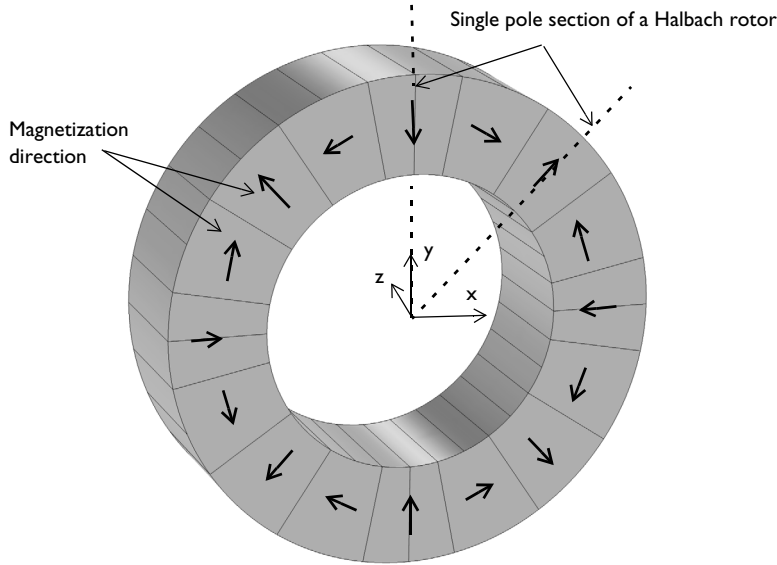


# Static Field Modeling of a Halbach Rotor

## Introduction

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This example presents the static-field modeling of an outward-flux-focusing magnetic rotor using permanent magnets, a magnetic rotor also known as a Halbach rotor. The use of permanent magnets in rotatory devices such as motors, generators, and magnetic gears is increasing due to their no-contact, frictionless operation. This model illustrates how to calculate the magnetic field of a 4-pole pair rotor in 3D by modeling only a single pole of the rotor using symmetry.



*Figure 1: Illustration of a 16-segments, 4-pole pair Halbach rotor. The symmetries of the problem allow restricting the model to a single pole of the rotor.*

## Model Definition

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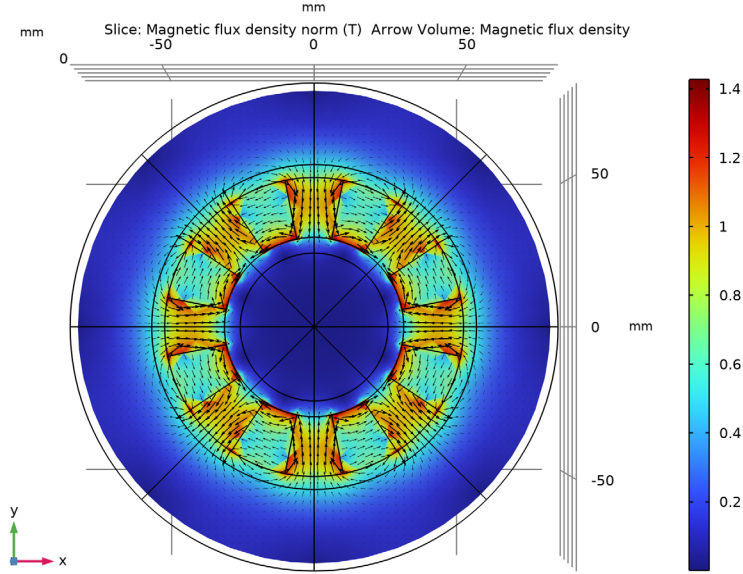
Set up the problem in a 3D modeling space. Due to symmetry, it is sufficient to model a single pole of the rotor. [Figure 1](#) shows a 3D view of the complete rotor with the magnetization direction of the magnets indicated. The black arrows show the radial and axial magnetization directions of the permanent magnets in the rotor. The permanent magnets are arranged in such a way that the magnetic flux density is minimized inside the rotor and maximized outside the rotor. The model consists of 16 permanent magnet pieces arranged to form a 4-pole pair rotor. The inner and outer rotor radii are 30 mm and 50 mm, respectively. The axial length of the rotor is 30 mm.

## Results and Discussion

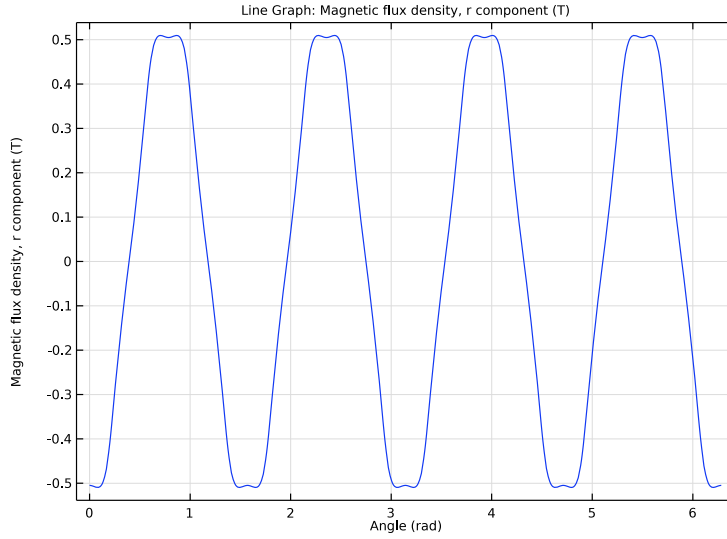
A steady-state study analysis is performed to calculate the magnetic fields of the Halbach rotor. The magnetic flux density is shown in [Figure 2](#).

[Figure 3](#) and [Figure 4](#) illustrate the variations of the radial and azimuthal magnetic flux density as functions of rotor angle. The magnetic flux density norm is evaluated outside the Halbach rotor at a radial distance of 55 mm from the center.

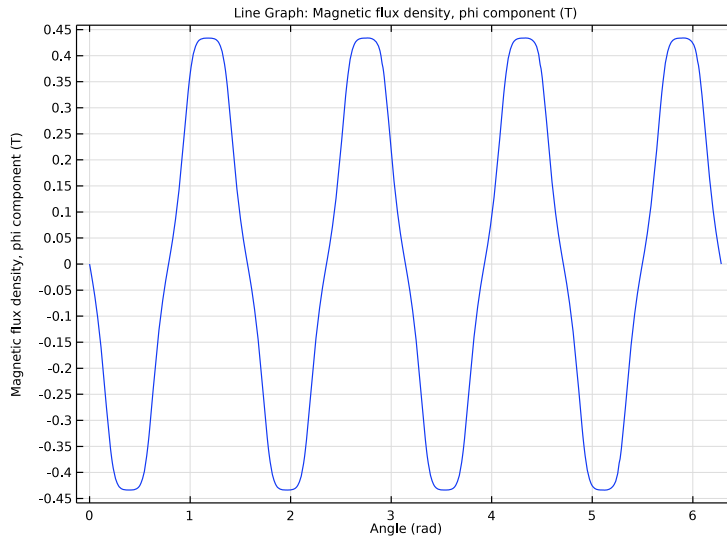
Finally, [Figure 5](#) and [Figure 6](#) show the polar plots of the magnetic flux density norm at radial distances from the rotor center of 55 mm and 25 mm, respectively.



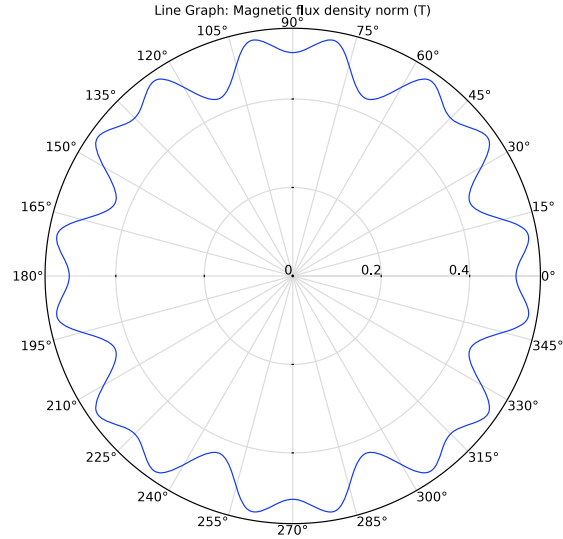
*Figure 2: Magnetic flux density norm at the cross section of the Halbach rotor (at  $z = 0$  mm).*



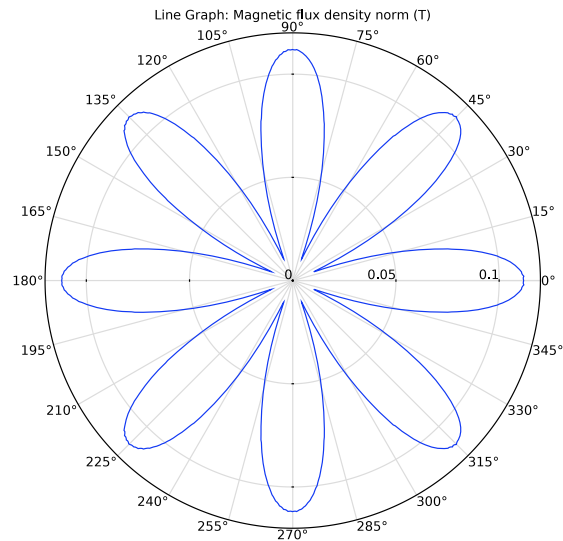
*Figure 3: The radial magnetic flux density as a function of rotor angle measured at a radial distance of 55 mm from the rotor center.*



*Figure 4: The azimuthal magnetic flux density as a function of rotor angle measured at a radial distance of 25 mm from the rotor center.*



*Figure 5: Polar plot of the magnetic flux density norm at a radial distance of 55 mm from the rotor center.*



*Figure 6: Polar plot of the magnetic flux density norm at a radial distance of 25 mm from the rotor center.*

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**Application Library path:** ACDC\_Module/Introductory\_Magnetostatics/  
static\_field\_halbach\_rotor\_3d


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### *Modeling Instructions*




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From the **File** menu, choose **New**.

#### **NEW**



In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**

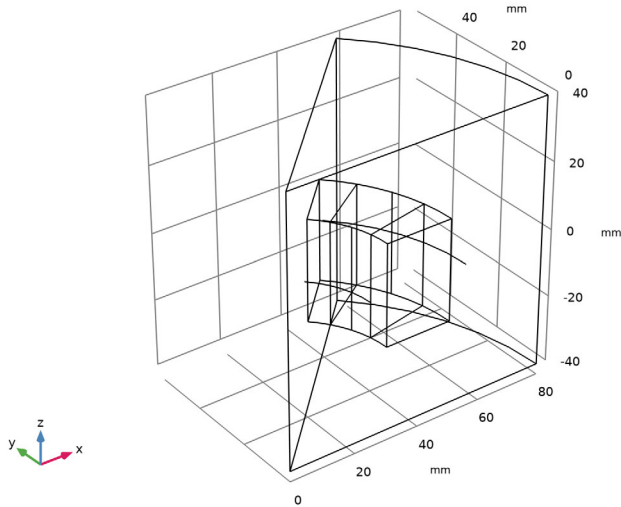
- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **AC/DC>Electromagnetic Fields>Magnetic Fields (mf)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Stationary**.
- 6 Click  **Done**.

#### **GEOMETRY I**

Insert the geometry sequence from the  
static\_field\_halbach\_rotor\_3d\_geom\_sequence.mph file.

- 1 In the **Geometry** toolbar, click **Insert Sequence** and choose **Insert Sequence**.
- 2 Browse to the model's Application Libraries folder and double-click the file  
static\_field\_halbach\_rotor\_3d\_geom\_sequence.mph.
- 3 In the **Geometry** toolbar, click  **Build All**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.


- 5 Click the  **Wireframe Rendering** button in the **Graphics** toolbar.





Define a selection for the magnets.

## DEFINITIONS


### *Magnets*


- 1 In the **Definitions** toolbar, click  **Explicit**.
- 2 Select Domains 2–4 only.
- 3 In the **Settings** window for **Explicit**, type Magnets in the **Label** text field.

### *Cylindrical System 2 (sys2)*

- 1 In the **Definitions** toolbar, click  **Coordinate Systems** and choose **Cylindrical System**.  
Define variables for the radial and azimuthal magnetic flux densities using the Vector Transform feature.
- 2 Click the  **Show More Options** button in the **Model Builder** toolbar.
- 3 In the **Show More Options** dialog box, in the tree, select the check box for the node **General>Variable Utilities**.
- 4 Click **OK**.

### *Vector Transform 1 (vectr1)*

- 1 In the **Definitions** toolbar, click  **Variable Utilities** and choose **Vector Transform**.
- 2 In the **Settings** window for **Vector Transform**, type B\_cyl in the **Name** text field.

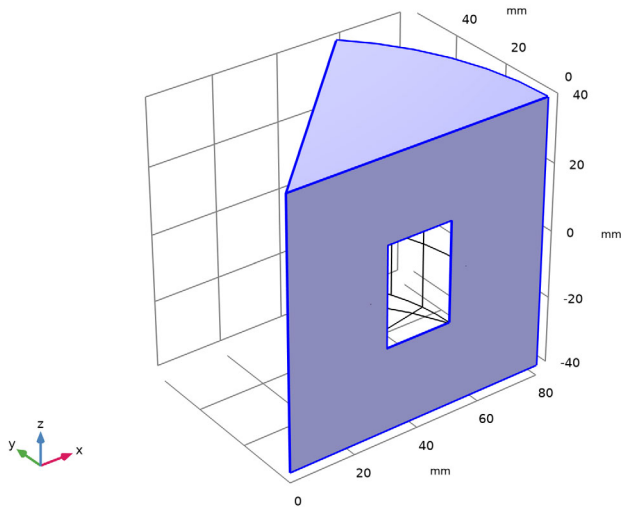
- 3 Clear all domains.
- 4 Click the  **Select All** button in the **Graphics** toolbar.
- 5 Click **Replace Expression** in the upper-right corner of the **Input** section. From the menu, choose **Component 1 (comp1)>Magnetic Fields>Magnetic>Magnetic flux density>mf.B - Magnetic flux density - T**.
- 6 Locate the **Output** section. From the **Coordinate system** list, choose **Cylindrical System 2 (sys2)**.
- 7 Locate the **Transform Settings** section. From the **Transform as** list, choose **Flux vector**.

#### *View 1*

Hide a few boundaries to view the results only in the inner part of the model domain.

#### *Hide for Physics 1*

- 1 In the **Model Builder** window, right-click **View 1** and choose **Hide for Physics**.
- 2 In the **Settings** window for **Hide for Physics**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 1, 2, and 4 only.



### **MAGNETIC FIELDS (MF)**

Now, set up the **Magnetic Fields** physics. Model the permanent magnets using the specific feature.




### *Magnet 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Magnetic Fields (mf)** and choose **Magnet**.
- 2 In the **Settings** window for **Magnet**, locate the **Domain Selection** section.
- 3 From the **Selection** list, choose **Magnets**.
- 4 Locate the **Magnet** section. From the **Direction method** list, choose **Specify by domains**.

### *Domain Direction 2*

In the **Physics** toolbar, click  **Attributes** and choose **Domain Direction**.

### *Magnet, Tangentially Magnetized*

- 1 In the **Model Builder** window, expand the **Component 1 (comp1)>Magnetic Fields (mf)>Magnet 1>Domain Direction 1** node, then click **Component 1 (comp1)>Magnetic Fields (mf)>Magnet 1>Domain Direction 2**.
- 2 In the **Settings** window for **Domain Direction**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Domain 3 only.
- 5 In the **Label** text field, type Magnet, Tangentially Magnetized.

### *North 1*

- 1 In the **Model Builder** window, expand the **Magnet, Tangentially Magnetized** node, then click **North 1**.
- 2 Select Boundary 10 only.

### *South 1*

- 1 In the **Model Builder** window, click **South 1**.
- 2 Select Boundary 15 only.

### *Magnet, Radially Magnetized*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Magnetic Fields (mf)>Magnet 1** click **Domain Direction 1**.
- 2 In the **Settings** window for **Domain Direction**, type Magnet, Radially Magnetized in the **Label** text field.



### *North 1*

- 1 In the **Model Builder** window, click **North 1**.
- 2 Select Boundaries 14 and 19 only.

### *South 1*

- 1 In the **Model Builder** window, click **South 1**.
- 2 Select Boundaries 5 and 22 only.

### **ADD MATERIAL**

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Built-in>Air**.
- 4 Right-click and choose **Add to Component 1 (comp1)**.
- 5 In the tree, select **AC/DC>Hard Magnetic Materials>Sintered NdFeB Grades (Chinese Standard)>N50 (Sintered NdFeB)**.
- 6 Right-click and choose **Add to Component 1 (comp1)**.
- 7 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.

### **MATERIALS**

#### *N50 (Sintered NdFeB) (mat2)*

- 1 In the **Settings** window for **Material**, locate the **Geometric Entity Selection** section.
- 2 From the **Selection** list, choose **Magnets**.

### **MESH 1**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.
- 2 In the **Settings** window for **Mesh**, locate the **Physics-Controlled Mesh** section.
- 3 From the **Element size** list, choose **Coarse**.

### *Size 1*

- 1 Right-click **Component 1 (comp1)>Mesh 1** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 From the **Selection** list, choose **Magnets**.
- 5 Locate the **Element Size** section. From the **Predefined** list, choose **Fine**.



Specify a very fine mesh on the curves where the magnetic flux density is to be evaluated. This helps to obtain a smooth curve for magnetic flux density.

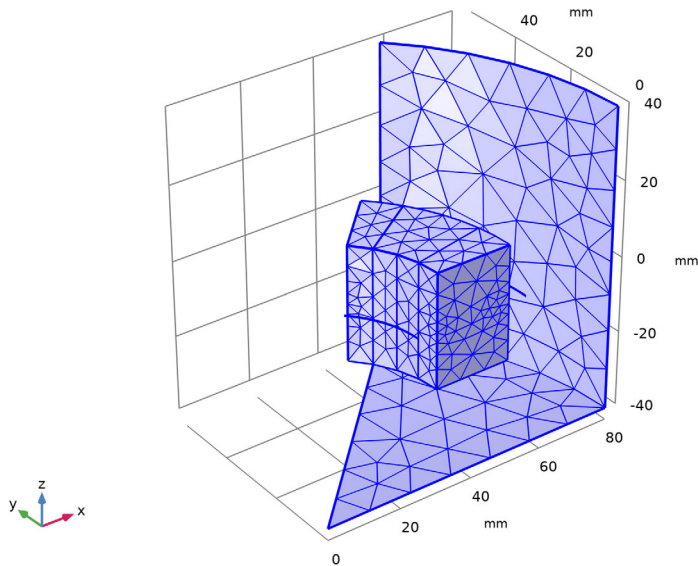
### *Size 2*

- 1 In the **Model Builder** window, right-click **Mesh 1** and choose **Size**.


- 2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Edge**.
- 4 Select Edges 6 and 31 only.
- 5 Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the **Element Size Parameters** section.
- 7 Select the **Maximum element size** check box. In the associated text field, type 0.5.

#### *Free Tetrahedral I*

- 1 In the **Mesh** toolbar, click  **Free Tetrahedral**.
  - 2 In the **Settings** window for **Free Tetrahedral**, click  **Build All**.
- Compare the mesh with the figure shown below.



#### **STUDY I**

- 1 In the **Model Builder** window, click **Study I**.
- 2 In the **Settings** window for **Study**, locate the **Study Settings** section.
- 3 Clear the **Generate default plots** check box.
- 4 In the **Home** toolbar, click  **Compute**.

## RESULTS

Use the Sector 3D dataset to produce a 3D dataset for the complete 3D model from the single-pole results.


### *Sector 3D 1*

- 1 In the **Model Builder** window, expand the **Results** node.
- 2 Right-click **Results>Datasets** and choose **More 3D Datasets>Sector 3D**.
- 3 In the **Settings** window for **Sector 3D**, locate the **Symmetry** section.
- 4 In the **Number of sectors** text field, type 8.
- 5 From the **Transformation** list, choose **Rotation and reflection**.
- 6 Click to expand the **Advanced** section. Select the **Define variables** check box.


The **Sector number** will be used later on, to get the right expression for  $B_{cyl.vphi}$  in [Figure 4](#).

Next, construct circles to visualize the magnetic flux density on the inside and the outside of the Halbach rotor.

### *Parameterized Curve 3D 1*


- 1 In the **Results** toolbar, click  **More Datasets** and choose **Parameterized Curve 3D**.
- 2 In the **Settings** window for **Parameterized Curve 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Sector 3D 1**.
- 4 Locate the **Parameter** section. In the **Name** text field, type  $\phi$ .
- 5 In the **Maximum** text field, type  $2\pi$ .
- 6 Locate the **Expressions** section. In the **x** text field, type  $55 \cdot \cos(\phi)$ .
- 7 In the **y** text field, type  $55 \cdot \sin(\phi)$ .

### *Parameterized Curve 3D 2*


- 1 In the **Results** toolbar, click  **More Datasets** and choose **Parameterized Curve 3D**.
- 2 In the **Settings** window for **Parameterized Curve 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Sector 3D 1**.
- 4 Locate the **Parameter** section. In the **Name** text field, type  $\phi$ .
- 5 In the **Maximum** text field, type  $2\pi$ .
- 6 Locate the **Expressions** section. In the **x** text field, type  $25 \cdot \cos(\phi)$ .
- 7 In the **y** text field, type  $25 \cdot \sin(\phi)$ .

Use the following instructions to reproduce the plot shown in [Figure 2](#).



### *B Field*

- 1 In the **Results** toolbar, click  **3D Plot Group**.
- 2 In the **Settings** window for **3D Plot Group**, type **B Field** in the **Label** text field.
- 3 Locate the **Data** section. From the **Dataset** list, choose **Sector 3D I**.

### *Slice I*


- 1 Right-click **B Field** and choose **Slice**.
- 2 In the **Settings** window for **Slice**, locate the **Plane Data** section.
- 3 From the **Plane** list, choose **xy-planes**.
- 4 In the **Planes** text field, type 1.
- 5 In the **B Field** toolbar, click  **Plot**.

### *Arrow Volume I*

- 1 In the **Model Builder** window, right-click **B Field** and choose **Arrow Volume**.
- 2 In the **Settings** window for **Arrow Volume**, locate the **Arrow Positioning** section.
- 3 Find the **x grid points** subsection. In the **Points** text field, type 60.
- 4 Find the **y grid points** subsection. In the **Points** text field, type 60.
- 5 Find the **z grid points** subsection. In the **Points** text field, type 1.
- 6 Locate the **Coloring and Style** section. From the **Color** list, choose **Black**.
- 7 In the **B Field** toolbar, click  **Plot**.
- 8 Click the  **Go to XY View** button in the **Graphics** toolbar.

Next, generate a plot for the radial magnetic flux density outside the Halbach rotor. Compare the result with [Figure 3](#).


### *Br vs. phi*

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type **Br vs. phi** in the **Label** text field.
- 3 Locate the **Data** section. From the **Dataset** list, choose **Parameterized Curve 3D I**.
- 4 Locate the **Plot Settings** section.
- 5 Select the **x-axis label** check box. In the associated text field, type **Angle (rad)**.

### *Line Graph I*


- 1 Right-click **Br vs. phi** and choose **Line Graph**.
- 2 In the **Settings** window for **Line Graph**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component I (comp I)>Definitions>**

**Vector Transform I (B\_cyl)>Transformed vector - T>B\_cyl.vr - Transformed vector, r-component.**


- 3 Locate the **x-Axis Data** section. From the **Parameter** list, choose **Expression**.
- 4 In the **Expression** text field, type  $\phi$ .
- 5 Locate the **y-Axis Data** section.
- 6 Select the **Description** check box. In the associated text field, type Magnetic flux density,  $r$  component.
- 7 In the **Br vs.  $\phi$**  toolbar, click  **Plot**.

Create the azimuthal magnetic flux density plot as shown in [Figure 4](#).

#### *B $\phi$ vs. $\phi$*

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type  $B\phi$  vs.  $\phi$  in the **Label** text field.
- 3 Locate the **Data** section. From the **Dataset** list, choose **Parameterized Curve 3D I**.
- 4 Locate the **Plot Settings** section.
- 5 Select the **x-axis label** check box. In the associated text field, type Angle (rad).

#### *Line Graph I*

- 1 Right-click **B $\phi$  vs.  $\phi$**  and choose **Line Graph**.
- 2 In the **Settings** window for **Line Graph**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component I (comp I)>Definitions>Vector Transform I (B\_cyl)>Transformed vector - T>B\_cyl.vphi - Transformed vector, phi-component**.
- 3 Locate the **y-Axis Data** section. In the **Expression** text field, type  $B_{cyl.vphi} * (1 - 2 * \text{mod}(\text{sec1number}, 2))$ .
- 4 Select the **Description** check box. In the associated text field, type Magnetic flux density,  $\phi$  component.
- 5 Locate the **x-Axis Data** section. From the **Parameter** list, choose **Expression**.
- 6 In the **Expression** text field, type  $\phi$ .
- 7 In the **B $\phi$  vs.  $\phi$**  toolbar, click  **Plot**.


Here, the expression  $B_{cyl.vphi} * (1 - 2 * \text{mod}(\text{sec1number}, 2))$  perhaps requires some additional clarification: The even sectors of the rotor are mirrored in the  $\phi$  direction, with respect to the odd ones. The original dataset contains the values of  $B_{cyl.vphi}$

for one odd sector only. The added correction term uses the modulus operator; it will flip between +1 and -1 every other sector.


The reason **Arrow Volume 1** did not need such data manipulation, is because it considers its input ( $m_f.B_x$ ,  $m_f.B_y$ ,  $m_f.B_z$ ) a vector field and is able to apply the transformation itself. **Line Graph 1** on the other hand, is in no way capable of relating its input to a certain "direction". It will therefore consider  $B_{cyl.vphi}$  a scalar.

Next, generate the polar plot of the magnetic flux density norm at a distance 55 mm away from the center of the rotor.

*normB vs. phi at r=55 mm*


- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **Polar Plot Group**.
- 2 In the **Settings** window for **Polar Plot Group**, type *normB vs. phi at r=55 mm* in the **Label** text field.
- 3 Locate the **Data** section. From the **Dataset** list, choose **Parameterized Curve 3D 1**.
- 4 Locate the **Axis** section. Select the **Manual axis limits** check box.
- 5 In the **r maximum** text field, type 0.56.

*Line Graph 1*

- 1 Right-click *normB vs. phi at r=55 mm* and choose **Line Graph**.
- 2 In the **Settings** window for **Line Graph**, locate the **θ Angle Data** section.
- 3 From the **Parameter** list, choose **Expression**.
- 4 In the **Expression** text field, type  $\phi$ .
- 5 In the *normB vs. phi at r=55 mm* toolbar, click  **Plot**.

Finally, reproduce the plot for the magnetic flux density norm at a distance 25 mm from the rotor center.

*normB vs. phi at r=25 mm*

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **Polar Plot Group**.
- 2 In the **Settings** window for **Polar Plot Group**, type *normB vs. phi at r=25 mm* in the **Label** text field.
- 3 Locate the **Data** section. From the **Dataset** list, choose **Parameterized Curve 3D 2**.
- 4 Locate the **Axis** section. Select the **Manual axis limits** check box.
- 5 In the **r maximum** text field, type 0.12.


*Line Graph 1*

- 1 Right-click *normB vs. phi at r=25 mm* and choose **Line Graph**.

**2** In the **Settings** window for **Line Graph**, locate the  $\theta$  **Angle Data** section.

**3** From the **Parameter** list, choose **Expression**.

**4** In the **Expression** text field, type  $\phi$ .

**5** In the **normB vs.  $\phi$  at r=25 mm** toolbar, click  **Plot**.

Compare this figure with that shown in [Figure 6](#).