

Degradation of DNA in Plasma

Gene therapy is one biotechnology example of a clinical application where it is possible to produce proteins in vivo, using the body's own mechanisms for protein production. Major issues in gene delivery involve the transport of plasmid DNA (pDNA) to target sites and the conversion between different forms of pDNA.

This example uses the Parameter Estimation feature with the Reaction Engineering interface to find the rate constants of three consecutive reactions involved in a DNA degradation process.

Note: This application requires the Optimization Module.

Model Description

pDNA can be used to express proteins in the human body, proteins that can have therapeutic effects. pDNA exists in three forms — a supercoiled form (SC), an opencircular form (OC), and a linear form (L) — each with varying protein-expression rates. These pDNA-forms interconvert and degrade with time, which means a patient's therapy benefits from knowledge about the distribution of pDNA-forms over time.

The protein expression rate for the SC form is greater than the one for the OC form, which in turn is significantly greater than that for the L form. The kinetic model in this study assumes that the pDNA-forms interconvert and decompose according to the mechanism in Figure 1.

SC
$$\frac{k_1}{}$$
 OC $\frac{k_2}{}$ L $\frac{k_3}{}$ F

Figure 1: Kinetic model of plasmid DNA interconversion and decomposition. Supercoiled pDNA (SC) converts to an open-circular form (OC), which in turn converts to a linear form (L). The linear pDNA decomposes to form linear fragments (F).

This example proposes a set of irreversible reactions in which an SC-form pDNA converts to the OC form and then to the L form. Then the L-form decomposes into a number of linear fragments, collectively denoted as F.

The three irreversible reactions in Figure 1 translate into these reaction rate expressions:

$$r_1 = k_1 c_{\rm SC}$$

$$r_2 = k_2 c_{\text{OC}}$$

$$r_3 = k_3 c_{\rm L}$$

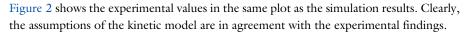
The rate constants k_1 through k_3 are found by parameter estimation, making use of the experimental data summarized in the table:

TABLE I: EXPERIMENTAL CONCENTRATION DATA.

Time (s)	$c_{ m SC}$ (ng/ μ l)	$c_{ m OC}$ (ng/ μ l)	$c_{ m L}$ (ng/ μ l)
5	9.3	0.5	0
60	5.0	4.1	0.1
120	3.5	6.5	0.3
180	1.1	7.0	0.5
300	0.5	8.1	0.8
420	0.1	8.0	1.2
600	0	7.8	1.7
900	0	7.1	2.4
1200	0	6.3	2.5
1800	0	4.5	2.6
2400	0	3.0	2.0
3000	0	2.1	1.8
3600	0	1.5	1.2

Results and Discussion

The following rate constants are calculated from the experimental data and proposed reaction mechanism: $k_1 = 9.6 \cdot 10^{-3} (1/s)$, $k_2 = 4.8 \cdot 10^{-4} (1/s)$, and $k_3 = 9.6 \cdot 10^{-4} (1/s)$. In addition, the initial concentration of the SC species is estimated to 9.7 ng/µl.



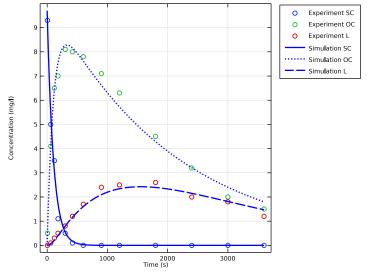


Figure 2: A plot resulting from reading in experimental data and comparing it to simulation

The estimated rate constants show that the supercoiled pDNA rapidly transforms into the open-circular form with a half-life of approximately 1.2 minutes:

$$t_{1/2} = \frac{\ln 2}{k}$$

The open-circular and linear pDNA decay with half-lives of 24.1 and 12.0 minutes, respectively. As mentioned, the supercoiled pDNA has the highest protein-expression rate of the three forms. However, because the SC form has a half-life of only 1.2 minutes, it is likely that it decomposes during transport to the therapeutic target sites. These findings imply that you have to find ways to hinder the relatively fast decay of SC.

Reference

1. B.E. Houk, G. Hochhaus, and J.A. Hughes, "Kinetic modeling of plasmid DNA degradation in rat plasma," AAPS Pharmsci, vol. 1, no. 3, pp. 15-20, 1999.

Application Library path: Chemical Reaction Engineering Module/

Ideal_Tank_Reactors/dna_degradation

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 0D.
- 2 In the Select Physics tree, select Chemical Species Transport>Reaction Engineering (re).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click M Done.

GLOBAL DEFINITIONS

Read model parameters from a text file.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file dna_degradation_parameters.txt.

Start by entering the reaction properties in the **Reaction Engineering** interface.

REACTION ENGINEERING (RE)

- I In the Model Builder window, under Component I (compl) click Reaction Engineering (re).
- 2 In the Settings window for Reaction Engineering, click to expand the Mixture Properties section.
- 3 From the Phase list, choose Liquid.

Reaction I

- I In the Reaction Engineering toolbar, click A Reaction.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- 3 In the Formula text field, type SC=>0C.
- **4** Locate the **Rate Constants** section. In the k^{f} text field, type k1.

Species: SC

- I In the Model Builder window, click Species: SC.
- 2 In the Settings window for Species, locate the Chemical Formula section.
- **3** Clear the **Enable formula** check box.

Species: OC

- I In the Model Builder window, click Species: OC.
- 2 In the Settings window for Species, locate the Chemical Formula section.
- 3 Clear the **Enable formula** check box.

Reaction 2

- I In the Reaction Engineering toolbar, click _ Reaction.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- **3** In the **Formula** text field, type OC=>L.
- 4 Locate the Rate Constants section. In the k^{f} text field, type k2.

Reaction 3

- I In the Reaction Engineering toolbar, click \angle Reaction.
- 2 In the Settings window for Reaction, locate the Reaction Formula section.
- **3** In the **Formula** text field, type L=>F.
- **4** Locate the **Rate Constants** section. In the k^{f} text field, type k3.

Species: F

- I In the Model Builder window, click Species: F.
- 2 In the Settings window for Species, locate the Chemical Formula section.
- **3** Clear the **Enable formula** check box.

Species 1

The species are dissolved in water. Add water as a solvent.

- I In the Reaction Engineering toolbar, click 🟃 Species.
- 2 In the Settings window for Species, locate the Name section.

- **3** In the text field, type H20.
- 4 Locate the Type section. From the list, choose Solvent.

Parameter Estimation 1

Choose a Parameter Estimation feature to optimize the three reaction constants in the reactions entered in the interface.

- I In the Reaction Engineering toolbar, click Parameter Estimation. Select the parameters to be estimated and provide an initial guess. The parameter c SC init will be used to estimate the initial concentration of the species SC. Note that the experimental data have compositions in ng/µl unit and only first order reaction constants are optimized. Therefore, the same unit will apply also for the model compositions.
- 2 In the Settings window for Parameter Estimation, locate the Estimation Parameters section.
- 3 In the Parameter table, enter the following settings:

Parameter	Initial value	Scale	Lower bound	Upper bound
kl	1e-3	1e-3		

- 4 Click + Add.
- 5 In the **Parameter** table, enter the following settings:

Parameter	Initial value	Scale	Lower bound	Upper bound
k2	1e-3	1e-3		

- 6 Click + Add.
- 7 In the Parameter table, enter the following settings:

Parameter	Initial value	Scale	Lower bound	Upper bound
k3	1e-3	1e-3		

8 Click + Add.

9 In the **Parameter** table, enter the following settings:

Parameter	Initial value	Scale	Lower bound	Upper bound
c_SC_init	10	10		

Prescribing scales for the estimation parameters increases the efficiency of the optimization procedure. A good starting point is to use scales of the same order as the initial values.

Experiment I

Select an **Experiment** feature to import experimental data to which the simulation will be optimized.

- I In the Reaction Engineering toolbar, click Attributes and choose Experiment.
- 2 In the Settings window for Experiment, locate the Experimental Data section.
- 3 Click **Browse**.
- 4 Browse to the model's Application Libraries folder and double-click the file dna_degradation_experiment1.csv.
- 5 Click | Import.
- **6** In the table, enter the following settings:

Data column	Use	Model variables	Unit	Weight
Time		t	1	1
Conc. SC	$\sqrt{}$	c_SC	1	1
Conc. OC	V	c_0C	1	1
Conc. L	V	c_L	1	1

Initial Values 1

Note that the unit ng/l should be used due to the unit of the imported data in the Parameter Estimation feature. For water, enter the value 1000 ng/µl.

- I In the Model Builder window, under Component I (compl)>Reaction Engineering (re) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Volumetric Species Initial Values section.

3 In the table, enter the following settings:

Species	Concentration (mol/m^3)
H2O	1000
SC	c_SC_init

Set all reaction rate constants to the same names chosen in the Parameter Estimation feature.

In the **Study** node, add an optimization step to finalize the optimization settings.

STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** In the **Output times** text field, type **0** 3600.

Obtimization

- I In the Study toolbar, click optimization and choose Optimization.
- 2 In the Settings window for Optimization, locate the Optimization Solver section.
- 3 From the Method list, choose Levenberg-Marquardt.
- 4 In the Optimality tolerance text field, type 1.0E-4.
- **5** Locate the **Output While Solving** section. Select the **Plot** check box.
- 6 In the Study toolbar, click **Compute**.

Follow these steps to create Figure 2. The experimental and simulation data should match.

RESULTS

Concentrations

- I In the Model Builder window, under Results click Experiment I Group.
- 2 In the Settings window for ID Plot Group, type Concentrations in the Label text field.
- **3** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section.
- 5 Select the x-axis label check box. In the associated text field, type Time (s).
- 6 Select the y-axis label check box. In the associated text field, type Concentration (mg/ 1).

7 Locate the Legend section. From the Layout list, choose Outside graph axis area.

Experimental Data

- I In the Model Builder window, expand the Concentrations node, then click Experiment | Data.
- 2 In the Settings window for Table Graph, type Experimental Data in the Label text field.
- 3 Click to expand the Legends section. From the Legends list, choose Manual.
- **4** In the table, enter the following settings:

Legends	
Experiment	SC
Experiment	ОС
Experiment	L

Simulation Data

- I In the Model Builder window, under Results>Concentrations click Global I.
- 2 In the Settings window for Global, type Simulation Data in the Label text field.
- 3 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c_SC - Concentration - mol/ m³.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c_OC - Concentration mol/m³.
- 5 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Reaction Engineering>re.c L - Concentration - mol/ m³.
- 6 Click to expand the Coloring and Style section. Find the Line style subsection. From the Line list, choose Cycle.
- 7 From the Width list, choose 2.
- **8** Click to expand the **Legends** section. Select the **Show legends** check box.
- 9 From the Legends list, choose Manual.
- **10** In the table, enter the following settings:

Legends		
Simulation	SC	

Legends	
Simulation	ОС
Simulation	L

II In the Concentrations toolbar, click Plot.

12 Click the **Zoom Extents** button in the **Graphics** toolbar.

Output the values of the estimated parameters to a table.

13 In the Results toolbar, click **= Evaluate** and choose **Evaluate** All.

Last plot group is not used and is therefore removed.

Concentration (re)

In the Model Builder window, under Results right-click Concentration (re) and choose Delete.