

# Thermal Bridges in Building Construction — 2D Composite Structure

The European standard EN ISO 10211:2017 for thermal bridges in building constructions provides four test cases — two 2D and two 3D — for validating a numerical method (Ref. 1). If the values obtained by a method conform to the results of all these four cases, the method is classified as a three-dimensional steady-state high precision method.

COMSOL Multiphysics successfully passes all the test cases described by the standard. This document presents an implementation of the second 2D model (Case 2).

The example studies the temperature distribution and heat flux through a twodimensional cross-section of an insulating wall. Table 1 and Table 2 compare the numerical results with the target solution provided by the standard.

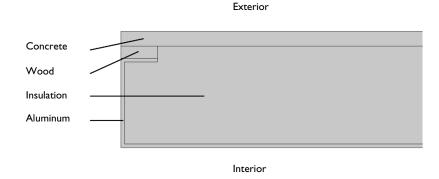


Figure 1: Geometry and material distribution of ISO 10211:2017 test case 2.

# Model Definition

Figure 1 shows the geometry and material distribution. Four materials with distinct thermal conductivities are used in the structure: a concrete layer on the top side, an aluminum layer on the left and bottom sides, an insulation material layer occupying the largest space in the structure, and a wooden batten between the aluminum and concrete lavers.

The left and right boundaries are thermally insulated. The top and bottom boundaries, corresponding to cold exterior and hot interior sides, are subject to convective heat flux. The exterior temperature is 0°C while interior temperature is 20°C. The ISO 10211:2017 standard specifies the values of the thermal resistance, R, which is related to the heat transfer coefficient, h, according to

$$h = \frac{1}{R}$$

# Results and Discussion

The temperature profile in Figure 2 shows the effects of the highly conductive aluminum layer on the left side.

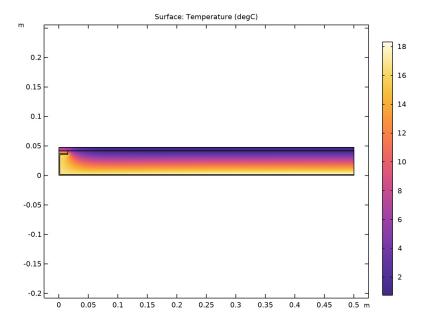


Figure 2: Temperature distribution of ISO 10211:2017 test case 2.

The numerical results of the COMSOL Multiphysics simulation are compared with the expected values provided by EN ISO 10211:2017 (Ref. 1). Table 1 shows the comparison for the total heat flux and Table 2 compares temperature at nine particular points.

TABLE I: COMPARISON BETWEEN EXPECTED VALUES AND COMPUTED VALUES (TOTAL HEAT FLUX).

EXPECTED VALUE	COMPUTED VALUE	DIFFERENCE
9.5 W/m	9.49 W/m	0.08%

TABLE 2: COMPARISON BETWEEN EXPECTED VALUES AND COMPUTED VALUES (TEMPERATURE).

(X,Y) COORD. (MM)	EXPECTE D VALUE (°C)	COMPUTE D VALUE (°C)	DIFF. (°C)	(X,Y) COORD. (MM)	EXPECTE D VALUE (°C)	COMPUTE D VALUE (°C)	DIFF. (°C)
(0, 47.5)	7.1	7.07	0.03	(15, 41.5)	6.3	6.27	0.03
(0, 41.5)	7.9	7.90	0.00	(15, 36.5)	16.3	16.33	0.03
(0, 36.5)	16.4	16.41	0.01	(500, 47.5)	0.8	0.76	0.04
(0, 0)	16.8	16.77	0.03	(500, 41.5)	0.8	0.83	0.03
				(500, 0)	18.3	18.33	0.03

The maximum permissible differences to pass this case validation, 0.1°C for temperature and 0.1% for total heat flux, are respected.

# Reference

1. European Committee for Standardization, EN ISO 10211, Thermal bridges in building construction – Heat flows and surface temperatures – Detailed calculations (ISO 10211:2017), Appendix A, pp. 54–60, 2017.

**Application Library path:** Heat\_Transfer\_Module/

Buildings\_and\_Constructions/thermal\_bridge\_2d\_composite\_structure

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click **Q** 2D.
- 2 In the Select Physics tree, select Heat Transfer>Heat Transfer in Solids (ht).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

#### **GLOBAL DEFINITIONS**

#### Parameters 1

Define the parameters necessary to build the geometry.

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
W	0.5[m]	0.5 m	Structure width
W	15[mm]	0.015 m	Short width for wood and aluminum domains
h1	6[mm]	0.006 m	Concrete domain height
h2	5[mm]	0.005 m	Wood domain height
h3	41.5[mm]	0.0415 m	Insulation domain height
h4	h3-h2	0.0365 m	Aluminum domain height
t4	1.5[mm]	0.0015 m	Aluminum domain thickness

#### **GEOMETRY I**

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type W.
- 4 In the **Height** text field, type h3+h1.
- **5** Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	h3

6 Click Pauld Selected.

This two-layered rectangle corresponds to the insulation and concrete layers. Continue with the aluminum layer, which consists of three rectangles.

# Rectangle 2 (r2)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.

- 3 In the Width text field, type W.
- 4 In the Height text field, type t4.
- 5 Click | Build Selected.

# Rectangle 3 (r3)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type t4.
- 4 In the Height text field, type h4.
- 5 Click | Build Selected.

# Rectangle 4 (r4)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type w.
- 4 In the Height text field, type t4.
- 5 Locate the Position section. In the y text field, type h4-t4.
- 6 Click | Build Selected.

## Union I (uni I)

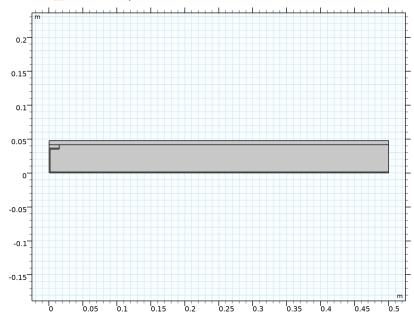
- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 In the Settings window for Union, locate the Union section.
- 3 Clear the Keep interior boundaries check box.
- 4 Click Clear Selection.
- 5 Select the objects r2, r3, and r4 only.
- 6 Click | Build Selected.

Add a rectangle for the wooden batten.

#### Rectangle 5 (r5)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type w.
- 4 In the Height text field, type h2.
- **5** Locate the **Position** section. In the **y** text field, type h4.

6 Click **Build All Objects**.



# MATERIALS

## Concrete

- I In the Materials toolbar, click **Blank Material**.
- 2 In the Settings window for Material, type Concrete in the Label text field.
- **3** Select Domain 3 only.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	1.15	W/(m·K)	Basic
Density	rho	2300	kg/m³	Basic
Heat capacity at constant pressure	Ср	880	J/(kg·K)	Basic

## Wood

- I In the Materials toolbar, click **Blank Material**.
- 2 In the Settings window for Material, type Wood in the Label text field.

- **3** Select Domain 2 only.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	0.12	W/(m·K)	Basic
Density	rho	500	kg/m³	Basic
Heat capacity at constant pressure	Ср	2500	J/(kg·K)	Basic

## Insulation

- I In the Materials toolbar, click Blank Material.
- 2 In the Settings window for Material, type Insulation in the Label text field.
- **3** Select Domain 4 only.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	0.029	W/(m·K)	Basic
Density	rho	150	kg/m³	Basic
Heat capacity at constant pressure	Ср	1000	J/(kg·K)	Basic

## Aluminum

- I In the Materials toolbar, click **Blank Material**.
- 2 In the Settings window for Material, type Aluminum in the Label text field.
- **3** Select Domain 1 only.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	230	W/(m·K)	Basic
Density	rho	2700	kg/m³	Basic
Heat capacity at constant pressure	Ср	900	J/(kg·K)	Basic

#### HEAT TRANSFER IN SOLIDS (HT)

Heat Flux I

- I In the Model Builder window, under Component I (compl) right-click Heat Transfer in Solids (ht) and choose Heat Flux.
- 2 Select Boundaries 2 and 10 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- 4 From the Flux type list, choose Convective heat flux.
- **5** In the h text field, type 1/0.11.
- **6** In the  $T_{\rm ext}$  text field, type 20[degC].

Heat Flux 2

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- 2 Select Boundary 9 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- 4 From the Flux type list, choose Convective heat flux.
- **5** In the h text field, type 1/0.06.
- **6** In the  $T_{\rm ext}$  text field, type O[degC].

#### STUDY I

In the **Home** toolbar, click **Compute**.

#### RESULTS

Surface

The first default plot shows the temperature distribution (Figure 2).

- I In the Model Builder window, expand the Results>Temperature (ht) node, then click Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose degC.
- **4** Click the **Zoom Extents** button in the **Graphics** toolbar.

Isothermal Contours (ht)

The second default plot shows isothermal contours in the structure.

Follow the steps below to compute the heat flux given in Table 1.

## Line Integration I

- I In the Results toolbar, click 8.85 More Derived Values and choose Integration> Line Integration.
- **2** Select Boundaries 2 and 10 only.
- 3 In the Settings window for Line Integration, click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Heat Transfer in Solids>Boundary fluxes>ht.q0 - Inward heat flux - W/m2.
- 4 Click **= Evaluate**.

Finally, export the temperature values at the points given in Table 2 to compare the results with the expected values.

#### Data I

- I In the Results toolbar, click Data and choose Data.
- 2 In the Settings window for Data, locate the Expressions section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
Т	degC	Temperature

- **4** Locate the **Output** section. Click **Browse**.
- **5** Browse to a suitable folder, enter the filename thermal\_bridge\_2d\_composite\_structure\_result.txt, and then click Save.
- 6 From the Points to evaluate in list, choose Grid.
- 7 In the X text field, type 0, w, W.
- 8 In the Y text field, type 0, h4, h4+h2, h4+h2+h1.
- 9 Click Export.