

Porous Catalytic Reactor with Injection Needle

Introduction

Heterogeneous catalytic reactors have been widely used in the chemical engineering industry. This type of gas-solid catalytic reactors, where gas phase reactions are catalyzed by a solid catalyst, have widespread applications in the areas such as catalytic oxidation and selective catalytic reduction. This example illustrates the modeling of a porous catalytic reactor for hydrogen oxidation on a noble metal Rh catalyst dispersed on an alumina support (Rh/Al₂O₃). The model investigates the kinetics of the heterogeneous catalytic reaction system, the species concentration distribution (both the species in the bulk gas phase and absorbed on the catalytic surface) and the velocity field in the pore volume.

First, the hydrogen oxidation rate and the rates of adsorption and desorption for all species are studied by using the Reaction Engineering interface, assuming that the chemical system is perfectly mixed. Then, in a space-dependent model of the porous catalytic reactor, the concentration and velocity fields are investigated by using the Transport of Diluted Species in Porous Catalysts interface, which is a combination of Transport of Diluted Species with Porous Catalyst feature and the Brinkman Equation interfaces. The thermodynamic and kinetic properties of the reaction system in the space-dependent model are provided using a Chemistry interface.

Model Definition

HETEROGENEOUS CATALYTIC REACTIONS

For a gas-solid catalytic reaction, the reaction rate (R_s) can be expressed as

$$R_s = \frac{n_{\text{prod}}}{(\text{time})(\text{catalystunit})}$$

where n_{prod} is the number of product moles; catalystunit is the measure unit of catalyst amount, which has following different unit bases:

- Active surface area of catalyst (m²)
- Unit mass of catalyst (kg)
- Unit volume of catalyst (m³)
- · Active metal loading percentage

The reaction-rate unit depends on the measurement unit of the catalyst. In the Porous Catalyst feature in the Transport of Diluted Species and Transport of Concentrated Species interfaces, there are two measure units for the catalyst: one based on the surface area (m^2) and another based on the mass amount (kg).

A general surface reaction can be written as

$$A(ads) + B(ads) \xrightarrow{k_f} AB(ads)$$

The reaction rate of this elemental reaction is

$$R_s = k_f \theta_A \theta_B - k_r \theta_{AB}$$

where k_f and k_r are the forward and backward reaction rate constants, respectively, and θ_A , θ_B , and θ_{AB} are the surface coverages of surface species A(ads), B(ads), and AB(ads). The coefficient k_f has the form

$$k_f = AT^{\beta} \exp\left(\frac{-E}{RT}\right)$$

where

- A is a pre-exponential factor
- *T* is the temperature (K)
- β is the temperature exponent
- *E* is the activation energy (J/mol)
- R is the gas constant $(J/(mol \cdot K))$

The rate constant k_r has the same form as that for k_f . Alternatively, it can be obtained from the reaction equilibrium constant (K_0):

$$k_r = \frac{k_f}{K_0}$$

The gas-solid catalytic reaction system of $H_2 + O_2 + H_2O$ on Rh/Al₂O₃ catalyst is investigated using the Reaction Engineering interface. The following reactions are considered:

• Gaseous H₂ being dissociatively adsorbed on two neighboring Rh sites:

$$H_2 + 2Rh(ads) = 2H(ads)$$

• Gaseous O₂ being dissociatively absorbed on two neighboring Rh sites:

$$O_2 + 2Rh(ads) = 2O(ads)$$

• Gaseous H₂O being absorbed on a Rh site:

$$H_2O + Rh(ads) = H_2O(ads)$$

• The surface reactions of the adsorbed species H(ads), O(ads), OH(ads), and H₂O(ads):

O(ads) + H(ads) = OH(ads) + Rh(ads) $OH(ads) + H(ads) = H_2O(ads) + Rh(ads)$ $OH(ads) + OH(ads) = O(ads) + H_2O(ads)$

The thermodynamic and kinetic behaviors of all species and reactions can be simulated provided that the rate constants k_f and k_r are available for these six reactions.

After the initial analysis of the gas-solid reaction system in the Reaction Engineering interface, the reaction system will be exported to a Chemistry interface using the Generate Space-Dependent Model feature. The Chemistry interface will then be used to define the gas-solid reaction system in the space-dependent model.

SPACE-DEPENDENT MODEL OF POROUS CATALYTIC REACTOR

The reactor consists of a tubular structure, with an injection tube whose main axis is perpendicular to the reactor axis. The reactor geometry is shown in Figure 1. The incoming species in the main and injection tubes react in a fixed porous catalyst bed. The model couples the free fluid and porous media flow through the Brinkman equation interface. This physics interface includes two physics features for modeling the fluid flow, one being Porous Medium for porous domain, and the other being Fluid Properties for free flow domain. Because of symmetry, only one half of the reactor is modeled.



Figure 1: The species O_2 and H_2 enter the reactor from the main and injection tubes, respectively, and react in a fixed porous catalyst bed to produce H_2O .

In the porous catalyst domain, the hydrogen oxidation on the Rh/Al₂O₃ catalyst takes place. The net reaction of the gas phase species is $2H_2 + O2 \rightarrow 2H_2O$.

Governing Equations

The Navier–Stokes equations describe the fluid flow in the free-flow regions. In the porous domain, the Brinkman equations for porous media apply.

As the modeled species are present in low concentrations, diffusion is assumed to take place according to Fick's law. The mass transport for the three species H_2 , O_2 , and H_2O can therefore be modeled with the following convection-diffusion equation

$$\mathbf{u} \cdot \nabla c_i = \nabla \cdot (D_i \nabla c_i) + R_i \tag{1}$$

In this equation, c_i denotes the concentration (SI unit: mol/m³), D_i the diffusivity (SI unit: m²/s), and R_i the reaction rate for species i (SI unit: mol/(m³·s)). Because the reaction takes place in the porous bed only, the reaction term is zero in the free-flow regions. The reaction rate R_i is contributed by the surface reaction, which takes place inside the porous catalyst material.

The bulk transport species H_2 , O_2 , and H_2O adsorb onto the active sites on the Rh catalyst surface. The adsorption of H_2 , O_2 , and H_2O is described using the Langmuir adsorption isotherm:

$$c_{\mathrm{P, e, }i} = \frac{K_{\mathrm{L,}i}c_{\mathrm{Pmax,}i}c_{i}}{1 + K_{\mathrm{L,}i}c_{i}}$$

Here, for species *i*,

- $c_{\mathrm{P,e},i}$ is the equilibrium amount adsorbed on the catalyst (mol/kg),
- K_{L,i} is the Langmuir constant (m³/mol),
- c_{Pmax.i} is the maximum adsorbed amount (mol/kg), and
- c_i is the species molar concentration in the gas phase (mol/m³)

In the Langmuir isotherm, the equilibrium adsorbed amount is dependent both on the maximum possible amount adsorbed ($c_{Pmax,i}$), and the bulk concentration of species *i* (c_i). If the bulk concentration is zero, the equilibrium concentration is also zero.

The equilibrium molar concentration $(c_{eq,i}, \text{mol/m}^3)$ for adsorbed species *i* is given by

$$c_{\text{eq},i} = \rho_{\text{b}} c_{\text{P},e,i} \tag{2}$$

where ρ_b is the catalyst bulk density.

For the adsorbed species concentration $c_{ads,i} \pmod{m^2}$, its corresponding volumetric concentration $c_{vol,i} \pmod{m^3}$ is

$$c_{\text{vol},i} = S_{\text{area,cat}} c_{\text{ads},i} \tag{3}$$

Using Equation 2 and Equation 3, the adsorption/desorption rate $R_{ads,i}$ (mol/(m³·s)) is defined as

$$R_{\text{ads},i} = h_{\text{LDF},i}(c_{\text{vol},i} - c_{\text{eq},i})$$

where $h_{\text{LDF},i}$ is the mass transfer coefficient (1/s), which is based on based on a linear driving force. The adsorption rate is a mass source term and contributes to the bulk reaction rate R_i in Equation 1. With this definition, a positive $R_{\text{ads},i}$ corresponds to desorption of species *i*, i.e. a positive source term of species *i* in Equation 1.

For the adsorbed species, the governing equation is

$$\frac{dc_{\mathrm{ads},i}}{dt} = R_{\mathrm{s,\,ads},\,i}$$

and for other surface species (without mass transfer between the bulk and the catalyst surface)

$$\frac{dc_{\text{surf},i}}{dt} = R_{\text{s, surf},i}$$

where $R_{s,ads,i}$ and $R_{s,surf,i}$ are the surface reaction rates for adsorbed and surface species, respectively.

Boundary Conditions

In the Brinkman Equations interface, a constant velocity profile is assumed at the inlet boundaries:

$$\mathbf{u} = u_{in}$$

For the outlet, a zero pressure condition is applied.

In the Transport of Diluted Species in Porous Catalysts interface, the concentrations at the inflows are fixed:

$$c_i = c_{i0, \text{ inlet}}$$

At the outflow, the convection is assumed to dominate the mass transport:

$$\mathbf{n} \cdot (-D_i \nabla c_i) = 0$$

This implies that the gradient of c_i in the direction perpendicular to the outlet boundary is negligible. This is a common assumption for tubular reactors with a high degree of transport by convection in the direction of the main reactor axis. The condition eliminates the need for specifying a concentration or a fixed value for the flux at the outlet boundary. At all other boundaries, no flux conditions apply:

$$\mathbf{n} \cdot (-D_i \nabla c_i + c_i \mathbf{u}) = 0$$

Results and Discussion

Figure 2 shows the velocity magnitude. The flow is almost homogeneous in the porous part of the reactor.

m/s 300 0.45 ⁶4₂₀ mm 0.4 250 10 0.35 5 200 0.3 0 -5 0.25 150 60 0.2 40 0.15 100 20 mm 0.1 50 0.05 0 0

Time=1 s Slice: Velocity magnitude (m/s) Surface: br.U*1[cm]/br.nu (1) Arrow Surface: Velocity field

Figure 2: Magnitude of the velocity field in the free and porous reactor domains.

Figure 3 shows the pressure drop, which occurs mainly across the porous bed.



Figure 3: The pressure drop across the reactor.



Figure 4 and Figure 5 show the concentrations of species H_2 and $\mathrm{O}_2,$ respectively.



Time=1 s Streamline: Total flux Isosurface: Concentration (mol/m³)



Figure 5: Isoconcentration surfaces for species O₂.

Figure 4 shows that the concentration of the injected species H_2 decreases very rapidly with distance from the injection point due to quick mixing with the main flow. It also

shows that hydrogen is consumed in the porous catalyst domain. The rate of hydrogen oxidation is significantly lower after about half the bed length, meaning that half the bed is poorly utilized. This indicates an opportunity for optimizing the reactor design by e.g. using a thinner catalyst bed. Figure 5 shows the isoconcentration surfaces of species O_2 , which is introduced in the main channel of the reactor. Similar to the species H_2 , its concentration also decreases across the porous domain. The injection of H_2 results in a reduction in O_2 concentration at the injection point.

Figure 6 and Figure 7 show the surface concentration distributions along the center line of the porous catalyst bed for adsorbed, and for surface species, respectively. There is a surplus of oxygen in the gas phase. The surface-gas equilibrium, as expressed by the Langmuir isotherm, limits the conversion of hydrogen to water, so that the concentration of hydrogen in the gas phase does not reach zero. As the hydrogen concentration in the gas phase outside the porous catalyst decreases, the adsorption rate of hydrogen decreases, and thus also the hydrogen adatom concentration on the surface. With less hydrogen present on the surface, the rate of oxygen removal (water formation) from the surface decreases. The net effect is that, after about half the bed length, the empty Rh surface sites are successively covered by oxygen adatoms.



Figure 6: Concentration distribution along the center line of catalyst for surface species.



Figure 7: Concentration distribution along the center line of catalyst for adsorbed species.

Application Library path: Chemical_Reaction_Engineering_Module/ Reactors_with_Porous_Catalysts/porous_reactor

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🙆 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 0D.
- 2 In the Select Physics tree, select Chemical Species Transport>Reaction Engineering (re).
- 3 Click Add.
- 4 Click 😔 Study.

- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click **M** Done.

Load reaction parameters (general) from a text file.

GLOBAL DEFINITIONS

Parameters 1, reaction

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, type Parameters 1, reaction in the Label text field.
- 3 Locate the Parameters section. Click 📂 Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file porous_reactor_reaction_parameters.txt.

REACTION ENGINEERING (RE)

- I In the Model Builder window, under Component I (compl) click Reaction Engineering (re).
- 2 In the Settings window for Reaction Engineering, locate the Energy Balance section.
- **3** In the *T* text field, type T_iso.

Create the H2+02 reaction system over the Rh/A1203 catalyst.

Reaction I

- I In the Reaction Engineering toolbar, click 👗 Reaction.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type H2+2Rh(ads)<=>2H(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf1.
- **6** In the $k^{\mathbf{r}}$ text field, type kr1.

Reaction 2

- I In the **Reaction Engineering** toolbar, click <u>A</u> **Reaction**.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type 02+2Rh(ads)<=>20(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf2.
- **6** In the $k^{\mathbf{r}}$ text field, type kr2.

Reaction 3

- I In the Reaction Engineering toolbar, click 👗 Reaction.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- **3** In the **Formula** text field, type H2O+Rh(ads)<=>H2O(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf3.
- **6** In the $k^{\mathbf{r}}$ text field, type kr3.

Reaction 4

- I In the **Reaction Engineering** toolbar, click 👗 **Reaction**.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type O(ads)+H(ads)<=>OH(ads)+Rh(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf4.
- **6** In the $k^{\mathbf{r}}$ text field, type kr4.

Reaction 5

- I In the **Reaction Engineering** toolbar, click 👗 **Reaction**.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type OH(ads)+H(ads)<=>H2O(ads)+Rh(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf5.
- **6** In the $k^{\rm r}$ text field, type kr5.

Reaction 6

- I In the **Reaction Engineering** toolbar, click 👗 **Reaction**.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type OH(ads)+OH(ads)<=>0(ads)+H20(ads).
- 4 Click Apply.
- **5** Locate the **Rate Constants** section. In the k^{f} text field, type kf6.
- **6** In the $k^{\mathbf{r}}$ text field, type kr6.

Species 1

I In the Reaction Engineering toolbar, click 📩 Species.

Add a solvent (N2). It is not involved in any reaction but it will later be exported to a space-dependent model.

- 2 In the Settings window for Species, locate the Name section.
- **3** In the text field, type N2.
- 4 Locate the Type section. From the list, choose Solvent.

Enter the reactive specific surface for the surface reactions.

- 5 In the Model Builder window, click Reaction Engineering (re).
- 6 In the Settings window for Reaction Engineering, locate the Reactor section.
- 7 Find the Surface reaction area subsection. Click the Surface area to volume ratio button.
- **8** In the a_s text field, type cat_area.

Initial Values 1

- I In the Model Builder window, click Initial Values I.
- **2** In the **Settings** window for **Initial Values**, locate the **Volumetric Species Initial Values** section.
- **3** In the table, enter the following settings:

Species	Concentration (mol/m ³)
H2	cOH2_inflow
N2	c0N2
O2	c002_inflow

4 Locate the Surface Species Initial Values section. In the $\Gamma_{\rm s}$ text field, type 2.72E-5.

5 In the table, enter the following settings:

Species	Surface concentration (mol/m^2)	Site occupancy number (1)
H(ads)	cOH_surf	1
H2O(ads)	c0H20_surf	1
O(ads)	c00_surf	1
OH(ads)	c00H_surf	1
Rh(ads)	cORh_surf	1

STUDY I

- Step 1: Time Dependent
- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the **Output times** text field, type range(0,0.01,0.2).
- **4** In the **Home** toolbar, click **= Compute**.

RESULTS

Concentration (re), bulk species

- I Right-click Results>Concentration (re) and choose Rename.
- 2 In the Rename ID Plot Group dialog box, type Concentration (re), bulk species in the New label text field.
- 3 Click OK.

Plot the bulk species concentrations.

Global I

- I In the Model Builder window, expand the Concentration (re), bulk species node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- 3 Click 📐 Clear Table.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c_H2 - Concentration mol/m³.
- 5 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c_H2O Concentration mol/m³.
- 6 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c_02 Concentration mol/m³.
- 7 In the Concentration (re), bulk species toolbar, click **O** Plot.
- 8 Click the 🕂 Zoom Extents button in the Graphics toolbar.

Create a figure for surface species concentrations.

Concentration (re), surface species

I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.

2 In the Settings window for ID Plot Group, type Concentration (re), surface species in the Label text field.

Global I

- I Right-click Concentration (re), surface species and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- 3 Click **Clear Table**.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.csurf_H_surf Surface concentration mol/m².
- 5 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.csurf_0_surf Surface concentration mol/m².
- 6 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.csurf_OH_surf Surface concentration mol/m².
- 7 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.csurf_H2O_surf Surface concentration mol/m².
- 8 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.csurf_Rh_surf Surface concentration mol/m².
- 9 Click the **x-Axis Log Scale** button in the **Graphics** toolbar.
- **IO** Click the **y-Axis Log Scale** button in the **Graphics** toolbar.
- II In the Concentration (re), surface species toolbar, click 💿 Plot.

12 Click the **F Zoom Extents** button in the **Graphics** toolbar.

Export catalytic oxidation of hydrogen over Rh/Al203 to a space-dependent model.

REACTION ENGINEERING (RE)

Generate Space-Dependent Model I

- I In the Reaction Engineering toolbar, click 🖙 Generate Space-Dependent Model.
- **2** In the **Settings** window for **Generate Space-Dependent Model**, locate the **Physics Interfaces** section.
- **3** Find the **Chemical species transport** subsection. From the list, choose **Transport of Diluted Species in Porous Catalysts: New**.

- 4 Locate the Study Type section. From the Study type list, choose Time dependent.
- 5 Locate the Space-Dependent Model Generation section. Click Create/Refresh.Load catalyst parameters from a text file.

GLOBAL DEFINITIONS

Parameters 2, catalyst

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, type Parameters 2, catalyst in the Label text field.
- 3 Locate the Parameters section. Click 📂 Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file porous_reactor_catalyst_parameters.txt.

COMPONENT 2 (COMP2)

Build the geometry for the catalytic reactor.

I In the Model Builder window, expand the Component 2 (comp2) node.

GEOMETRY I(3D)

- I In the Model Builder window, expand the Component 2 (comp2)>Geometry 1(3D) node, then click Geometry 1(3D).
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Cylinder I (cyl1)

- I In the **Geometry** toolbar, click 💭 **Cylinder**.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type do_reac/2.
- 4 In the **Height** text field, type 5*do_reac.
- 5 Locate the Axis section. From the Axis type list, choose Cartesian.
- **6** In the **x** text field, type **1**.
- **7** In the **z** text field, type **0**.
- 8 Click to expand the Layers section. In the table, enter the following settings:

Layer name	Thickness (mm)	
Layer 1	wt_reac	

Cylinder 2 (cyl2)

- I In the **Geometry** toolbar, click 问 **Cylinder**.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type do_reac/2-wt_reac.
- 4 In the **Height** text field, type 0.7*do_reac.
- 5 Locate the **Position** section. In the **x** text field, type 3*do_reac.
- 6 Locate the Axis section. From the Axis type list, choose Cartesian.
- 7 In the **x** text field, type 1.
- **8** In the **z** text field, type 0.

Cylinder 3 (cyl3)

- I In the **Geometry** toolbar, click **(_____ Cylinder**.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the **Radius** text field, type do_needle/2.
- 4 In the **Height** text field, type do_reac.
- 5 Locate the **Position** section. In the **x** text field, type 2.7*do_reac/2.
- 6 Locate the Layers section. In the table, enter the following settings:

Layer name	Thickness (mm)
Layer 1	wt_needle

Difference I (dif1)

- I In the Geometry toolbar, click is Booleans and Partitions and choose Difference.
- 2 Select the object cyll only.
- 3 In the Settings window for Difference, locate the Difference section.
- **4** Find the **Objects to subtract** subsection. Click to select the **Delta Activate Selection** toggle button.
- **5** Select the object **cyl3** only.
- 6 Select the Keep objects to subtract check box.

Union I (uni I)

- I In the Geometry toolbar, click 📕 Booleans and Partitions and choose Union.
- 2 Select the objects cyl3 and difl only.
- 3 In the Settings window for Union, locate the Union section.
- 4 Click **Paste Selection**.

- 5 In the Paste Selection dialog box, type cy12 in the Selection text field.
- 6 Click OK.

Block I (blk1)

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 5*do_reac.
- 4 In the **Depth** text field, type 2*do_reac.
- 5 In the **Height** text field, type 3*do_reac.
- 6 Locate the **Position** section. In the **y** text field, type -2*do_reac.
- 7 In the z text field, type -1.5*do_reac.

Difference 2 (dif2)

- I In the Geometry toolbar, click i Booleans and Partitions and choose Difference.
- 2 Select the object unil only.
- 3 In the Settings window for Difference, locate the Difference section.
- **4** Find the **Objects to subtract** subsection. Click to select the **Activate Selection** toggle button.
- 5 Select the object **blk1** only.

Form Union (fin)

In the Geometry toolbar, click 📗 Build All.

Add a Mesh Control Faces feature to control the mesh in the vertical injection needle.

Mesh Control Faces 1 (mcfl)

I In the Geometry toolbar, click 🏠 Virtual Operations and choose Mesh Control Faces.

Select the faces corresponding to the symmetry plane and the outlet into the reactor.

2 On the object fin, select Boundaries 19 and 20 only.

Ignore Faces 1 (igf1)

- I In the Geometry toolbar, click 🏷 Virtual Operations and choose Ignore Faces.
- 2 In the Settings window for Ignore Faces, locate the Input section.
- **3** Click **Paste Selection**.
- 4 In the Paste Selection dialog box, type 11, 20 in the Selection text field.
- 5 Click OK.
- 6 In the Geometry toolbar, click 🟢 Build All.

DEFINITIONS (COMP2)

Create a geometry selection list for model entities.

Catalyst Bed

- I In the Model Builder window, expand the Component 2 (comp2)>Definitions node.
- 2 Right-click Component 2 (comp2)>Definitions and choose Selections>Explicit.
- 3 In the Settings window for Explicit, type Catalyst Bed in the Label text field.
- **4** Select Domain 4 only.

Symmetry plane

- I In the **Definitions** toolbar, click 🗞 **Explicit**.
- 2 In the Settings window for Explicit, type Symmetry plane in the Label text field.
- **3** Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 5, 19, and 22 only.

Inlet species O2

- I In the Definitions toolbar, click 🐚 Explicit.
- 2 In the Settings window for Explicit, type Inlet species 02 in the Label text field.
- **3** Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- **4** Select Boundary 4 only.

Inlet species H2

- I In the **Definitions** toolbar, click http://www.click
- 2 In the Settings window for Explicit, type Inlet species H2 in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- **4** Select Boundary 15 only.

Outlet

- I In the **Definitions** toolbar, click 🗞 **Explicit**.
- 2 In the Settings window for Explicit, type Outlet in the Label text field.
- **3** Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundary 25 only.

First Free-Porous Interface

- I In the **Definitions** toolbar, click **** Cylinder**.
- 2 In the Settings window for Cylinder, type First Free-Porous Interface in the Label text field.

- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Size and Shape section. In the Top distance text field, type 0.5*do_reac.
- 5 In the Bottom distance text field, type 0.
- 6 Locate the **Position** section. In the **x** text field, type 2.5*do_reac.
- 7 In the y text field, type 0.25*do_reac.
- 8 Locate the Axis section. From the Axis type list, choose x-axis.

Free Flow Domains

- I In the Definitions toolbar, click 🗞 Explicit.
- 2 In the Settings window for Explicit, type Free Flow Domains in the Label text field.
- **3** Select Domains 2 and 5 only.

Free and Porous Media Domains

- I In the **Definitions** toolbar, click **H Union**.
- 2 In the Settings window for Union, type Free and Porous Media Domains in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- **4** In the **Add** dialog box, in the **Selections to add** list, choose **Catalyst Bed** and **Free Flow Domains**.
- 5 Click OK.

Solid Domains

- I In the Definitions toolbar, click 🗞 Adjacent.
- 2 In the Settings window for Adjacent, type Solid Domains in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, select Free and Porous Media Domains in the Input selections list.
- 5 Click OK.
- 6 In the Settings window for Adjacent, locate the Output Entities section.
- 7 From the Geometric entity level list, choose Adjacent domains.

Solid Bnds

- I In the Definitions toolbar, click 🐂 Adjacent.
- 2 In the Settings window for Adjacent, type Solid Bnds in the Label text field.
- **3** Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, select Solid Domains in the Input selections list.

5 Click OK.

Porous Bed Bnds

- I In the Definitions toolbar, click 🗞 Adjacent.
- 2 In the Settings window for Adjacent, type Porous Bed Bnds in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, select Catalyst Bed in the Input selections list.
- 5 Click OK.

Outer Bnds

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, type Outer Bnds in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- **4** Locate the **Input Entities** section. Under **Selections to add**, click + **Add**.
- 5 In the Add dialog box, select Solid Bnds in the Selections to add list.
- 6 Click OK.
- 7 In the Settings window for Difference, locate the Input Entities section.
- **8** Under Selections to subtract, click + Add.
- 9 In the Add dialog box, select Porous Bed Bnds in the Selections to subtract list.
- IO Click OK.

Bed Bnds

- I In the **Definitions** toolbar, click 🗞 **Explicit**.
- 2 In the Settings window for Explicit, type Bed Bnds in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- **4** Click to select the **EXECUTE** Activate Selection toggle button.
- 5 Click Paste Selection.
- 6 In the Paste Selection dialog box, type 18,20,21 in the Selection text field.
- 7 Click OK.

COMPONENT 2 (COMP2)

Add a Brinkman Equations physics interface to the newly generated component.

ADD PHYSICS

I In the Home toolbar, click 🖄 Add Physics to open the Add Physics window.

- 2 Go to the Add Physics window.
- 3 In the tree, select Fluid Flow>Porous Media and Subsurface Flow>Brinkman Equations (br).
- 4 Click Add to Component 2 in the window toolbar.
- 5 In the Home toolbar, click 🖄 Add Physics to close the Add Physics window.

MATERIALS

Add a Material node for nitrogen.

ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Liquids and Gases>Gases>Nitrogen.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

Add a porous material for the **Porous Catalyst** feature.

MATERIALS

Porous Material I (pmat1)

- I In the Model Builder window, under Component 2 (comp2) right-click Materials and choose More Materials>Porous Material.
- **2** Select Domain 4 only.
- Fluid I (pmat1.fluid1)

Right-click Porous Material I (pmatl) and choose Fluid.

Fluid I (pmat1.fluid1)

- I In the Model Builder window, expand the Component 2 (comp2)>Materials> Porous Material I (pmat1) node, then click Fluid I (pmat1.fluid1).
- 2 In the Settings window for Fluid, locate the Fluid Properties section.
- 3 From the Material list, choose Nitrogen (matl).

Solid I (pmat1.solid1)

- I In the Model Builder window, right-click Porous Material I (pmatl) and choose Solid.
- 2 In the Settings window for Solid, locate the Solid Properties section.
- **3** In the θ_8 text field, type **0.7**.

4 Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	2800	kg/m³	Basic

Porous Material I (pmat1)

- I In the Model Builder window, click Porous Material I (pmatl).
- 2 In the Settings window for Porous Material, locate the Homogenized Properties section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Permeability	kappa_iso ; kappaii = kappa_iso,	1e-9	m²	Basic
	kappaij = 0			

MULTIPHYSICS

Reacting Flow, Diluted Species 1 (rfd1)

In the Physics toolbar, click A Multiphysics Couplings and choose Domain>Reacting Flow, Diluted Species.

TRANSPORT OF DILUTED SPECIES IN POROUS CATALYSTS (TDS)

- I In the Model Builder window, click Transport of Diluted Species in Porous Catalysts (tds).
- 2 In the Settings window for Transport of Diluted Species in Porous Catalysts, locate the Domain Selection section.
- **3** From the Selection list, choose Free and Porous Media Domains.

Set all parameters for the **Porous Catalyst** feature and its subfeatures.

Porous Catalyst I

Assume that all the bulk species (from the **Transport of Diluted Species** interface) are adsorbed into the catalyst. Enter the initial concentrations for the these species.

I In the Model Builder window, expand the

Transport of Diluted Species in Porous Catalysts (tds) node, then click Porous Catalyst I.

- 2 In the Settings window for Porous Catalyst, locate the Adsorbed Species section.
- **3** In the $\Gamma_{0,cH2ads}$ text field, type **0**.
- **4** In the $\Gamma_{0.cH2Oads}$ text field, type **0**.

5 In the $\Gamma_{0,cO2ads}$ text field, type 0.

The surface species H2O is assumed to be an adsorbed species. Remove it from the **Surface Species** table.

- 6 Locate the Surface Species section. Click to select row number 2 in the table.
- 7 Click 🗮 Delete.

Enter the initial molar concentrations for the other surface species.

8 In the table, enter the following settings:

Surface species	Initial values (mol/m^2)
Н	cOH_surf
0	c00_surf
ОН	c00H_surf
Rh	cORh_surf

Fluid I

Select the diffusion coefficients from Chemistry.

- I In the Model Builder window, expand the Porous Catalyst I node, then click Fluid I.
- 2 In the Settings window for Fluid, locate the Diffusion section.
- **3** From the D_{cH2} list, choose Diffusion coefficient, H2 in N2 (solvent) (chem).
- 4 From the D_{cH2O} list, choose Diffusion coefficient, H2O in N2 (solvent) (chem).
- 5 From the $D_{\rm cO2}$ list, choose Diffusion coefficient , O2 in N2 (solvent) (chem).
- 6 From the Effective diffusivity model list, choose Bruggeman model.

Adsorption I

Enter the model parameters for the Langmuir adsorption isotherm model.

- I In the Model Builder window, click Adsorption I.
- 2 In the Settings window for Adsorption, locate the Adsorption section.
- 3 Select the Species cH2 check box.
- **4** In the $K_{\text{L,cH2}}$ text field, type k1H2_ads.
- **5** In the $c_{P,max,cH2}$ text field, type cplH2_ads.
- 6 In the $h_{\text{LDF,cH2}}$ text field, type kfH2_ads.
- 7 Select the Species cH20 check box.
- 8 In the $K_{L,cH2O}$ text field, type k1H20_ads.
- **9** In the $c_{P,max,cH2O}$ text field, type cplH20_ads.

IO In the $h_{\text{LDF,cH2O}}$ text field, type kfH20_ads.

II Select the Species cO2 check box.

12 In the $K_{\text{L,cO2}}$ text field, type k102_ads.

I3 In the $c_{P,max,cO2}$ text field, type cpl02_ads.

I4 In the $h_{\text{LDF,cO2}}$ text field, type kf02_ads.

Surface Reaction 1

The adsorbed species H20 also takes part in the surface reactions. Couple its reaction rate to the surface species H20 in **Chemistry**.

- I In the Model Builder window, click Surface Reaction I.
- 2 In the Settings window for Surface Reaction, locate the Surface Reaction Rate for Adsorbed Species section.
- 3 From the $R_{cadscH2O}$ ^s list, choose Surface reaction rate for surface species H2O_surf (chem).

CHEMISTRY I (CHEM)

- I In the Model Builder window, under Component 2 (comp2) click Chemistry I (chem).
- 2 In the Settings window for Chemistry, locate the Species Matching section.

3 Find the Surface species subsection. In the table, enter the following settings:

Species	Species concentration type	Surface concentration (mol/m^2)
H2O(ads)	Variable	tds.cads_cH20

DEFINITIONS (COMP2)

Variables 1, bulk concentration defined from surface concentration

- I In the Model Builder window, under Component 2 (comp2) right-click Definitions and choose Variables.
- 2 In the **Settings** window for **Variables**, type Variables 1, bulk concentration defined from surface concentration in the **Label** text field.

Load variable definitions from a text file.

- **3** Locate the **Geometric Entity Selection** section. From the **Geometric entity level** list, choose **Domain**.
- **4** Select Domain 4 only.
- **5** Locate the **Variables** section. Click *b* Load from File.

6 Browse to the model's Application Libraries folder and double-click the file porous_reactor_variables.txt.

TRANSPORT OF DILUTED SPECIES IN POROUS CATALYSTS (TDS)

Initial Values 1

- I In the Model Builder window, under Component 2 (comp2)> Transport of Diluted Species in Porous Catalysts (tds) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the cH2 text field, type 0.
- **4** In the cO2 text field, type 0.

Add necessary features to the Transport of Diluted Species interface.

Transport Properties 1

- I In the Physics toolbar, click 🔚 Domains and choose Transport Properties.
- **2** Select Domains 2 and 5 only.
- 3 In the Settings window for Transport Properties, locate the Diffusion section.
- **4** From the **Source** list, choose **Chemistry**.
- 5 From the D_{cH2} list, choose Diffusion coefficient, H2 in N2 (solvent) (chem).
- 6 From the D_{cH2O} list, choose Diffusion coefficient , H2O in N2 (solvent) (chem).
- 7 From the D_{cO2} list, choose Diffusion coefficient, O2 in N2 (solvent) (chem).

Symmetry I

- I In the Physics toolbar, click 🔚 Boundaries and choose Symmetry.
- 2 In the Settings window for Symmetry, locate the Boundary Selection section.
- 3 From the Selection list, choose Symmetry plane.

Inflow I

- I In the Physics toolbar, click 📄 Boundaries and choose Inflow.
- 2 In the Settings window for Inflow, locate the Boundary Selection section.
- **3** From the Selection list, choose Inlet species **02**.
- **4** Locate the **Concentration** section. In the $c_{0,cO2}$ text field, type c002_inflow.

Inflow 2

- I In the Physics toolbar, click 📄 Boundaries and choose Inflow.
- 2 In the Settings window for Inflow, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Inlet species H2**.

4 Locate the **Concentration** section. In the $c_{0,cH2}$ text field, type cOH2_inflow.

Outflow I

- I In the Physics toolbar, click 🔚 Boundaries and choose Outflow.
- 2 In the Settings window for Outflow, locate the Boundary Selection section.
- 3 From the Selection list, choose Outlet.

BRINKMAN EQUATIONS (BR)

- I In the Model Builder window, under Component 2 (comp2) click Brinkman Equations (br).
- 2 In the Settings window for Brinkman Equations, locate the Domain Selection section.
- 3 From the Selection list, choose Free and Porous Media Domains.
- **4** Locate the **Physical Model** section. Clear the **Neglect inertial term (Stokes flow)** check box.
- 5 Click to expand the **Discretization** section. From the **Discretization of fluids** list, choose **PI+PI**.

Fluid Properties 1

- I In the Physics toolbar, click ⊨ Domains and choose Fluid Properties.
- **2** Select Domains 2 and 5 only.

Inlet 1

- I In the Physics toolbar, click 📄 Boundaries and choose Inlet.
- 2 In the Settings window for Inlet, locate the Boundary Selection section.
- **3** From the Selection list, choose Inlet species **02**.
- 4 Locate the Boundary Condition section. From the list, choose Fully developed flow.
- 5 Locate the Fully Developed Flow section. In the U_{av} text field, type v_inlet.

Inlet 2

- I In the Physics toolbar, click 🔚 Boundaries and choose Inlet.
- 2 In the Settings window for Inlet, locate the Boundary Selection section.
- **3** From the Selection list, choose Inlet species H2.
- 4 Locate the Boundary Condition section. From the list, choose Fully developed flow.
- **5** Locate the **Fully Developed Flow** section. In the U_{av} text field, type v_inlet.

Outlet I

- I In the Physics toolbar, click 📄 Boundaries and choose Outlet.
- 2 In the Settings window for Outlet, locate the Boundary Selection section.

3 From the **Selection** list, choose **Outlet**.

Symmetry 1

- I In the Physics toolbar, click 🔚 Boundaries and choose Symmetry.
- 2 In the Settings window for Symmetry, locate the Boundary Selection section.
- 3 From the Selection list, choose Symmetry plane.

MESH I

Size I

- I In the Model Builder window, under Component 2 (comp2) right-click Mesh I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click the i Zoom Extents button in the Graphics toolbar.
- **5** Select Domain 5 only.
- 6 Locate the Element Size section. From the Calibrate for list, choose Fluid dynamics.
- 7 From the Predefined list, choose Coarser.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Calibrate for list, choose Fluid dynamics.
- 4 From the **Predefined** list, choose **Coarse**.

Size 2

- I In the Model Builder window, right-click Mesh I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 6,9,10,14,20,23 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size section.
- 8 From the Calibrate for list, choose Fluid dynamics.
- 9 From the Predefined list, choose Fine.

Free Triangular 1

- I In the Mesh toolbar, click \bigwedge Boundary and choose Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Boundary Selection section.
- 3 From the Selection list, choose First Free-Porous Interface.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Calibrate for list, choose Fluid dynamics.
- 4 From the **Predefined** list, choose Fine.

Size 2

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Edge.
- 4 Click **Paste Selection**.
- 5 In the Paste Selection dialog box, type 31, 32 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size section.
- 8 From the Calibrate for list, choose Fluid dynamics.
- 9 Click the **Custom** button.
- **IO** Locate the **Element Size Parameters** section.
- II Select the Maximum element size check box. In the associated text field, type 0.5.

Swept 1

- I In the Mesh toolbar, click A Swept.
- 2 In the Settings window for Swept, locate the Domain Selection section.
- **3** From the **Geometric entity level** list, choose **Domain**.
- 4 From the Selection list, choose Catalyst Bed.

Distribution I

- I Right-click Swept I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 From the Distribution type list, choose Predefined.
- **4** In the **Number of elements** text field, type **30**.

Corner Refinement I

- I In the Mesh toolbar, click 🖄 More Attributes and choose Corner Refinement.
- 2 In the Settings window for Corner Refinement, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 2 and 4–6 only.
- 5 Locate the Boundary Selection section. Click 📄 Paste Selection.
- 6 In the Paste Selection dialog box, type 6,9,10,14,20,23 in the Selection text field.
- 7 Click OK.

Free Tetrahedral I

In the Mesh toolbar, click ؊ Free Tetrahedral.

Size 1

- I Right-click Free Tetrahedral I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Click **Paste Selection**.
- 5 In the Paste Selection dialog box, type 26 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size section.
- 8 From the Calibrate for list, choose Fluid dynamics.

Size 2

- I In the Model Builder window, right-click Free Tetrahedral I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- **3** From the Geometric entity level list, choose Domain.
- 4 Click **Paste Selection**.
- 5 In the Paste Selection dialog box, type 2,6 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size section.
- 8 From the Calibrate for list, choose Fluid dynamics.
- 9 Click the **Custom** button.
- 10 Locate the Element Size Parameters section.

II Select the Maximum element size check box. In the associated text field, type 0.9.

Boundary Layers 1

- I In the Mesh toolbar, click Boundary Layers.
- 2 In the Settings window for Boundary Layers, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Free Flow Domains.
- 5 Click to expand the Corner Settings section. From the Handling of sharp edges list, choose Trimming.

Boundary Layer Properties

- I In the Model Builder window, click Boundary Layer Properties.
- **2** In the **Settings** window for **Boundary Layer Properties**, locate the **Boundary Selection** section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 6,9,10,14,18,21,23 in the Selection text field.
- 5 Click OK.
- 6 In the Settings window for Boundary Layer Properties, locate the Layers section.
- 7 In the Number of layers text field, type 2.
- 8 In the Stretching factor text field, type 1.75.
- 9 In the Thickness adjustment factor text field, type 4.5.

Boundary Layers 2

- I In the Mesh toolbar, click Boundary Layers.
- 2 In the Settings window for Boundary Layers, locate the Geometric Entity Selection section.
- **3** From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Catalyst Bed.
- 5 Locate the Corner Settings section. From the Handling of sharp edges list, choose Trimming.
- **6** Click to expand the **Transition** section. Clear the **Smooth transition to interior mesh** check box.

Boundary Layer Properties

- I In the Model Builder window, click Boundary Layer Properties.
- **2** In the **Settings** window for **Boundary Layer Properties**, locate the **Boundary Selection** section.
- **3** Click **Paste Selection**.

- 4 In the Paste Selection dialog box, type 18,20,21 in the Selection text field.
- 5 Click OK.
- 6 In the Settings window for Boundary Layer Properties, locate the Layers section.
- 7 In the Number of layers text field, type 4.
- 8 In the Stretching factor text field, type 1.25.
- 9 In the Thickness adjustment factor text field, type 2.75.
- IO Click 📗 Build All.

STUDY 2

Stationary

I In the Study toolbar, click 🔁 Study Steps and choose Stationary>Stationary.

There are two study steps in **Study 2**. The first **Stationary** study step solves for the pressure and velocity (from the **Brinkman Equations**) which is supposed to reach stationary state quickly and is insignificantly affected by the concentration field. The second **Time Dependent** study step solves for the molar concentrations (from the **Transport of Diluted Species** interface) with the velocity field from the first study step.

- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- **3** In the table, enter the following settings:

Physics interface	Solve for	Equation form
Reaction Engineering (re)		Automatic (Time dependent)
Chemistry I (chem)	\checkmark	Automatic (Stationary)
Transport of Diluted Species in Porous Catalysts (tds)		Automatic (Time dependent)
Brinkman Equations (br)	\checkmark	Automatic (Stationary)

4 In the table, enter the following settings:

Multiphysics couplings	Solve for	Equation form
Reacting Flow, Diluted Species I (rfd1)		Automatic (Time dependent)

5 Right-click Study 2>Step 2: Stationary and choose Move Up.

Step 2: Time Dependent

- I In the Model Builder window, click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.

- 3 In the **Output times** text field, type range(0,0.05,1).
- **4** Locate the **Physics and Variables Selection** section. In the table, enter the following settings:

Physics interface	Solve for	Equation form
Reaction Engineering (re)		Automatic (Time dependent)
Chemistry I (chem)	\checkmark	Automatic (Time dependent)
Transport of Diluted Species in Porous Catalysts (tds)	\checkmark	Automatic (Time dependent)
Brinkman Equations (br)		Automatic (Stationary)

Solution 2 (sol2)

In the Study toolbar, click **Show Default Solver**.

Step 2: Time Dependent

- I In the Model Builder window, under Study 2 click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, click to expand the Values of Dependent Variables section.
- **3** Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.

Solution 2 (sol2)

I In the Model Builder window, expand the Solution 2 (sol2) node.

Set the scaling factor to 1 for the bulk species dependent variables.

- In the Model Builder window, expand the Study 2>Solver Configurations>
 Solution 2 (sol2)>Dependent Variables 2 node, then click Concentration (comp2.cH2).
- 3 In the Settings window for Field, locate the Scaling section.
- 4 From the Method list, choose Manual.
- 5 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Concentration (comp2.cH20).
- 6 In the Settings window for Field, locate the Scaling section.
- 7 From the Method list, choose Manual.
- 8 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Concentration (comp2.c02).
- 9 In the Settings window for Field, locate the Scaling section.

IO From the **Method** list, choose **Manual**.

Set the scaling factor to **Initial value based** for the adsorbed species dependent variables.

- II In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Adsorbed concentration (comp2.tds.cads_cH2).
- 12 In the Settings window for Field, locate the Scaling section.
- **I3** From the **Method** list, choose **Manual**.
- **I4** In the **Scale** text field, type cH2_ads_scale.
- I5 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Adsorbed concentration (comp2.tds.cads_cH20).
- 16 In the Settings window for Field, locate the Scaling section.
- 17 From the Method list, choose Manual.
- **I8** In the **Scale** text field, type cH20_ads_scale.
- 19 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Adsorbed concentration (comp2.tds.cads_c02).
- **20** In the Settings window for Field, locate the Scaling section.
- 21 From the Method list, choose Manual.
- **22** In the **Scale** text field, type c02_ads_scale.

Set the scaling factors for all surface species dependent variables.

- 23 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Surface concentration (comp2.tds.csurf_H).
- 24 In the Settings window for Field, locate the Scaling section.
- **25** From the **Method** list, choose **Manual**.
- **26** In the **Scale** text field, type cH_surf_scale.
- 27 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)>
 Dependent Variables 2 click Surface concentration (comp2.tds.csurf_0).
- 28 In the Settings window for Field, locate the Scaling section.
- **29** From the **Method** list, choose **Manual**.
- **30** In the **Scale** text field, type c0_surf_scale.
- 31 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Surface concentration (comp2.tds.csurf_OH).
- 32 In the Settings window for Field, locate the Scaling section.
- **33** From the **Method** list, choose **Manual**.

- **34** In the **Scale** text field, type cOH_surf_scale.
- 35 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Dependent Variables 2 click Surface concentration (comp2.tds.csurf_Rh).
- 36 In the Settings window for Field, locate the Scaling section.
- 37 From the Method list, choose Manual.
- **38** In the **Scale** text field, type cRh_surf_scale.
- 39 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2) click Time-Dependent Solver I.
- **40** In the **Settings** window for **Time-Dependent Solver**, click to expand the **Absolute Tolerance** section.
- **4** In the **Tolerance factor** text field, type 0.05.
- **42** Click to expand the **Time Stepping** section. Find the **Algebraic variable settings** subsection. From the **Error estimation** list, choose **Exclude algebraic**.
- 43 In the Model Builder window, expand the Solution 2 (sol2) node.
- **44** In the Model Builder window, expand the Study 2>Solver Configurations> Solution 2 (sol2)>Time-Dependent Solver I node.
- **45** Right-click **Study 2>Solver Configurations>Solution 2 (sol2)>Time-Dependent Solver I** and choose **Segregated**.
- 46 In the Settings window for Segregated, locate the General section.
- **47** From the **Stabilization and acceleration** list, choose **Anderson acceleration**.
- **48** In the **Dimension of iteration space** text field, type **5**.
- **49** In the **Mixing parameter** text field, type 0.9.
- **50** In the **Iteration delay** text field, type **1**.
- 51 Right-click Study 2>Solver Configurations>Solution 2 (sol2)>Time-Dependent Solver I> Segregated I and choose Segregated Step.
- **52** In the **Settings** window for **Segregated Step**, type **Concentrations** in the **Label** text field.
- **3** Locate the **General** section. Under **Variables**, click + **Add**.
- 54 In the Add dialog box, in the Variables list, choose Concentration (comp2.cH2), Concentration (comp2.cH20), and Concentration (comp2.cO2).
- 55 Click OK.
- **56** In the **Settings** window for **Segregated Step**, click to expand the **Method and Termination** section.
- **57** From the **Jacobian update** list, choose **Once per time step**.

- 58 Right-click Segregated I and choose Segregated Step.
- **59** In the **Settings** window for **Segregated Step**, type **Surface concentrations** in the **Label** text field.
- 60 Locate the General section. Under Variables, click + Add.
- 61 In the Add dialog box, in the Variables list, choose
 Adsorbed concentration (comp2.tds.cads_cH2),
 Adsorbed concentration (comp2.tds.cads_cH20),
 Adsorbed concentration (comp2.tds.cads_cO2), Surface concentration (comp2.tds.csurf_H),
 Surface concentration (comp2.tds.csurf_0), Surface concentration (comp2.tds.csurf_OH),
 and Surface concentration (comp2.tds.csurf_Rh).
- 62 Click OK.
- 63 In the Settings window for Segregated Step, locate the Method and Termination section.
- 64 From the Jacobian update list, choose Once per time step.
- 65 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Time-Dependent Solver 1>Segregated 1 right-click Segregated Step and choose Delete. Add a Lower Limit to the surface species dependent variables.
- 66 Right-click Study 2>Solver Configurations>Solution 2 (sol2)>Time-Dependent Solver I> Segregated I and choose Lower Limit.
- 67 In the Settings window for Lower Limit, locate the Lower Limit section.
- 68 In the Lower limits (field variables) text field, type comp2.tds.csurf_Rh 1e-16 comp2.tds.csurf_H 1e-16 comp2.tds.csurf_O 1e-16 comp2.tds.csurf_OH 1e-16.
- **69** In the **Study** toolbar, click **= Compute**.

RESULTS

Cut Plane 1

- I In the **Results** toolbar, click **Cut Plane**.
- 2 In the Settings window for Cut Plane, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution Store I (sol3).
- 4 Locate the Plane Data section. From the Plane list, choose xy-planes.
- 5 In the z-coordinate text field, type -0.5.

Cut Line 3D 1

I In the **Results** toolbar, click Cut Line 3D.

- 2 In the Settings window for Cut Line 3D, locate the Line Data section.
- 3 In row Point I, set x to 3*do_reac.
- 4 In row Point 2, set x to 3.7*do_reac.

Velocity (br)

- I In the Model Builder window, under Results click Velocity (br).
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- **3** Select the **Show units** check box.

The following steps reproduce, in turn, the plots shown in Figure 2, Figure 3, Figure 4, and Figure 5.

Slice

- I In the Model Builder window, expand the Velocity (br) node, then click Slice.
- 2 In the Settings window for Slice, locate the Plane Data section.
- 3 From the Plane list, choose yz-planes.
- 4 In the Planes text field, type 8.
- 5 Click to expand the Coloring and Style section. Select the Color legend check box.
- 6 Click Change Color Table.
- 7 In the Color Table dialog box, select Rainbow>Spectrum in the tree.
- 8 Click OK.

Velocity, Surface

- I In the Model Builder window, under Results click Velocity (br).
- 2 In the Settings window for 3D Plot Group, type Velocity, Surface in the Label text field.

Surface 1

- I Right-click Velocity, Surface and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the **Expression** text field, type br.U*1[cm]/br.nu.

Selection I

- I Right-click Surface I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the Selection list, choose Symmetry plane.

Transparency 1

- I In the Model Builder window, right-click Surface I and choose Transparency.
- 2 In the Settings window for Transparency, locate the Transparency section.
- **3** Set the **Transparency** value to **0**.

Arrow Surface 1

- I In the Model Builder window, right-click Velocity, Surface and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Data section.
- 3 From the Dataset list, choose Cut Plane I.
- **4** Locate the **Expression** section. In the **x-component** text field, type u.
- **5** In the **y-component** text field, type v.
- 6 In the **z-component** text field, type w.
- 7 Locate the Arrow Positioning section. In the Number of arrows text field, type 300.
- 8 Locate the Coloring and Style section. From the Color list, choose Gray.
- 9 In the Velocity, Surface toolbar, click 🗿 Plot.
- **10** Click the 4 **Zoom Extents** button in the **Graphics** toolbar.

Pressure (br)

- I In the Model Builder window, under Results click Pressure (br).
- 2 In the Pressure (br) toolbar, click **O** Plot.
- **3** Click the \longleftrightarrow **Zoom Extents** button in the **Graphics** toolbar.

Concentration, H2, Surface (tds)

- I In the Model Builder window, click Concentration, H2, Surface (tds).
- 2 In the Settings window for 3D Plot Group, click to expand the Title section.
- **3** From the **Title type** list, choose **Automatic**.
- 4 Locate the Plot Settings section. Clear the Plot dataset edges check box.

Surface: pipe

- I In the Model Builder window, expand the Concentration, H2, Surface (tds) node, then click Surface I.
- 2 In the Settings window for Surface, type Surface: pipe in the Label text field.
- **3** Locate the **Expression** section. In the **Expression** text field, type 1.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.

6 From the Color list, choose Gray.

Selection 1

- I Right-click Surface: pipe and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Outer Bnds.

Surface: Catalyst

- I In the Model Builder window, right-click Concentration, H2, Surface (tds) and choose Surface.
- 2 In the Settings window for Surface, type Surface: Catalyst in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type 1.
- 4 Locate the Title section. From the Title type list, choose None.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Gray.

Selection I

- I Right-click Surface: Catalyst and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the **Selection** list, choose **Bed Bnds**.

Material Appearance 1

- I In the Model Builder window, right-click Surface: Catalyst and choose Material Appearance.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Appearance list, choose Custom.
- 4 From the Material type list, choose Wood.

Streamline 1

- I In the Model Builder window, right-click Concentration, H2, Surface (tds) and choose Streamline.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.
- **3** In the **Number** text field, type 10.
- 4 Locate the Selection section. Click 📄 Paste Selection.
- 5 In the Paste Selection dialog box, type 18 in the Selection text field.
- 6 Click OK.

- 7 In the Settings window for Streamline, locate the Coloring and Style section.
- 8 Find the Point style subsection. From the Type list, choose Arrow.
- 9 From the Color list, choose Black.

Concentration, cH2, Isosurface

- I Right-click Concentration, H2, Surface (tds) and choose Isosurface.
- 2 In the Settings window for Isosurface, type Concentration, cH2, Isosurface in the Label text field.
- 3 Locate the Levels section. From the Entry method list, choose Levels.
- 4 In the Levels text field, type range(0.1,0.1,2).

Transparency I

- I Right-click Concentration, cH2, Isosurface and choose Transparency.
- 2 In the Concentration, H2, Surface (tds) toolbar, click 🗿 Plot.
- **3** Click the \longleftrightarrow **Zoom Extents** button in the **Graphics** toolbar.

Concentration, O2, Surface (tds)

- I In the Model Builder window, under Results click Concentration, 02, Surface (tds).
- 2 In the Settings window for 3D Plot Group, click to expand the Title section.
- 3 Click to expand the Title section. From the Title type list, choose Automatic.
- 4 Locate the Plot Settings section. Clear the Plot dataset edges check box.

Surface: Pipe

- I In the Model Builder window, expand the Concentration, 02, Surface (tds) node, then click Surface I.
- 2 In the Settings window for Surface, type Surface: Pipe in the Label text field.
- **3** Locate the **Expression** section. In the **Expression** text field, type 1.
- 4 Locate the Title section. From the Title type list, choose None.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Gray.

Selection 1

- I Right-click Surface: Pipe and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the Selection list, choose Outer Bnds.

Surface: Catalyst

- I In the Model Builder window, right-click Concentration, 02, Surface (tds) and choose Surface.
- 2 In the Settings window for Surface, type Surface: Catalyst in the Label text field.
- **3** Locate the **Expression** section. In the **Expression** text field, type **1**.
- 4 Locate the Title section. From the Title type list, choose None.

Selection I

- I Right-click Surface: Catalyst and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the **Selection** list, choose **Bed Bnds**.

Material Appearance 1

- I In the Model Builder window, right-click Surface: Catalyst and choose Material Appearance.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Appearance list, choose Custom.
- 4 From the Material type list, choose Wood.

Streamline 1

- I In the Model Builder window, right-click Concentration, 02, Surface (tds) and choose Streamline.
- 2 In the Settings window for Streamline, locate the Expression section.
- 3 In the x-component text field, type tds.tflux_c02x.
- **4** In the **y-component** text field, type tds.tflux_c02y.
- 5 In the z-component text field, type tds.tflux_c02z.
- 6 Locate the Streamline Positioning section. In the Number text field, type 10.
- 7 Locate the Selection section. Click Paste Selection.
- 8 In the Paste Selection dialog box, type 18 in the Selection text field.
- 9 Click OK.
- 10 In the Settings window for Streamline, locate the Coloring and Style section.
- II Find the Point style subsection. From the Type list, choose Arrow.
- 12 From the Color list, choose Black.

Concentration, cO2, Isosurface

I Right-click Concentration, 02, Surface (tds) and choose Isosurface.

- 2 In the Settings window for Isosurface, locate the Expression section.
- **3** In the **Expression** text field, type c02.
- **4** In the **Label** text field, type Concentration, c02, Isosurface.
- 5 Locate the Levels section. From the Entry method list, choose Levels.
- 6 In the Levels text field, type range (0.5, 0.025, 0.9).

Transparency I

- I Right-click Concentration, c02, Isosurface and choose Transparency.
- 2 In the Concentration, 02, Surface (tds) toolbar, click **O** Plot.
- **3** Click the 4 **Zoom Extents** button in the **Graphics** toolbar.

Plot the bulk species concentrations (mol/m^3) in the porous domain.

Porous domain: bulk species

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Porous domain: bulk species in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Cut Line 3D I.
- 4 From the Time selection list, choose From list.
- 5 In the Times (s) list, select 1.

Line Graph 1

- I Right-click Porous domain: bulk species and choose Line Graph.
- 2 In the Settings window for Line Graph, click to expand the Title section.
- **3** From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Molar concentration, bulk.
- 5 Click to expand the Legends section. Select the Show legends check box.
- 6 Find the Include subsection. Clear the Solution check box.
- **7** Select the **Expression** check box.

Line Graph 2

- I In the Model Builder window, right-click Porous domain: bulk species and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type c02.
- **4** Locate the **Title** section. From the **Title type** list, choose **None**.

- 5 Locate the Legends section. Select the Show legends check box.
- 6 Find the Include subsection. Clear the Solution check box.
- **7** Select the **Expression** check box.

Line Graph 3

- I Right-click Porous domain: bulk species and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cH20.
- **4** Locate the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Legends section. Select the Show legends check box.
- 6 Find the Include subsection. Clear the Solution check box.
- **7** Select the **Expression** check box.
- 8 In the Porous domain: bulk species toolbar, click **OM** Plot.
- 9 Click the **Zoom Extents** button in the **Graphics** toolbar.

Plot the species concentrations (mol/m³) being converted from surface species in the porous domain.

Porous domain: surface species

- I Right-click Porous domain: bulk species and choose Duplicate.
- 2 In the Model Builder window, click Porous domain: bulk species I.
- **3** In the **Settings** window for **ID Plot Group**, type Porous domain: surface species in the **Label** text field.

Line Graph 1

- I In the Model Builder window, click Line Graph I.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cs_Rh.
- 4 Locate the Title section. In the Title text area, type Molar concentration, surface.

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type cs_H.

Line Graph 3

I In the Model Builder window, click Line Graph 3.

- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cs_0.

Line Graph 4

- I Right-click Results>Porous domain: surface species>Line Graph 3 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cs_OH.
- **4** In the **Porous domain: surface species** toolbar, click **O Plot**.
- **5** Click the **F Zoom Extents** button in the **Graphics** toolbar.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Plot the species concentrations (mol/m³) being converted from adsorbed species in the porous domain.

Porous domain: adsorbed species

- I In the Model Builder window, right-click Porous domain: bulk species and choose Duplicate.
- 2 In the Model Builder window, click Porous domain: bulk species I.
- **3** In the **Settings** window for **ID Plot Group**, type Porous domain: adsorbed species in the **Label** text field.

Line Graph 1

- I In the Model Builder window, click Line Graph I.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cads_cH2.
- 4 Locate the Title section. In the Title text area, type Molar concentration, adsorbed.

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cads_c02.

Line Graph 3

- I In the Model Builder window, click Line Graph 3.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type cads_cH20.
- **4** In the **Porous domain: adsorbed species** toolbar, click **OM Plot**.

- **5** Click the **F Zoom Extents** button in the **Graphics** toolbar.
- 6 Click the 4 Zoom Extents button in the Graphics toolbar.

Porous domain: all species

- I In the Model Builder window, right-click Porous domain: bulk species and choose Duplicate.
- 2 In the Model Builder window, click Porous domain: bulk species I.
- 3 In the Settings window for ID Plot Group, type Porous domain: all species in the Label text field.

Bulk: cH2

- I In the Model Builder window, under Results>Porous domain: all species click Line Graph I.
- 2 In the Settings window for Line Graph, type Bulk: cH2 in the Label text field.
- 3 Locate the Title section. In the Title text area, type Molar concentration.

Bulk: cO2

- I In the Model Builder window, under Results>Porous domain: all species click Line Graph 2.
- 2 In the Settings window for Line Graph, type Bulk: c02 in the Label text field.

Bulk: cH2O

- I In the Model Builder window, under Results>Porous domain: all species click Line Graph 3.
- 2 In the Settings window for Line Graph, type Bulk: cH20 in the Label text field.

Bulk: cH2O, Bulk: cO2

- I In the Model Builder window, under Results>Porous domain: all species, Ctrl-click to select Bulk: cO2 and Bulk: cH20.
- 2 Right-click and choose **Duplicate**.

Surface: cs_Rh

- I In the Settings window for Line Graph, type Surface: cs_Rh in the Label text field.
- 2 Locate the y-Axis Data section. In the Expression text field, type cs_Rh.

Surface: cs_H

- I In the Model Builder window, under Results>Porous domain: all species click Bulk: cH20 I.
- 2 In the Settings window for Line Graph, type Surface: cs_H in the Label text field.
- 3 Locate the y-Axis Data section. In the Expression text field, type cs_H.

Surface: cs_H, Surface: cs_Rh

- I In the Model Builder window, under Results>Porous domain: all species, Ctrl-click to select Surface: cs_Rh and Surface: cs_H.
- 2 Right-click and choose **Duplicate**.

Surface: cs_O

- I In the Settings window for Line Graph, type Surface: cs_0 in the Label text field.
- 2 Locate the y-Axis Data section. In the Expression text field, type cs_0.

Surface: cs_OH

- I In the Model Builder window, under Results>Porous domain: all species click Surface: cs_H I.
- 2 In the Settings window for Line Graph, type Surface: cs_OH in the Label text field.
- 3 Locate the y-Axis Data section. In the Expression text field, type cs_0H.

Adsorbed: cads_cH2

- I Right-click Surface: cs_OH and choose Duplicate.
- 2 In the Settings window for Line Graph, type Adsorbed: cads_cH2 in the Label text field.
- 3 Locate the y-Axis Data section. In the Expression text field, type cads_CH2.

Adsorbed: cads_cO2

- I Right-click Adsorbed: cads_cH2 and choose Duplicate.
- 2 In the Settings window for Line Graph, type Adsorbed: cads_c02 in the Label text field.
- 3 Locate the y-Axis Data section. In the Expression text field, type cads_c02.

Adsorbed: cads_cH2O

- I Right-click Adsorbed: cads_c02 and choose Duplicate.
- 2 In the Settings window for Line Graph, type Adsorbed: cads_cH20 in the Label text field.
- 3 Locate the y-Axis Data section. In the Expression text field, type cads_cH20.
- **4** In the **Porous domain: all species** toolbar, click **O Plot**.
- **5** Click the **F Zoom Extents** button in the **Graphics** toolbar.

50 | POROUS CATALYTIC REACTOR WITH INJECTION NEEDLE