

# Cracking of a Notched Beam

# Introduction

Cracking is an important failure mechanism in many materials, especially in brittle and quasi-brittle materials such as concrete. To model the failure of such materials require not only an appropriate material model, but also modeling techniques to properly describe the size effect in order to avoid mesh dependent results.

In this example, failure is examined by simulating a three-point bending fracture test of a notched concrete beam. The model is based on the experiments presented in Ref. 1. In that paper, several tests are presented on specimens of different sizes and configurations (different notch sizes or no notch) to study the size effect. In this example one of those specimens is modeled, although the model is parameterized such that all specimens from the reference can be reproduced. The results are compared to measured data.

# Model Definition

The geometry of a general specimen from Ref. 1 is given in Figure 1. The parameter  $D_n$  is defined by

$$D_n = \frac{D_0}{2^{n-1}}$$
(1)

where  $D_0 = 400 \text{ mm}$  and n = (1, 2, 3, 4).

Furthermore, the notch is described by its depth  $\alpha_m = (0.5, 0.2, 0)$ . In this example, the specimen given by n = 2 and  $\alpha_m = 0.2$  is modeled. Notice that the width of the notch is set to one mesh element. The depth of the beam is constant and equal to 50 mm. The assumption of plane stress is used. The beam is simply supported and loaded with a 'distributed' point load above the notch. As in the experimental set up described in Ref. 1, the load is controlled through the crack mouth opening displacement (CMOD) which is monotonically increased for all tested specimens. Although the deflection is also monotonically increased for n = 2 and  $\alpha_m = 0.2$ , this might not be the case for larger specimens.

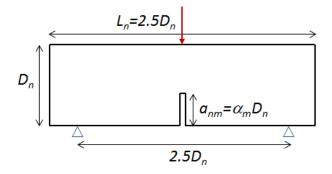


Figure 1: Geometry of the specimens, as specified in Ref. 1.

According to Ref. 1, measurements on the used concrete gave a Young's modulus of 37 GPa and a Poisson's ratio of 0.21. The measured compressive strength is 42.3 MPa and the tensile strength is 3.9 MPa. The material is described by a linear elastic material model with damage to account for tensile cracking. The damage model is set up to describe tensile material failure by using the Rankine equivalent strain definition. A damage evolution law with an exponential strain softening is used. With this option, the fracture energy enters as an additional input parameter, and is here set to 85 J/m<sup>2</sup>. When modeling tensile cracking it is also necessary to add regularization to the damage model in order to ensure that a consistent amount of energy is dissipated during mesh refinement or for different discretization orders. Two techniques for this are available in COMSOL Multiphysics and both are evaluated in this model:

- The crack band method
- The implicit gradient method

The crack band method considers the current discretization and modifies the damage model locally at each material point based on the element size. A more refined approach is to use the implicit gradient method which enforces a predefined width of the damage zone through a localization limiter. This is done by adding a nonlocal strain variable and an internal length scale to the material model through an additional PDE that is solved simultaneously with the displacements. While the recommendation to use a linear displacement field when using the crack band method is used, the study with the implicit gradient method is set up to use the default discretization settings (that is, quadratic serendipity). For simplicity, the same mesh size is used for both cases. This can be considered as a bit unfair when comparing results; when using first order discretization a significantly finer mesh would be needed to obtain a similar accuracy in both methods.

Two studies are defined to compare the two regularization techniques:

- The crack band method with a linear displacement field
- The implicit gradient method

The results from both studies are compared in Figure 2 showing the force versus CMOD curves as well as the measured data from Ref. 1. As an additional comparison, the force versus deflection curves are shown in Figure 3, despite no measured data being available. The crack band method in Study 1 is in very good agreement with the measured data at the peak load, while for the post peak behavior, the simulated force is underestimated for a given CMOD. For the implicit gradient method in Study 2, the peak load is overestimated by approximately 1 kN. Also for this case, the force is underestimated for the post peak response. However, both solutions can describe the overall failure behavior of the beam.

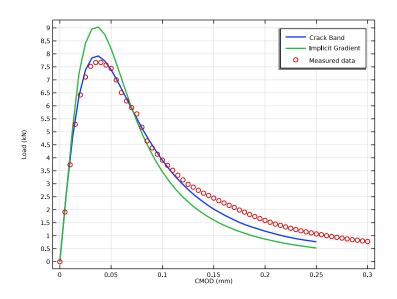


Figure 2: Load versus crack mouth opening displacement.

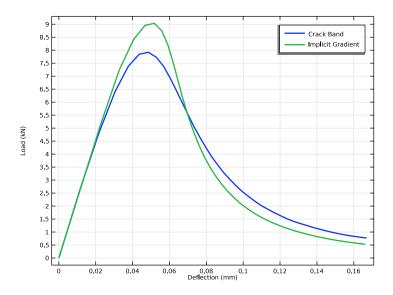


Figure 3: Load versus vertical deflection.

The results of Study 1 can be analyzed in more detail in Figure 4 and Figure 5, which show the damage and strain fields, respectively, at the final step of the solution. As expected for the crack band method, both the damage and the strains are localized in to a single row of elements. It can also be noticed that the crack almost propagates through the entire height of the beam.

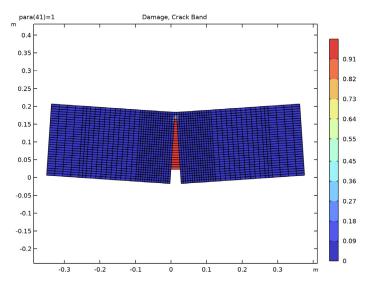


Figure 4: Damage distribution when using the crack band model.

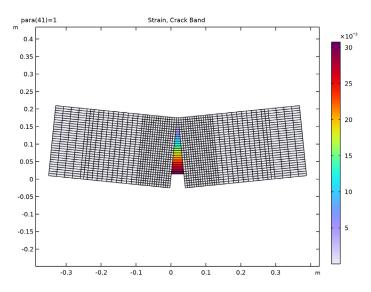


Figure 5: Distribution of equivalent strain when using the crack band model.

#### 6 | CRACKING OF A NOTCHED BEAM

The same plots are shown for the results from Study 2 in Figure 6 and Figure 7. For this modeling technique, a clearly distributed zone of damage over several elements is obtained. Also, the strains are much less localized as compared to the crack band method. In Figure 6, it can be noticed that the damage field stretches below the tip of the notch. This is a nonphysical behavior that results from the nonlocal modeling approach. This could explain the overestimation of the peak load seen in Figure 2 and is a general issue of nonlocal regularization methods for problems where a crack initiates at non-trivial physical boundaries, such as a notch. Finally, the stress versus strain response of the models are compared in Figure 8 at four points located at different heights above the notch.

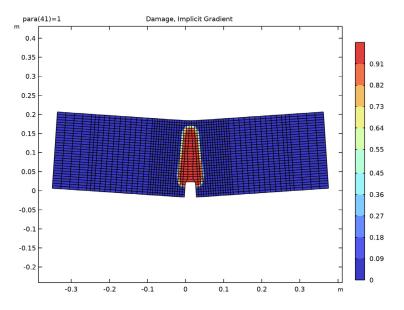


Figure 6: Damage distribution when using the implicit gradient model.

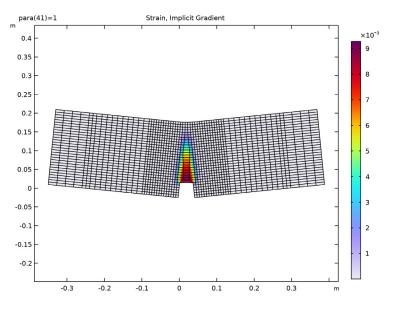


Figure 7: Distribution of equivalent strain when using the implicit gradient model.

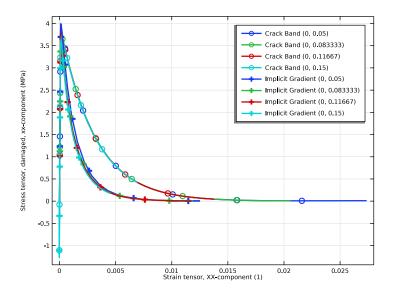


Figure 8: Horizontal stress versus horizontal strain at four points above the notch.

# Notes about the COMSOL implementation

Apart from being prone to tensile cracking, concrete is also highly nonlinear in compression. Accounting for this can improve the force versus CMOD curves. This can for example be done by using the Mazars damage model for concrete available in the Geomechanics module.

The loading of the beam is controlled through the CMOD. A suitable modeling technique to accomplish this is to use an algebraic equation that controls the applied force so that the model reaches the desired CMOD. This is implemented using a **Global Equation**, and the parametric solver steps up the desired CMOD.

Although a single specimen is analyzed, the model is parameterized so that all set-ups presented in Ref. 1 can be described. For example, the size effect can be examined by running a parametric sweep over n. However, if a specimen without a notch is to be modeled by setting i = 0, some minor modifications to the geometry and load control are necessary:

- Remove the part of the geometry that creates the notch.
- Redefine the position of the CMOD coupling operators so that the measuring points are further from the midsection.

For some configurations, the nonlinear solver also have to be modified to obtain a converging solution. In particular, this is the case for the specimens without a notch. For example, better convergence is often obtained if in the **Fully Coupled** node the **Nonlinear method** is set to **Constant (Newton)** with **Jacobian update** on every iteration.

# Reference

1. D. Grégoire, L.B. Rojas-Solano, and G. Pijaudier-Cabot, "Failure and size effect for notched and unnotched concrete beams," *Int. J. Numer. Anal. Meth. Geomech.*, vol. 37, no. 10, pp. 1434–1452, 2013.

Application Library path: Geomechanics\_Module/Damage/notched\_beam\_damage

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click 🚳 Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 🧐 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- **3** Right-click and choose **Add Physics**.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **M** Done.

## GLOBAL DEFINITIONS

#### Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click 📂 Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file notched\_beam\_damage\_parameters.txt.

## GEOMETRY I

#### Rectangle 1 (r1)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **3.5**\*Dn.
- 4 In the **Height** text field, type Dn.
- 5 Locate the Position section. From the Base list, choose Center.
- 6 In the y text field, type Dn/2.
- 7 Click to expand the **Layers** section. Add a number of subdivisions to the beam in order to facilitate application of loads and constraints, as well as mesh control.
- 8 Select the Layers to the left check box.
- **9** Clear the Layers on bottom check box.

**IO** In the table, enter the following settings:

Layer name	Thickness (m)	
Layer 1	0.5*Dn-loadSurf/2	
Layer 2	loadSurf	
Layer 3	0.75*Dn-loadSurf/2	
Layer 4	0.5*Dn-loadSurf/2	
Layer 5	loadSurf	
Layer 6	0.5*Dn-loadSurf/2	
Layer 7	0.75*Dn-loadSurf/2	
Layer 8	loadSurf	

## Parameter Check I (pchI)

- I In the Geometry toolbar, click 🧮 Programming and choose Parameter Check.
- 2 In the Settings window for Parameter Check, locate the Parameter Check section.
- **3** In the **Condition** text field, type am<=0.
- 4 In the Message text field, type Notch size must be larger than zero.

## Rectangle 2 (r2)

- I In the **Geometry** toolbar, click **Rectangle**.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type eSize.
- 4 In the **Height** text field, type am.
- 5 Locate the Position section. From the Base list, choose Center.
- 6 In the y text field, type am/2.

#### Difference I (dif1)

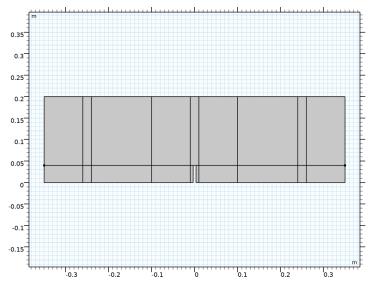
- I In the Geometry toolbar, click 📕 Booleans and Partitions and choose Difference.
- 2 Click in the Graphics window and then press Ctrl+A to select both objects.
- **3** Select the object **r1** only.
- 4 In the Settings window for Difference, locate the Difference section.
- **5** Find the **Objects to subtract** subsection. Click to select the **Comparison of Comparison of Comp**
- 6 Select the object r2 only.
- 7 Click 📄 Build Selected.

## Polygon I (poll)

I In the Geometry toolbar, click / Polygon.

Add a help line for easy mapped meshing.

- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.
- 4 In the x text field, type -Dn\*1.75 Dn\*1.75.
- 5 In the y text field, type am am.
- 6 Click 🟢 Build All Objects.



Most internal edges and vertices are only needed to facilitate a mapped mesh. Use **Virtual Operations** to only make them visible during meshing.

## Mesh Control Edges 1 (mcel)

- I In the Geometry toolbar, click 🏠 Virtual Operations and choose Mesh Control Edges.
- **2** On the object **fin**, select Boundaries 4, 6, 8, 9, 11, 13, 14, 16, 18, 19, 21, 23, 24, 27, 30, 31, 33, 34, 36, 38, 39, 41, 43, 44, 46, 48, and 49 only.
- 3 In the Settings window for Mesh Control Edges, locate the Input section.
- 4 Clear the Include adjacent vertices check box.

#### Mesh Control Vertices 1 (mcv1)

I In the Geometry toolbar, click 🏷 Virtual Operations and choose Mesh Control Vertices.

- **2** On the object **mce1**, select Points 2, 5, 6, 8–14, 20, 21, 23–25, 27, 28, 30, 31, and 33 only.
- 3 In the Geometry toolbar, click 🟢 Build All.

#### DEFINITIONS

Create a variable measuring the crack mouth opening displacement (CMOD).

Crack Mouth Opening Displacement, Right

- I In the Definitions toolbar, click Ronlocal Couplings and choose Average.
- 2 In the Settings window for Average, type CMOD\_right in the Operator name text field.
- 3 In the Label text field, type Crack Mouth Opening Displacement, Right.
- 4 Locate the Source Selection section. From the Geometric entity level list, choose Point.
- 5 Select Point 8 only.

Crack Mouth Opening Displacement, Left

- I In the Definitions toolbar, click 🖉 Nonlocal Couplings and choose Average.
- 2 In the Settings window for Average, type Crack Mouth Opening Displacement, Left in the Label text field.
- 3 In the **Operator name** text field, type CMOD\_left.
- 4 Locate the Source Selection section. From the Geometric entity level list, choose Point.
- 5 Select Point 6 only.

#### Variables I

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
CMOD	CMOD_right(u)- CMOD_left(u)	m	Crack mouth opening displacement

#### SOLID MECHANICS (SOLID)

- I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).
- 2 In the Settings window for Solid Mechanics, locate the 2D Approximation section.
- 3 From the list, choose Plane stress.
- **4** Locate the **Thickness** section. In the *d* text field, type depth.

#### Linear Elastic Material I

In the Model Builder window, under Component I (comp1)>Solid Mechanics (solid) click Linear Elastic Material I.

#### Damage: Crack Band

- I In the Physics toolbar, click Attributes and choose Damage.
- 2 In the Settings window for Damage, type Damage: Crack Band in the Label text field.

#### Damage: Implicit Gradient

- I Right-click Damage: Crack Band and choose Duplicate.
- 2 In the Settings window for Damage, type Damage: Implicit Gradient in the Label text field.
- **3** Locate the **Damage** section. Find the **Spatial regularization method** subsection. From the list, choose **Implicit gradient**.
- **4** In the  $l_{int}$  text field, type lscale.
- **5** In the  $h_{\rm dmg}$  text field, type 3\*lscale.

## Rigid Connector 1

- I In the Physics toolbar, click Boundaries and choose Rigid Connector.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Rigid Connector, locate the
  - Prescribed Displacement at Center of Rotation section.
- **4** Select the **Prescribed in x direction** check box.
- **5** Select the **Prescribed in y direction** check box.

#### Rigid Connector 2

- I In the Physics toolbar, click Boundaries and choose Rigid Connector.
- 2 Select Boundary 12 only.
- **3** In the Settings window for Rigid Connector, locate the Prescribed Displacement at Center of Rotation section.
- 4 Select the **Prescribed in y direction** check box.

## Boundary Load I

- I In the **Physics** toolbar, click **Boundaries** and choose **Boundary Load**.
- **2** Select Boundary 6 only.
- 3 In the Settings window for Boundary Load, locate the Force section.
- 4 From the Load type list, choose Total force.

## **5** Specify the **F**<sub>tot</sub> vector as

0 x

-load y

The applied load is controlled through the CMOD.

- 6 Click the 🐱 Show More Options button in the Model Builder toolbar.
- 7 In the Show More Options dialog box, in the tree, select the check box for the node Physics>Equation-Based Contributions.
- 8 In the tree, select the check box for the node Physics>Advanced Physics Options.

9 Click OK.

Load Control

I In the Physics toolbar, click 🖗 Global and choose Global Equations.

2 In the Settings window for Global Equations, type Load Control in the Label text field.

3 Locate the Global Equations section. In the table, enter the following settings:

Name	f(u,ut,utt,t) (l)	Initial value (u_0) (1)	Initial value (u_t0) (1/s)	Description
load	CMOD-para* maxCMOD	0	0	

4 Locate the Units section. Click **Select Dependent Variable Quantity**.

- 5 In the Physical Quantity dialog box, type force in the text field.
- 6 Click 🔫 Filter.
- 7 In the tree, select General>Force (N).
- 8 Click OK.
- 9 In the Settings window for Global Equations, locate the Units section.
- 10 Click Select Source Term Quantity.
- II In the Physical Quantity dialog box, type displ in the text field.
- 12 Click 👆 Filter.
- **I3** In the tree, select **General>Displacement (m)**.

I4 Click OK.

## Discretization, Linear

I In the Physics toolbar, click 🖗 Global and choose Discretization.

For the crack band method, linear shape order for the displacements is preferred.

- **2** In the **Settings** window for **Discretization**, type **Discretization**, Linear in the **Label** text field.
- 3 Locate the Discretization section. From the Displacement field list, choose Linear.

## MATERIALS

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	37[GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.21	I	Young's modulus and Poisson's ratio
Density	rho	2400	kg/m³	Basic
Peak strength	sigmap	3.9[MPa]	N/m²	Scalar damage
Fracture energy per area	Gf	85	J/m²	Scalar damage

## MESH I

Mapped I

In the Mesh toolbar, click I Mapped.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type eSize.

Mapped I

- I In the Model Builder window, click Mapped I.
- 2 In the Settings window for Mapped, click to expand the Control Entities section.
- 3 Clear the Smooth across removed control entities check box.

## Distribution I

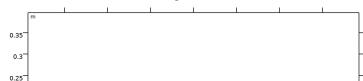
- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- **3** In the **Number of elements** text field, type **4**.
- 4 Select Boundaries 2 and 13 only.

## Distribution 2

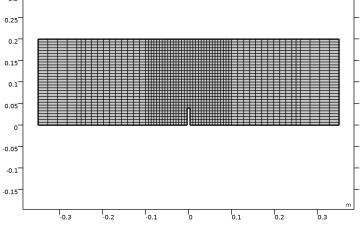
- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 In the Number of elements text field, type 2.
- **4** Select Boundaries 4 and 12 only.

## Distribution 3

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- **3** In the **Number of elements** text field, type 10.
- 4 Select Boundaries 10 and 20 only.



5 In the Model Builder window, right-click Mesh I and choose Build All.



#### STUDY I

Step 1: Stationary

- I In the Model Builder window, under Study I click Step I: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- **3** Select the Modify model configuration for study step check box.
- 4 In the tree, select Component I (comp1)>Solid Mechanics (solid)> Linear Elastic Material I>Damage: Implicit Gradient.
- **5** Right-click and choose **Disable**.
- 6 In the tree, select Component I (compl)>Solid Mechanics (solid).
- 7 From the Discretization list, choose Discretization, Linear.
- 8 Click to expand the Study Extensions section. Select the Auxiliary sweep check box.
- 9 Click + Add.

**IO** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Loading parameter)	range(0,0.025,1)	

II In the Model Builder window, click Study I.

12 In the Settings window for Study, type Study: Crack Band in the Label text field.

**I3** In the **Home** toolbar, click **Compute**.

14 Click 📕 Add Predefined Plot.

#### ADD PREDEFINED PLOT

- I Go to the Add Predefined Plot window.
- 2 In the tree, select Study: Crack Band/Solution 1 (sol1)>Solid Mechanics>Damage (solid).
- 3 Click Add Plot in the window toolbar.
- **4** In the **Home** toolbar, click **M** Add **Predefined Plot**.

#### RESULTS

Damage, Crack Band

- I In the Model Builder window, under Results click Damage (solid).
- 2 In the Settings window for 2D Plot Group, type Damage, Crack Band in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Label.

4 Locate the Plot Settings section. Clear the Plot dataset edges check box.

## Deformation I

- I In the Model Builder window, expand the Damage, Crack Band node.
- 2 Right-click Surface I and choose Deformation.
- 3 In the Settings window for Deformation, locate the Scale section.
- 4 Select the Scale factor check box. In the associated text field, type 100.

#### Mesh I

- I In the Model Builder window, right-click Damage, Crack Band and choose Mesh.
- 2 In the Settings window for Mesh, locate the Coloring and Style section.
- 3 From the Element color list, choose None.
- 4 Click to expand the Inherit Style section. From the Plot list, choose Surface 1.

## Deformation I

- I Right-click Mesh I and choose Deformation.
- 2 In the Damage, Crack Band toolbar, click **O** Plot.

## Strain, Crack Band

- I In the Model Builder window, right-click Stress (solid) and choose Duplicate.
- 2 In the Settings window for 2D Plot Group, type Strain, Crack Band in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.
- 4 Locate the Plot Settings section. Clear the Plot dataset edges check box.

## Surface 1

- I In the Model Builder window, expand the Strain, Crack Band node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (comp1)>Solid Mechanics> Damage>solid.kappadmg - Maximum value of equivalent strain.
- 3 Click to expand the Quality section. From the Resolution list, choose No refinement.
- 4 From the Smoothing list, choose None.

#### Mesh I

- I In the Model Builder window, right-click Strain, Crack Band and choose Mesh.
- 2 In the Settings window for Mesh, locate the Coloring and Style section.
- 3 From the Element color list, choose None.

4 Locate the Inherit Style section. From the Plot list, choose Surface 1.

#### Deformation 1

- I Right-click Mesh I and choose Deformation.
- 2 In the Strain, Crack Band toolbar, click 🗿 Plot.

#### ADD STUDY

- I In the Home toolbar, click  $\sim 2$  Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Right-click and choose Add Study.
- 5 In the Home toolbar, click 2 Add Study to close the Add Study window.

#### STUDY 2

## Step 1: Stationary

- I In the Settings window for Stationary, locate the Study Extensions section.
- 2 Select the Auxiliary sweep check box.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Loading parameter)	range(0,0.025,1)	

- 5 In the Model Builder window, click Study 2.
- 6 In the Settings window for Study, type Study: Implicit Gradient in the Label text field.
- 7 Locate the Study Settings section. Clear the Generate default plots check box.
- 8 In the Home toolbar, click **=** Compute.

## RESULTS

Damage, Crack Band, Strain, Crack Band

- I In the Model Builder window, under Results, Ctrl-click to select Damage, Crack Band and Strain, Crack Band.
- 2 Right-click and choose **Duplicate**.

## Damage, Implicit Gradient

- I In the Settings window for 2D Plot Group, type Damage, Implicit Gradient in the Label text field.
- 2 Locate the Data section. From the Dataset list, choose Study: Implicit Gradient/ Solution 2 (sol2).
- **3** In the **Damage, Implicit Gradient** toolbar, click **OM Plot**.

#### Strain, Implicit Gradient

- I In the Model Builder window, under Results click Strain, Crack Band I.
- 2 In the Settings window for 2D Plot Group, type Strain, Implicit Gradient in the Label text field.
- **3** In the Strain, Implicit Gradient toolbar, click **OD** Plot.
- 4 Locate the Data section. From the Dataset list, choose Study: Implicit Gradient/ Solution 2 (sol2).
- 5 In the Strain, Implicit Gradient toolbar, click 💽 Plot.

## Load vs. Deflection

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Load vs. Deflection in the Label text field.

## Global I

- I Right-click Load vs. Deflection and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
load	kN	State variable load

- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **5** In the **Expression** text field, type -CMOD\_left(v).
- 6 From the **Unit** list, choose **mm**.
- 7 Click to expand the Legends section. From the Legends list, choose Manual.
- 8 In the table, enter the following settings:

#### Legends

Crack Band

9 Click to expand the Coloring and Style section. From the Width list, choose 2.

**10** In the **Load vs. Deflection** toolbar, click **ID Plot**.

Global 2

- I Right-click Global I and choose Duplicate.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study: Implicit Gradient/Solution 2 (sol2).
- 4 Locate the Legends section. In the table, enter the following settings:

#### Legends

Implicit Gradient

5 In the Load vs. Deflection toolbar, click **I** Plot.

Load vs. Deflection

- I In the Model Builder window, click Load vs. Deflection.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- **3** From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section.
- **5** Select the **x-axis label** check box. In the associated text field, type Deflection (mm).
- 6 Select the y-axis label check box. In the associated text field, type Load (kN).
- 7 In the Load vs. Deflection toolbar, click 💿 Plot.

Load vs. CMOD

- I Right-click Load vs. Deflection and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Load vs. CMOD in the Label text field.
- 3 Locate the Plot Settings section. In the x-axis label text field, type CMOD (mm).

#### Global I

- I In the Model Builder window, expand the Load vs. CMOD node, then click Global I.
- 2 In the Settings window for Global, locate the x-Axis Data section.
- **3** In the **Expression** text field, type CMOD.

Global 2

- I In the Model Builder window, click Global 2.
- 2 In the Settings window for Global, locate the x-Axis Data section.
- **3** In the **Expression** text field, type CMOD.

## Table I

- I In the **Results** toolbar, click **Table**.
- 2 In the Settings window for Table, locate the Data section.
- 3 Click Import.
- 4 Browse to the model's Application Libraries folder and double-click the file notched\_beam\_damage\_measured.txt.

## TABLE

- I Go to the Table window.
- 2 Click Table Graph in the window toolbar.

## RESULTS

#### Table Graph I

In the Model Builder window, under Results>ID Plot Group 8 right-click Table Graph I and choose Copy.

#### Table Graph I

- I In the Model Builder window, right-click Load vs. CMOD and choose Paste Table Graph.
- 2 In the Settings window for Table Graph, locate the Coloring and Style section.
- **3** Find the Line style subsection. From the Line list, choose None.
- 4 Find the Line markers subsection. From the Marker list, choose Circle.
- 5 Click to expand the Legends section. Select the Show legends check box.
- 6 From the Legends list, choose Manual.
- 7 In the table, enter the following settings:

#### Legends

Measured data

8 In the Load vs. CMOD toolbar, click 💿 Plot.

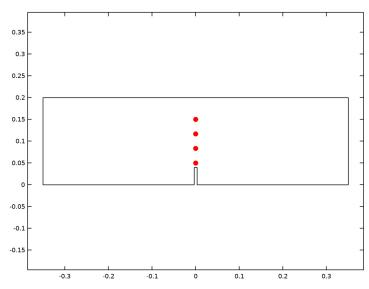
ID Plot Group 8

In the Model Builder window, under Results right-click ID Plot Group 8 and choose Delete.

#### Cut Points, Study I

- I In the **Results** toolbar, click **Cut Point 2D**.
- 2 In the Settings window for Cut Point 2D, type Cut Points, Study 1 in the Label text field.

- 3 Locate the Point Data section. In the X text field, type 0.
- 4 In the Y text field, type {3\*eSize/2 13\*eSize/2 23\*eSize/2 33\*eSize/2}+am.



5 Click 💽 Plot.

Cut Points, Study 2

- I Right-click Cut Points, Study I and choose Duplicate.
- 2 In the Settings window for Cut Point 2D, type Cut Points, Study 2 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study: Implicit Gradient/ Solution 2 (sol2).

Damaged Stress vs. Strain

- I In the **Results** toolbar, click  $\sim$  **ID** Plot Group.
- 2 In the Settings window for ID Plot Group, type Damaged Stress vs. Strain in the Label text field.

#### Point Graph 1

- I Right-click Damaged Stress vs. Strain and choose Point Graph.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Cut Points, Study I.

- 4 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Solid Mechanics>Damage>Stress tensor, damaged (spatial frame) N/m<sup>2</sup>>solid.sdxx Stress tensor, damaged, xx-component.
- 5 Locate the y-Axis Data section. From the Unit list, choose MPa.
- 6 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 7 Click Replace Expression in the upper-right corner of the x-Axis Data section. From the menu, choose Component I (comp1)>Solid Mechanics>Strain>
  Strain tensor (material and geometry frames)>solid.eXX Strain tensor, XX-component.
- 8 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 9 Find the Line markers subsection. From the Marker list, choose Circle.
- **IO** From the **Positioning** list, choose **Interpolated**.
- II Click to expand the Legends section. Select the Show legends check box.
- 12 Find the Prefix and suffix subsection. In the Prefix text field, type Crack Band .
- **I3** In the **Damaged Stress vs. Strain** toolbar, click **ID Plot**.

#### Point Graph 2

- I Right-click Point Graph I and choose Duplicate.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Cut Points, Study 2.
- 4 Locate the Legends section. Find the Prefix and suffix subsection. In the Prefix text field, type Implicit Gradient.
- 5 Locate the Coloring and Style section. From the Color list, choose Cycle (reset).
- 6 Find the Line markers subsection. From the Marker list, choose Plus sign.
- 7 From the **Positioning** list, choose **Interpolated**.

Damaged Stress vs. Strain

- I In the Model Builder window, click Damaged Stress vs. Strain.
- 2 In the Settings window for ID Plot Group, locate the Title section.
- **3** From the **Title type** list, choose **None**.