build All**.

### **STUDY 1**

In the **Home** toolbar, click  **Compute**.

### **RESULTS**

#### *Electric Field (emw)*

The default plot shows the electric field on slices through the geometry.

Visualize the electric field around the antenna by modifying this plot as follows:

Delete the Multislice plot.

#### *Multislice*

**1** In the **Model Builder** window, expand the **Electric Field (emw)** node.

**2** Right-click **Results>Electric Field (emw)>Multislice** and choose **Delete**.

#### *Electric Field (emw)*

Add two Slice plots.

#### *Slice 1*

**1** In the **Model Builder** window, right-click **Electric Field (emw)** and choose **Slice**.

**2** In the **Settings** window for **Slice**, locate the **Plane Data** section.

**3** From the **Plane** list, choose **XY-planes**.

**4** From the **Entry method** list, choose **Coordinates**.

**5** Click to expand the **Range** section. Select the **Manual color range** check box.

**6** In the **Maximum** text field, type 20.

**7** Select the **Manual data range** check box.

**8** In the **Maximum** text field, type 20.

#### *Slice 2*

**1** Right-click **Electric Field (emw)** and choose **Slice**.

**2** In the **Settings** window for **Slice**, locate the **Plane Data** section.

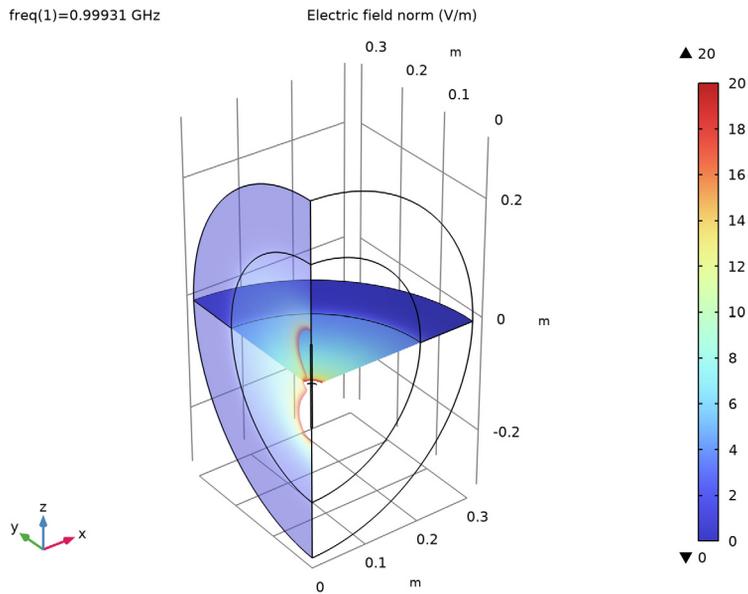
- 3 From the **Entry method** list, choose **Coordinates**.
- 4 Click to expand the **Inherit Style** section. From the **Plot** list, choose **Slice 1**.

*Transparency 1*

Right-click **Slice 2** and choose **Transparency**.

*Electric Field (emw)*

- 1 In the **Settings** window for **3D Plot Group**, click to expand the **Title** section.
- 2 From the **Title type** list, choose **Manual**.
- 3 In the **Title** text area, type Electric field norm (V/m).
- 4 In the **Electric Field (emw)** toolbar, click  **Plot**.



*Global Evaluation 1*

- 1 In the **Results** toolbar, click  **Global Evaluation**.
- 2 In the **Settings** window for **Global Evaluation**, locate the **Expressions** section.
- 3 In the table, enter the following settings:

Expression	Unit	Description
Z	1/A	Impedance

- 4 Click  **Evaluate**.

