

Voltammetry at a Microdisk Electrode

Cyclic voltammetry is a common electroanalytical technique. Since the 1980s, it has been common in voltammetry to use a microdisk electrode as the working electrode (Ref. 1). This is a disk electrode with a radius of the order of microns, embedded in an insulator whose surface is flush with the electrode.

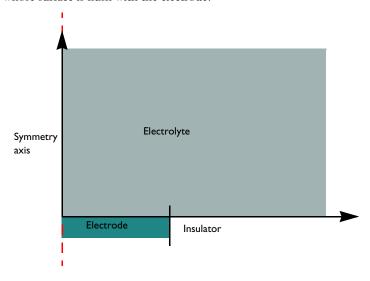


Figure 1: Schematic of the simulation geometry for a microdisk electrode.

These very small electrodes have advantageous mass transport properties that can maximize the measured current density, and so enable the study of electrochemical behavior that would not be observable by conventional voltammetry as performed on a large macroelectrode (See the model .)

This example demonstrates the use of a common approximation in which an electrode with microscale dimensions is assumed to have stationary (equilibrium) diffusion properties on the time scale of a voltammetry study. This simplifies the analysis because a time-dependent model is not required. Instead, a Parametric Sweep is used to assemble a voltammogram under a quasistatic approximation.

Model Definition

The model contains a 2D axisymmetric domain surrounded by a concentric region in which Infinite Elements are used to extend the bulk solution in the model to 'infinity'. The approximation that the bulk solution is infinitely distant is suitable if the electrochemical cell is several orders of magnitude larger than the electrode.

The z = 0 axis is divided by a point at the electrode radius, $r_{\rm e}$, which equals 10 μ m. At $r < r_{\rm e}$, this axis represents the working electrode (microdisk) where the electrochemical reaction takes place. At $r > r_e$, this axis represents the surrounding insulator in-plane with the disk electrode.

DOMAIN EQUATIONS

We assume the presence of a large quantity of supporting electrolyte. This is inert salt that is added in electroanalytical experiments to increase the conductivity of the electrolyte without otherwise interfering with the reaction chemistry. Under these conditions, the resistance of the solution is sufficiently low that the electric field is negligible, and we can assume that the electrolyte potential $\phi_I = 0$ (Ref. 2).

The Electroanalysis interface implements chemical species transport equations for the reactant and product species of the redox couple subject to this assumption. The domain equation is the diffusion equation (also known as Fick's 2nd law), which describes the chemical transport of the electroactive species A and B. At steady-state, this reduces to:

$$\nabla \cdot (D_i \nabla c_i) = 0$$

BOUNDARY EQUATIONS

At the bulk boundary $(r \to \infty)$, we assume a uniform concentration equal to the bulk concentration for the reactant. The product has zero concentration here, as in bulk.

At the insulating (inert) surface, the normal flux of both species A and B equals zero, since this surface is impermeable and neither species reacts there.

At the electrode boundary, the reactant species A oxidizes (loses one electron) to form the product B. By convention, electrochemical reactions are written in the reductive direction:

$$B + e^{-} \leftrightarrow A$$

The stoichiometric coefficient is -1 for B, the "reactant" in the reductive direction, and + 1 for A, the "product" in the reductive direction. This formulation is consistent even in examples such as this model where at certain applied potentials, the reaction proceeds favorably to convert A to B. The number of electrons transferred, n, equals one.

The current density for this reaction is given by the electroanalytical Butler-Volmer equation for an oxidation:

$$i_{\text{loc}} = nFk_0 \left(c_{\text{A}} \exp\left(\frac{(n - \alpha_{\text{c}})F\eta}{RT}\right) - c_{\text{B}} \exp\left(\frac{-\alpha_{\text{c}}F\eta}{RT}\right) \right)$$

in which k_0 is the heterogeneous rate constant of the reaction, α_c is the cathodic transfer *coefficient*, and η is the overpotential at the working electrode.

According to Faraday's laws of electrolysis, the flux of the reactant and product species are proportional to the current density drawn:

$$-\mathbf{n} \cdot \mathbf{J}_i = \frac{\mathbf{v}_i i_{\text{loc}}}{nF}$$

This is expressed in the Electrode Surface boundary condition.

The total current recorded at the disk electrode can be extracted by integrating the local current density across the electrode surface. For this purpose, the Electroanalysis interface defines an electrode current variable according to

$$I_{\rm el} = \int_{S} i_{\rm loc} dA$$

Note that it is not sufficient to simply multiply by the area of the electrode, because the current density may be non-uniform.

STATIONARY STUDY

In contrast to macroelectrode voltammetry, a voltammogram recorded at a microdisk does not exhibit hysteresis. Diffusion is so fast on the time scale of the experiment that a stationary approximation is suitable. A quasistatic approximation applies when:

$$\frac{r_{\rm e}^2}{D} \ll \frac{RT}{Fv}$$

where v is the voltammetric scan rate (SI unit: V/s). The two terms in this inequality are respectively the diffusive and voltammetric time scales of the system.

Within the Stationary study, a parametric sweep is used to study the range of applied potentials achieved in the voltammogram.

Results and Discussion

The stationary concentration profile around a microdisk electrode (Figure 2) has a distinct shape. At large distances from the electrode, the concentration profile is roughly

hemispherical, but close to the disk edge the flux is elevated. For fast kinetics the concentrations on the electrode surface are roughly equilibrated and so are uniform. This leads to unequal flux over the surface of the electrode — it is nonuniformly accessible.

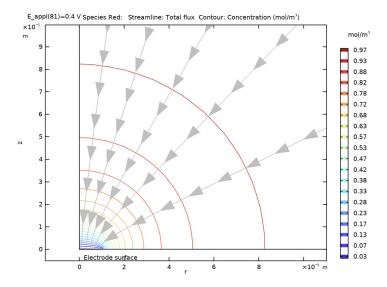


Figure 2: Characteristic concentration profile and mass flux streamlines for transportcontrolled oxidation of species A at a microdisk electrode (2D cross section).

The shape of the cyclic voltammogram (Figure 3) illustrates the relation between electrode kinetics and chemical species transport (diffusion).

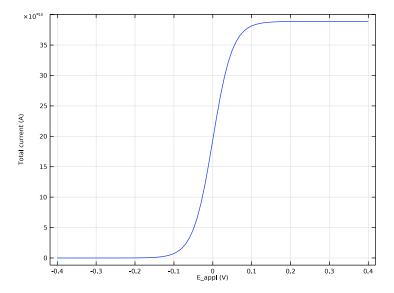


Figure 3: Quasistatic (steady-state) cyclic voltammetry recorded at a microdisk electrode. We can here see the limiting current density as explained below.

Initially, at reducing potentials, the oxidation reaction is not driven, and negligible current is drawn. As the potential moves toward the reduction potential of the redox couple (0 V), the oxidation reaction is accelerated and the current increases.

Once the oxidation reaction is fast enough that it consumes significant reactant at the electrode surface, the current becomes limited by the rate of transport of A toward the working electrode. Because the diffusion layer is equilibrated, this transport-limited current is constant in time and independent of applied potential. The analytical Saito equation gives this limiting current as (Ref. 3):

$$I_{\text{lim}} = 4nFcDr_{\text{e}}$$

where *c* is the bulk concentration of reactant.

Negative current is never observed for the "steady-state" voltammetry at a microdisk electrode, since the product species is effectively dispersed to bulk solution. Rapid diffusion on the voltammetric time scale ensures equilibration between the bulk and the electrode surface. Because of the absence of product in bulk, this equilibrium means that the reaction is always oxidative.

A refined mesh is required close to the electrode surface in order to accurately resolve the concentration profile, and hence the current. The mesh is refined further close to the singularity where the electrode and insulator boundaries meet. In the Infinite Element Domain, a Swept mesh is used.

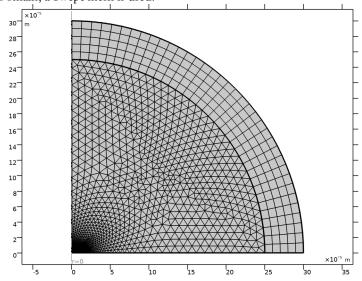


Figure 4: Customized mesh used for the microdisk analysis.

References

- 1. R.G. Compton and C.E. Banks, Understanding Voltammetry, 2nd ed., London, 2011.
- 2. A.J. Bard and L.R. Faulkner, Electrochemical Methods, Fundamentals and Applications, 2nd ed., Hoboken, 2001.
- 3. Y. Saito, Review of Polarography (Japan), vol. 15, pp. 177-187, 1968.

Application Library path: Fuel_Cell_and_Electrolyzer_Module/ General_Electrochemistry/microdisk_voltammetry

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select Electrochemistry>Electroanalysis (tcd).
- 3 Click Add.
- **4** In the **Concentrations** table, enter the following settings:

cRed c0x

- 5 Click 🔁 Study.
- 6 In the Select Study tree, select General Studies>Stationary.
- 7 Click M Done.

GLOBAL DEFINITIONS

Load the model parameters from a text file.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file microdisk_voltammetry_parameters.txt.

GEOMETRY I

Draw the model geometry as a quarter circle, and specify the electrode disk radius using a point.

Circle I (c1)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type r max.

4 In the Sector angle text field, type 90.

Point I (ptl)

- I In the Geometry toolbar, click Point
- 2 In the Settings window for Point, locate the Point section.
- 3 In the r text field, type re.

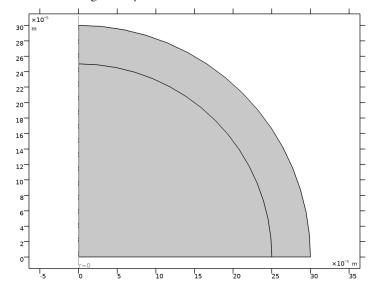
Circle I (c1)

Add a second circle that will be used to set up an Infinite Element domain.

Circle 2 (c2)

- I In the Model Builder window, under Component I (compl)>Geometry I right-click Circle I (cl) and choose Duplicate.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type r max*1.2.
- 4 In the Geometry toolbar, click 📳 Build All.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Your finalized geometry should now like this:



DEFINITIONS

Add an Infinite Element domain, and assign it to the outer domain.

Infinite Element Domain I (ie I)

- I In the Definitions toolbar, click ^{↑∞} Infinite Element Domain.
- 2 Select Domain 2 only.

ELECTROANALYSIS (TCD)

Electrolyte I

Now start setting up the physics. Start with the diffusion coefficients.

- I In the Model Builder window, under Component I (compl)>Electroanalysis (tcd) click Electrolyte 1.
- 2 In the Settings window for Electrolyte, locate the Diffusion section.
- **3** In the D_{cRed} text field, type D1.
- **4** In the $D_{\rm cOx}$ text field, type D2.

Electrode Surface 1

Add an Electrode Surface boundary node. Set up the electrode kinetics in the Electrode Reaction subnode.

- I In the Physics toolbar, click Boundaries and choose Electrode Surface.
- 2 In the Settings window for Electrode Surface, locate the **Electrode Phase Potential Condition** section.
- 3 From the Electrode phase potential condition list, choose Electrode potential.
- **4** In the E_{vsref} text field, type E_appl.
- **5** Select Boundary 2 only.

Electrode Reaction 1

- I In the Model Builder window, click Electrode Reaction I.
- 2 In the Settings window for Electrode Reaction, locate the Stoichiometric Coefficients section.
- 3 In the v_{cRed} text field, type 1.
- 4 In the v_{cOx} text field, type -1.
- **5** Locate the **Equilibrium Potential** section. In the $E_{\rm eq,ref}(T)$ text field, type Ef.
- **6** Locate the **Electrode Kinetics** section. In the $i_{0,\mathrm{ref}}(T)$ text field, type iOref.

Concentration I

Specify the bulk composition at the outer boundary.

I In the Physics toolbar, click — Boundaries and choose Concentration.

- 2 Select Boundary 7 only.
- 3 In the Settings window for Concentration, locate the Concentration section.
- **4** Select the **Species cRed** check box.
- **5** In the $c_{0,\text{cRed}}$ text field, type c_bulk.
- **6** Select the **Species cOx** check box.

Initial Values 1

- I In the Model Builder window, click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the cRed text field, type c bulk.

MESH I

Edit the default mesh to ensure good numerical accuracy.

Size

- I In the Model Builder window, under Component I (compl) right-click Mesh I and choose Edit Physics-Induced Sequence.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** From the **Predefined** list, choose **Finer**.
- 4 Click to expand the **Element Size Parameters** section. In the **Maximum element growth rate** text field, type 1.1.

Free Triangular 1

- I In the Model Builder window, click Free Triangular I.
- 2 In the Settings window for Free Triangular, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 1 only.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 4 only.
- **5** Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type re/100.

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domain 2 only.
- 5 In the Model Builder window, right-click Mesh I and choose Build All.

STUDY I

The problem is now ready for solving. Simulate a voltammogram by using a Parametric Sweep for a range of applied potentials.

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
E_appl (Applied potential)	range(E_start,E_step, E_vertex)	V

5 In the Study toolbar, click **Compute**.

RESULTS

Concentration, Red (tcd)

Two concentration plots are created by default for each species: one in 2D and one revolved 3D plot.

Modify the first default plot as follows:

DEFINITIONS

Change the default 2D view to show the results more clearly. Start by changing the view for the model and its plot. We want to position the view close to the electrode surface.

Axis

- I In the Model Builder window, expand the Component I (compl)>Definitions>View I node, then click **Axis**.
- 2 In the Settings window for Axis, locate the Axis section.

- 3 In the r minimum text field, type -1e-6.
- 4 In the r maximum text field, type 10e-5.
- 5 In the z minimum text field, type -0.5e-6.
- 6 In the z maximum text field, type 10e-5.
- 7 Click (Update.

RESULTS

Concentration, Red (tcd)

- I In the Model Builder window, expand the Results>Concentration, Red (tcd) node, then click Concentration, Red (tcd).
- 2 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 3 Select the x-axis label check box. In the associated text field, type r.
- 4 Select the y-axis label check box. In the associated text field, type z.
- 5 Locate the Color Legend section. Select the Show units check box.

Surface 1

Next, replace the surface plot with a contour plot for the concentration. Keep the streamlines for the total flux that show the increased reaction rate at the electrode edge compared with the center of the electrode.

In the Model Builder window, right-click Surface I and choose Disable.

Contour I

- I In the Model Builder window, right-click Concentration, Red (tcd) and choose Contour.
- 2 In the Settings window for Contour, locate the Expression section.
- 3 In the Expression text field, type cRed.
- 4 Locate the Coloring and Style section. From the Contour type list, choose Tube.
- 5 Select the Radius scale factor check box. In the associated text field, type 1.2E-7.
- 6 Click Change Color Table.
- 7 In the Color Table dialog box, select Rainbow>RainbowLight in the tree.
- 8 Click OK.

Streamline I

Polish the default streamline plot a little.

- I In the Model Builder window, click Streamline I.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.

- 3 From the Positioning list, choose On selected boundaries.
- 4 In the Number text field, type 5.
- **5** Locate the **Selection** section. Click to select the **E Activate Selection** toggle button.
- **6** Select Boundary 2 only.
- 7 Locate the Coloring and Style section. Find the Point style subsection. From the Arrow length list, choose Normalized.
- 8 Select the Number of arrows check box. In the associated text field, type 100.

Concentration, Red (tcd)

Also add a line to mark the electrode.

line l

- I In the Model Builder window, right-click Concentration, Red (tcd) and choose Line.
- 2 In the Settings window for Line, locate the Expression section.
- 3 In the Expression text field, type 1.
- **4** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Coloring and Style section. From the Line type list, choose Tube.
- 6 Select the Radius scale factor check box. In the associated text field, type 0.4E-6.
- **7** From the Coloring list, choose Uniform.
- 8 From the Color list, choose Gray.

Selection 1

- I Right-click Line I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 Click Paste Selection.
- **4** In the **Paste Selection** dialog box, type **2** in the **Selection** text field.
- 5 Click OK.

Annotation I

- I In the Model Builder window, right-click Concentration, Red (tcd) and choose Annotation.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type **Electrode** surface.
- 4 Locate the **Position** section. In the **Z** text field, type -1.5e-6.
- 5 Locate the Coloring and Style section. Clear the Show point check box.

Total current

Create a plot of the voltammogram as follows.

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Total current in the Label text field.
- 3 Locate the Legend section. Clear the Show legends check box.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **None**.

Global I

- I Right-click Total current and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Electroanalysis> Electrode kinetics>tcd.ltot esl - Total current - A.
- 3 In the Total current toolbar, click Plot.