

Steady-State 2D Axisymmetric Heat Transfer with Conduction

Introduction

The following example illustrates how to build and solve a conductive heat transfer problem using the Heat Transfer interface. The model, taken from a NAFEMS benchmark collection, shows an axisymmetric steady-state thermal analysis. As opposed to the NAFEMS benchmark model, the COMSOL Multiphysics simulation uses the kelvin temperature unit instead of degrees Celsius.

Model Definition

273.15 K z = 0.1 m $5 \cdot 10^5 \text{W/m}^2$ z = 0.04 m z = 0.04 m z = 0.04 mz = 0 m

The modeling domain describes the cross section of a 3D solid as shown in Figure 1.

Figure 1: Model geometry and boundary conditions.

You set three types of boundary conditions:-

- Prescribed heat flux
- Insulation/Symmetry
- Prescribed temperature

The governing equation for this problem is the steady-state heat equation for conduction with the volumetric heat source set to zero:

$$\nabla \cdot (-k\nabla T) = 0$$

The thermal conductivity k is 52 W/(m·K).

Results





Figure 2: Temperature distribution.

The benchmark result for the target location (r = 0.04 m and z = 0.04 m) is a temperature of 59.82 °C (332.97 K). The COMSOL Multiphysics model, using a default mesh with about 540 elements, gives a temperature of 332.96 K at the same location.

Reference

1. A.D. Cameron, J.A. Casey, and G.B. Simpson, *NAFEMS Benchmark Tests for Thermal Analysis (Summary)*, NAFEMS, 1986.

Application Library path: Heat_Transfer_Module/Tutorials,_Conduction/ cylinder_conduction

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🔗 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 🚈 2D Axisymmetric.
- 2 In the Select Physics tree, select Heat Transfer>Heat Transfer in Solids (ht).
- 3 Click Add.
- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click 🗹 Done.

GEOMETRY I

Rectangle 1 (r1)

- I In the Geometry toolbar, click 📃 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.08**.
- **4** In the **Height** text field, type **0.14**.
- 5 Locate the **Position** section. In the **r** text field, type 0.02.

Point I (ptl)

- I In the **Geometry** toolbar, click **Point**.
- 2 In the Settings window for Point, locate the Point section.
- **3** In the **r** text field, type 0.02 0.02.
- **4** In the **z** text field, type 0.04 0.1.
- 5 In the Geometry toolbar, click 🟢 Build All.

HEAT TRANSFER IN SOLIDS (HT)

Solid I

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Solids (ht) click Solid I.
- 2 In the Settings window for Solid, locate the Heat Conduction, Solid section.

- 3 From the *k* list, choose User defined. In the associated text field, type 52.
- 4 Locate the Thermodynamics, Solid section. From the C_p list, choose User defined. From the ρ list, choose User defined.

Temperature 1

- I In the Physics toolbar, click Boundaries and choose Temperature.
- 2 In the Settings window for Temperature, locate the Temperature section.
- **3** In the T_0 text field, type 273.15[K].
- **4** Select Boundaries 2, 5, and 6 only.

Heat Flux 1

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- 2 In the Settings window for Heat Flux, locate the Heat Flux section.
- **3** In the q_0 text field, type **5e5**.
- **4** Select Boundary **3** only.

MESH I

In the Model Builder window, under Component I (comp1) right-click Mesh I and choose Build All.

STUDY I

In the **Home** toolbar, click **= Compute**.

RESULTS

Temperature, 3D (ht)

The first default plot is a revolved 3D plot visualizing the temperature field on the surface; compare with Figure 2.

I Click the 🕂 Zoom Extents button in the Graphics toolbar.

Isothermal Contours (ht)

The second default plot shows a contour plot of the temperature field.



To obtain the temperature value at any point, just click at that point in the **Graphics** window; The result appears in the Table window at the bottom of the COMSOL Desktop.

Alternatively, you can create a Cut Point dataset and Point Evaluation feature as follows.

Cut Point 2D I

- I In the Model Builder window, expand the Results>Temperature, 3D (ht) node.
- 2 Right-click Results>Datasets and choose Cut Point 2D.
- 3 In the Settings window for Cut Point 2D, locate the Point Data section.
- **4** In the **R** text field, type 0.04.
- **5** In the **Z** text field, type **0.04**.

Point Evaluation 1

- I In the **Results** toolbar, click ^{8.85}_{e-12} **Point Evaluation**.
- 2 In the Settings window for Point Evaluation, locate the Data section.
- 3 From the Dataset list, choose Cut Point 2D I.
- 4 Click **=** Evaluate.

TABLE

I Go to the **Table** window.

The result is approximately 333 K.

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